STUDY OF PHOTOVOLTAIC DEVICES BASED ON METAL-SEMICONDUCTOR STRUCTURES

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CERTIFICATE

Certified that this work "STUDY OF PHOTOVOLTAIC

DEVICES BASED ON METAL SEMICONDUCTOR STRUCTURES" by

Miss Basabi Bhaumik has been carried out under my

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SYNOPSIS

STUDY OF PHOTOVOLTAIC DEVICES BASED ON METAL-SEMICONDUCTOR STRUCTURES

Ву

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Recently there has been an intense interest in utilising photovoltaic conversion of solar energy for terrestrial applications. This has led to the exploration of novel structures which would provide an alternative to the conventional P-N junction solar cells. Our interest in this thesis has been in studying some of these novel structures which are based on metal-semiconductor junctions and act as Schottky barriers or analogously related devices. Particular attention has been paid to the understanding of the following aspects of these novel structures.

1. The characteristics of the Schottky barrier solar cells (SBSC) are rather well known [1]. In the published literature, there are also some reports on the effect of temperature on the characteristics of these cells. For example, it has been reported that the short circuit current I_{SC} of silicon SBSC increases with increasing operating temperature. Following the concepts prevalent at that time (1975), the increase in I_{SC} has been attributed to the availability of extra photons, belonging to the long-wavelength range of the solar spectrum, due to the lowering

of the forbidden energy gap of silicon with increasing temperature. Our study [2], presented in Chapter 1 of the thesis, however, shows that the contribution to the increase of I_{SC} due to the mechanism mentioned above is negligible and cannot explain the experimental results. Instead, it has been found that good agreement with experimental results is obtained when the increase in I_{SC} with increasing temperature is calculated by taking the change of the absorption coefficient of the semiconductor with temperature at all wavelengths. This conclusion is not limited only to SBSCs but would be valid for P-N junctions or other type of cells made on indirect bandgap semiconductors like silicon.

2. The major disadvantage of SBSCs is due to their low open circuit voltage. There are two ways in which this can be obviated. One of these is by using Schottky (MIS) cells [1] and the other is by using Schottky (oppositely doped semiconducting interface) cells [3]. In the case of former cells, the performance critically depends on the thickness of the interfacial insulating layer. When this thickness is large, both the short circuit current and the open circuit voltage decrease leading to a decrease of the conversion efficiency. The mechanisms responsible for this behaviours have been found to be the variation of the 'illuminated barrier height' and that of the density-of-surface states with the variation of the thickness of the interfacial layer. The details of this analysis are given in the second chapter.

The other type of cells where an oppositely doped semiconducing interface layer is sandwitched between the metal and the bulk semiconductor have so far not received the attention they deserve. Keeping in view that the increase of effective barrier height, which is obtained due to the presence of a thin oppositely doped semiconducting interface, would be of interest not only from the point of view of solar cells but of many other devices where Schottky barriers are employed, we have developed a rather general method of analysis including the effect of mobile carriers for these devices [3]. This is given in the third chapter.

3. All the devices mentioned above require a very thin film of metal to form the Schottky barrier because these films have to be transparent to light. This places stringent demand on the choice of the metal because it is required to simultaneously meet the optical, electrical and mechanical criteria. A way out would be to use a lateral (gridded) structure where the metal film is not thin and continuous, but thick and very finely gridded. Since the carriers are photogenerated in the area where there is no metal and are laterally collected by the thick film of metal forming the Schottky barrier, we call this a lateral SBSC. Its analysis entails the solution of a two-dimensional continuity equation. A further complication arises because all the boundary conditions are not known. A method of analysis which assumes the functional form of the

boundary condition has been developed [4] and is given in the fourth chapter. It allows the determination of the boundary condition by proper matching and leads to the solution of the continuity equation. A brief summary of the properties of different types of cells considered in this thesis is given in the concluding fifth chapter.

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CHAPTER 1

SCHOTTKY BARRIER SOLAR CELLS

Introduction

The photovoltaic effect in semiconductor P-N junctions is well known and has been extensively utilized for power generation using solar energy in space. Lately there have been attempts to use this phenomenon for terrestrial generation of electrical power. The main impediment towards this, which again is well known, is the cost. To overcome this impediment two major approaches have been taken; first approach is towards cutting down the cost of P-N junction photovoltaic cells and the other approach is to search for novel structures which may prove viable. The work in this thesis is concerned with the latter approach [1-5].

The structures that have been investigated are based on the photovoltaic properties of Schottky barrier (metal-semiconductor) diodes and related devices like metal-(thin) insulator-semiconductor, metal-(thin)P-N, metal-(thin)N-P, metal-(thin) insulator-(thin)P-N and metal-(thin) insulator-(thin)N-P diodes and are given in Chapters 1, 2 and 3. A common disadvantage of all these devices is that they require a very thin metallic film which is almost transparent to light. This thin metal film has different lattice constant and different temperature coefficient of expansion from the

substrate and has to undergo temperature cycling during actual operation. Thus, there are chances that the metallic film would peel off, affecting the durability of these types of cells. This can be obviated by evaporating a very closely spaced metallic grid structure which can be thick, rather than evaporating the conventional continuous metallic layer which has to be thin [3,6,7]. In the case of gridded structure, the carriers are photogenerated in the exposed region of the semiconductor and are laterally collected by the metallic strip forming a contact based on any of the structures mentioned above. Such a cell has been called a lateral cell and, as is obvious, it entails a two-dimensional analysis [3]. This is the subject matter of Chapter 4. We start the considerations of this chapter with a study of Schottky barrier solar cell.

1.1 Schottky Barrier Solar Jell (SBSC)

A good review of Schottky barrier solar cell (SBSC) is available in the book by Hovel [8]. Here we mention those aspects which are either required later or are necessary for the sake of completeness. A particular aspect needed later concerns the temperature variation of the characteristics of solar cells. Though the development given in this chapter is in the context of SBSC, the arguments are general enough to hold in the case of other photovoltaic structures also. The consideration of dependence of performance on temperature

has been necessitated by the fact that in actual operation the operating temperature of a solar cell keeps on changing. A perusal of the literature showed that there were some ambiguities regarding the physical mechanisms responsible for the dependence of the characteristics of SBSC on temperature. A clarification of these [1] is given in Section 1.3, and is preceded by a brief historical comment and the derivation of the current voltage characteristics of SBSC.

The photovoltaic properties of those metal semiconductor contacts which form a Schottky barrier have been known for a fairly long time [9]. At an earlier stage of development these were mostly used as photodiodes. basic operative mechanism of this system as photovoltaic device for energy conversion has been discussed by Lehovec [10] in 1948. However, barring these sporadic efforts, till recently no systematic attempt had been made to correlate the output characteristics of these devices with the process of fabrication. The recent resurgence of interest in the photovoltaic conversion of solar energy and ensuing search for photovoltaic structures which would provide alternatives to conventional P-N junction solar cells have, however, changed this picture. An important step in this direction was the theoretical analysis of Pulfrey and McQuat[11] which showed that under ideal conditions the efficiency of a Schottky

barrier solar cell (SBSC) would be comparable to that of a P-N junction solar cell. Added to this is the advantage that the fabrication of SBSC would be simpler and processing could be done at lower temperature. In actual practice, however, the conventional SBSC has not lived upto the promise due to its low open circuit voltage and the ensuing lower efficiency. The structure that seem to be viable are based on the analogous metal-(thin) insulator-semiconductor and are called tunnelling MIS (or MOS) diodes. These have higher open circuit voltage and efficiency as compared to SBSC. We would take up their study in the next chapter after studying the behaviour of SBSC, which is simpler, in this chapter.

A convenient, but round-about, way of coming to the operative mechanisms of SBSC is through those of a P-N junction solar cell which are more widely known. The energy band diagram of a P-N junction with light incident on it from the left is shown in Fig. 1.1(a). Here, the photons which have energy larger than the bandgap of the semiconductor create electron-hole pairs. The electric field in the region of the metallurgical junction acts to separate the pairs which are generated in the depletion region, and provide drift field for the minority carriers which manage to diffuse to the edges of the depletion regions on both P and N sides. Finally the separated carriers are collected by the two ohmic contacts, one on the back side (N side) being continuous and the other on the front (P side) being gridded to let the light in. In

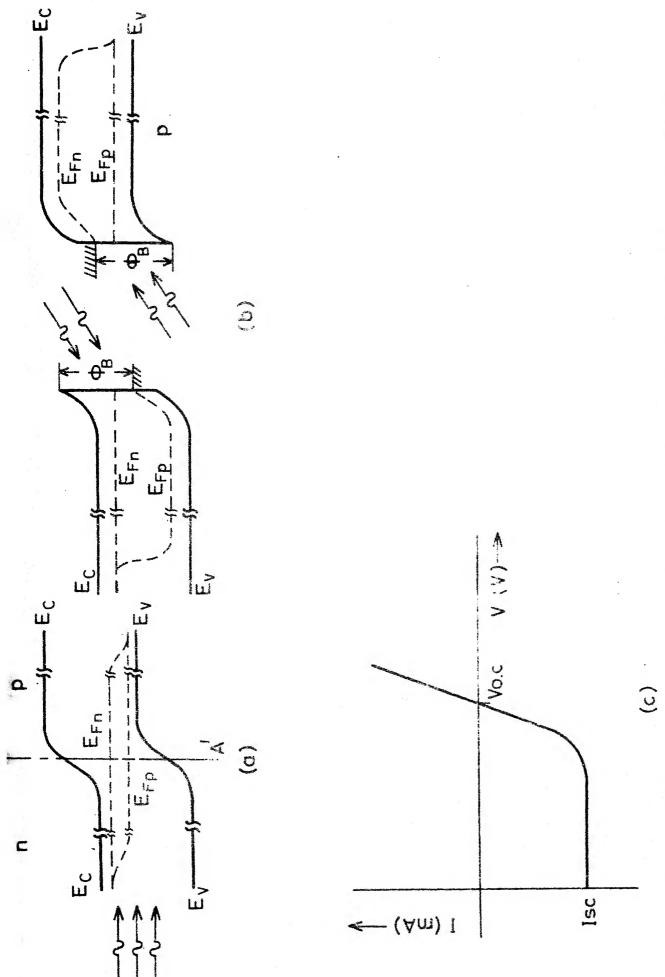


Fig.1.1 Energy band diagram of (a) a p-n junction solar cell,(b) a metal-n semiconductor and a metal-p semiconductor schottky barrier solar cell,(c) Typical 1-V characterstics of solar cell

summary, the operation of a photovoltaic cell requires the photo-generation of electron-hole pairs, their separation by an electric field and the collection of these separated carriers by the metallic contacts so that they can flow through the external circuit. In addition one of the metallic contacts should be in position to let the light in, i.e. either it has to be very thin or of gridded structure.

For a moment let us now imagine that the P-N junction is sectioned at plane AA' and light is incident from the left of plane AA'. When one considers the possibility of using this structure for photovoltaic conversion one finds that it meets the necessary conditions of generation of electron-hole pairs and their separation by an electric field, but does not meet the requirement of proper collection of the photogenerated carriers. Of course, there is the question that in the absence of P semiconductor how has the band bending to the right of AA' been obtained. Both this and the requirement of collection can be simultaneously met if one puts metallic contact at AA' so that it forms a Schottky barrier as shown in Fig. 1.1(b). It is needless to say that this metallic contact should be almost transparent to the incident radiation. This is the basic principle of operation of a Schottky barrier solar cell (SBSC) based on metal-N type structure. If we repeat, our argument by looking to the left of AA' and by considering light incident from right, a metal-P type SBSC can be observed.

The considerations given above clearly show the analogy between SBSC and P-N junction solar cells. Thus they allow us to carry through, but with caution, many of the concepts developed for the latter in the case of SBSC also.

1.2 I-V Characteristics of SBSC

Here there are two cases of interest. (i) The diode is forward biased by an applied voltage V and an I-V relation ensumes. There is no illumination hence we would call this as the characteristics of the 'dark'diode. (ii) The diode gets forward biased at a voltage V by the connection of a load R_L in the presence of illumination. Part of the I-V characteristic is in the fourth quadrant and would be denoted as the characteristics of the 'illuminated' diode. We take up the case of dark diode first.

1.2.1 Dark current of Schottky barrier

Current voltage characteristics of dark Schottky barriers have been well studied in the published literature [12]. Most of these studies are limited to small area diodes so that the fluctuations of any parameter on the diode do not complicate the properties. By necessity, solar cells have to be of comparatively larger area and due to this some new considerations come in. These considerations have been briefly pointed outafter first giving a method to determine the mechanism of current transport in diodes which have homogeneous properties.

It is by now well established that depending upon the barrier height, doping, temperature and applied bias the mechanism of current transport through a Schottky barrier diode can either be thermionic emission (TE), thermionic field emission (TFE) or field emission (FE). It would be of interest to find a method so that by making measurements on a finished Schottky barrier one could determine as to which one of the three mechanisms mentioned above is operative in the diode. Such a method has been suggested by Saxena [13]. The method consists of experimentally plotting a graph of nT versus T where n is the ideality factor of the diode. A typical plot of this is shown in Fig. 1.2. The graph I corresponds to the case of an ideal thermionic emission with n=1, whereas graph II also corresponds to thermionic emission but with n > 1. There is one more case shown by graph III where thermionic emission is the mechanism, but this graph does not pass through origin, rather it is parallel to n=1 line. This is the Case of 'T' anamoly and has been discussed by several workers [14 a, 14b].

In the case that the thermionic field emission is the mechanism of current transport through the diode under consideration one obtains graph IV as the plot, whereas in the case of the field emission graph V results. Thus, one sees that the plot of nT versus T provides a simple method for knowing the mechanism of current transport. However, the perusal of recent literature shows that there have been some

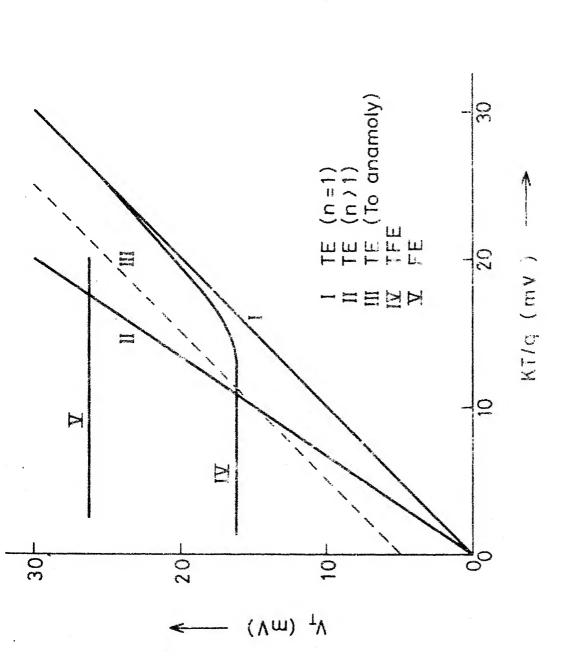


Fig. 1.2 Plot of V versus (KT/q) to determine the mechanism of current transport in Schottky Barriers (See Text)

ambiguities in this regard. A case in point is the experimental results of Vernon and Anderson [15]. They have fabricated large area Schottky barrier solar cells and in order to determine the mechanism of current transport in their samples. they have plotted nT versus T from the I-V characteristics of They have found this plot to be independent of temperature and have concluded therefrom that field emission is the dominant mechanism of carrent transport. This conclusion. however, seems to be suspect because neither is the semiconductor degenerately doped nor is the temperature low enough for field emission to dominate in current transport. true that if one only considers the conventional mechanisms (thermionic emission, thermionic field emission, and field emission) of current transport in a Schottky barrier diode, one is left with no choice but to conclude that the mechanism in this case is field emission. It should be noted, however, that the SBSC's are large area devices with no guard rings. In a large area device it is quite possible that the barrier height is not uniform over the whole sample. Johnson etal. 161, in a different context, have investigated the effect of the variation of barrier height on the I-V characteristic of a metal-semiconductor junction. In some cases they have observed that the plot of the product of the temperature and the slope of the I-V characteristic versus temperature is independent of temperature and have ascribed this to the variation of barrier height. Although the argument is not conclusive, it

may be that this rather than field emission is the controlling mechanism of current transport in large area SBSC's.

Thus it is evident that in the case of large area

Schottky barrier diodes great care must be exercised in using
the method of Saxena to determine the mechanism of current
transport. This has been followed through by another worker
of our group[17]. In this thesis, however, unless otherwise
specified, we would take the mechanism of current transport
to be thermionic emission and use the equation:

$$I = I_0 \left[\exp(qV/nkT) - 1 \right]$$
 (1.1)

where $I_0 = aJ_0$, a being the area of the diode and

$$J_{O} = A^{**}T^{2}[\exp(-q\phi_{R}/kT)]$$
 (1.1a)

for the dark current of SBSC. Here A** is the Richardson constant, ϕ_B is the barrier height, T is temperature, Q is the charge of electron and k is the Boltzmann constant. The value of n would be taken to be unity—unless otherwise specified.

1.2.2 I-V characteristics of SBSC

The typical nature of current voltage characteristic in the presence of illumination is shown in Fig. 1.1(c). At a given load $R_{\rm L}$, a voltage V is developed across the cell. For the present let us assume that the effect of the series and shunt resistances and the recombination of photo-generated

carriers in the depletion region and at the interface are negligible. Under these conditions, the following analysis holds. At the voltage V, let the current be I and the current density be J for a given area a. Let us consider a metal-P semiconductor Schottky barrier cell. At any cross-section of the cell, we have

$$J = J_p(x) + J_n(x)$$
 (1.2)

where $J_p(x)$ is due to the flow of majority carriers and under the assumptions given above, can be obtained from eqn.(1.1). $J_n(x)$ is due to the flow of minority carriers and is determined below. In general, it is given as:

$$J_n(x) = J_{nD}(x) + J_{nQ}(x) + J_{R1}(x) + J_{R2}(x)$$
 (1.2a)

where $J_{nD}(x)$ is the current due to the photo-generated carriers in the depletion region, $J_{nQ}(x)$ is due to diffusion of photo-generated carriers in the quasi-neutral region just beyond the depletion region, $J_{R1}(x)$ and J_{R2} are due to the recombination of carriers in the depletion region and at the interface, respectively. As mentioned earlier, here we would neglect the contribution of $J_{R1}(x)$ and J_{R2} . The expressions for $J_{nQ}(x)$ and $J_{nD}(x)$ are developed below. Under ecommonly employed assumptions [18] $J_{nQ}(x)$ can be obtained by using the continuity equation for the excess minority carriers n_D which is given as [1]

$$D_{n} \frac{d^{2}n_{p}}{dx^{2}} - \frac{n_{p}}{\tau_{n}} + Q(\lambda) \left\{1 - R(\lambda)\right\} \alpha(\lambda) \exp\left\{-\alpha(\lambda)(x+b)\right\} = 0 \quad (1.3)$$

Here b is the width of the depletion region (Fig.1.3a) and other symbols are explained in the first of all, let us consider eqn.(1.3) when the cell is short circuited.

The boundary conditions are

at
$$x = b$$
; $n_p = N$ (1.4)

at
$$x = W$$
; $D_n \frac{dn_p}{dx} \Big|_{x=W} = -s n_p(W)$ (1.5)

Here s is the surface recombination velocity at x=W and W is the total width of the semiconductor. A comment on the choice of the boundary conditions at x = b is given later. For the present we note that the solution of eqn.(1.3) with constraints of eqns. (1.4) and (1.5) is given as

$$n_{p} = c_{1} \exp(x/L_{n}) + c_{2} \exp(-x/L_{n}) + \frac{Q(1-R) \alpha \exp(-x)}{D_{n}(\frac{1}{L_{n}^{2}} - \alpha^{2})}$$
(1.6)

where

$$c_{1} = \chi\{ [(\alpha D_{n} - s) \exp\{-(\frac{b}{L_{n}} + W)\} + (s + \frac{D}{L_{n}}) \exp(-\alpha b)$$

$$\exp(\frac{W - 2b}{L_{n}})^{\frac{1}{2}} / 2A - \exp(-\{\frac{b}{L_{n}} + \alpha b\}) \} + N \exp(-\frac{b}{L_{n}})$$

$$\{1 - [(s + \frac{D}{L_{n}}) / 2A] \exp(\frac{W - b}{L_{n}}) \}$$

$$(1.6a)$$

$$c_{2} = -\chi \left[\left(\alpha D_{n} - s \right) \exp(-\alpha W + \frac{b}{L_{n}}) + \left(s + \frac{D}{L_{n}} \right) \exp(-\alpha b + \frac{W}{L_{n}}) \right] / 2A$$

$$+ N(s + \frac{D}{L_{n}}) \exp(W/L_{n}) / 2A$$
(1.6b)

where

$$\chi = Q(1-R) \alpha / D_n(L_n^{-2} - \alpha^2)$$
 (1.6c)

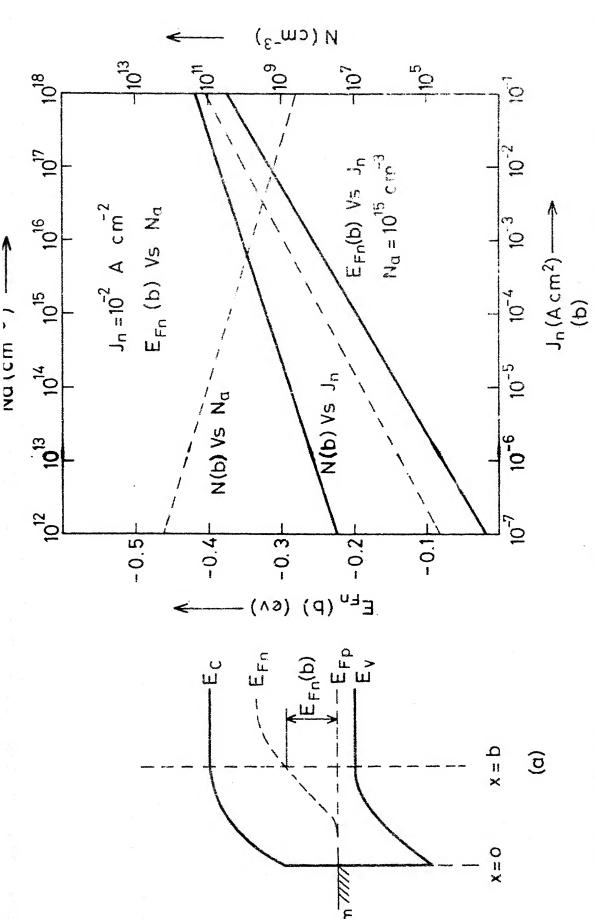


Fig.1.3(a) Energy band diagram of a P-semiconductor diode showing the quasi fermi levels. (b) Plot of $E_{Fn}(b)$ and N versus $J_n(\mathbf{o}r N_a)$. (Seetext).

$$A = s \sinh [(W-b)/L_n] + \frac{D_n}{L_n} \cosh [(W-b)/L_n]$$
 (1.6d)

From eqn. (1.6) one obtains the short circuit current $I_{SCQ}(x)$ as:

$$I_{SOQ}(\lambda) = qaD_n \frac{dn_p}{dx} \Big|_{x=b}$$

$$= qaQ(1-R) \frac{\alpha L_n \exp(-\alpha b)}{(1-\alpha^2 L_n^2)} \Big[\frac{(\alpha D_n - s)}{A \exp(\alpha W)} + \frac{\frac{B}{A} - \alpha L_n}{\exp(\alpha b)} \Big] + C$$

$$(1-7)$$

where $L_n^2 = D_n \tau_n$, a is the area of the cell and

$$B = s \cosh[(W-b)/L_n] + (D_n/L_n) \sinh[(W-b)/L_n]$$
 (1.7a)

$$C = \frac{qaD_{n}N}{L_{n}} \left[1 - \frac{D_{n}}{A} \left(\frac{s}{D_{n}} + \frac{1}{L_{n}}\right) \exp\left(\frac{W-1b}{L_{n}}\right)\right]$$
 (1.7b)

Note that inadvertently a printing error in eqn.(1.7b) has appeared in Ref. [1]. The corrected equation is given here.

Before proceeding further we would like to comment on the component C of short circuit current. It is customary in the case of short circuited cell to take N = O in the boundary condition at x=b (eqn. 1.4), in which case C becomes zero. The fact that N is non-zero even in the case of a short circuited cell can be seen as follows [19-21]. Let us consider the energy band diagram of a metal P semiconductor Schottky barrier solar cell shown in Fig. 1.3(a). The considerations for the metal N-semiconductor SBSC are very similar. At the metal-semiconductor interface the minority carrier _imref E_{Pn}

is shown to merge with the metal Fermi level E_{Fm} , indicating an infinite recombination velocity. Following an analysis similar to that of Card [19], it can be shown that the minority carrier imref E_{Fn} does not remain constant in the depletion region as is commonly assumed. Let us take the reference of energy at the metal Fermi level and denote the value of E_{Fn} at the edge of the depletion region at x = b by $E_{Fn}(b)$. The minority carrier current density in the absence of recombination is given by

$$J_{n} = q n \mu_{n} \frac{d E_{Fn}}{dx}$$
 (1.8a)

where

$$n = N_{C} \exp\left(-\frac{E_{C} - E_{Fn}}{kT}\right)$$
 (1.8b)

The symbols are defined in Appendix A.

Using eqn. (1.8), rearranging, and integrating for 0 < x < b one gets

$$\int_{0}^{b} \frac{J_{n}}{N_{C} \mu_{n}} \exp(E_{C}/kT) dx = \int_{E_{Fn}(0)}^{E_{Fn}(b)} \exp(E_{Fn}/kT) dE_{Fn}$$
 (1.9a)

Evaluating this, and making some simplifying assumptions, one obtains:

$$\exp(\frac{E_{Fn}(b) - E_{Fn}(o)}{kT}) - 1 = J_n N_a^{\frac{1}{2}} (1/n_{i}^2 \mu_n) (\pi \epsilon_s / 2q^2 kT)^{\frac{1}{2}} \exp[\frac{-E_{Fn}(o)}{kT}]$$
(1.9b)

In metal P semiconductor Schottky barrier diodes, $\mathbb{E}_{\mathrm{Fn}}(\circ)=0$. Using this, one obtains the equivalent expression of Card [19].

In the case of metal N-type contacts, eqn. (1.9b) still holds with E_{Fn} , N_a and μ_n replaced by $-\vec{R}_{Fp}$, N_d and μ_p respectively.

A plot of $\mathbb{E}_{Fn}(b)$ as a function of photo-generated current density J_n using eqn.(1.9b) is given in Fig.1.3. Also shown on this graph is the value of N given as

$$N = N_C \exp [-(E_G - E_{Fn}(b) - qV_p)/kT]$$
 (1.10a)

=
$$n_{po} \exp [E_{fn}(b)/kT]$$
 (1.10b)

where qV_p is the difference between Fermi level and the valence band. The existence of non-zero value of N in the case of short circuited photodiode was first noted by Berry [20] in the case of P-N junctions, and the numerical value of N was deduced from the short-circuited photocapacitance of commercial solar cells. The value obtained in this case was $N = 10^{14}$ cm⁻³. Moore [21] suggested that the analytical model of Berry based on depletion region photo-capacitance was not correct, rather a diffusion model of photocapacitance should be used. This correction gave a value of $N \approx 10^{11}$ cm⁻³. The point to note is that if one evaluates the current component C using N = 10^{11} cm⁻³ then the contribution of the term is negligible compared to the other terms. Hence the presence of N in the case of Schottky barrier solar cells is only of academic interest. However, this term becomes of considerable significance in the case of MIS solar cells as would be shown in the next chapter.

There we would use an expression for the current density J_{diff} which is equal to (-C/a) where C is given by eqn.(1.7b). If we evaluate the current C by assuming that W >> L_n such that the recombination velocity s at the contact x = W does not come into picture, one obtains a modified form of eqn.(1.7b) as

$$C = \frac{q \times p_n}{L_n} (N - n_{po})$$

Use of eqn. (1.10b) in this expression gives an expression for J_{diff} , which has been defined above, as:

$$J_{diff} = -C/a = \frac{q D_n}{L_n} n_{po} \{ exp(\frac{E_{Fn}(b)}{kT}) -1 \}$$
 (1.11a)

In the case of a metal N semiconductor Schottky barrier diode eqn.(1.11a) gets modified as:

$$J_{diff} = -C/a = q \frac{D_p}{L_p} p_{no} \{ exp (-\frac{E_{Fp}(b)}{kT}) -1 \}$$
 (1.11b)

where $\mathbf{E}_{\mathrm{Fp}}(\mathbf{b})$ < 0, if metal Fermi level is taken to be the reference energy. As already mentioned, these equations would be used in the next chapter while analysing Schottky (MIS) solar cells.

The current generated in the space charge region (0 < x < b) when recombination is neglected is given by

$$I_{SCD}(\lambda) = q a \{ 1-R(\lambda) \} \int_{0}^{b} Q(\lambda) \alpha(\lambda) \exp\{-\alpha(\lambda)x\} dx$$
(1.12)

The total current $I_{SC}(\lambda)$ for a monochromatic light of

wavelength λ is given by the sum of eqns. (1.7) and (1.12) as

$$I_{SC}(\lambda) = I_{SCQ}(\lambda) + I_{SCD}(\lambda) = a J_L(\lambda) + C$$
 (1.13)

This current has been evaluated for a metal I-silicon Schottky barrier solar cell and the values are given when we calculate the efficiency of the cell.

Having obtained the short circuit current let us obtain the open circuit voltage. This can be obtained by equating the sum of the majority and minority carrier currents to zero and solving for the voltage. The majority carrier component can be obtained either by using the thermionic emission model or by diffusion model of current transport. If thermionic emission model is used then the use of eqn.(1.1) and (1.3) gives the total current as

$$I = I_0 [\exp(qV/kT) -1] - I_{SC}$$
 (1.14)

By equating I=0 and solving for V one gets the well known expression for V_{OC} as

$$V_{O\ddot{U}} = \frac{n kT}{q} \ln \left[1 + \frac{I_{S\dot{U}}}{I_{O}} \right]$$
 (1.15)

An expression for $V_{O\!O}$ using the diffusion model of the majority carrier transport has been obtained by Dubey and Paranjape [22]. They have used a method of boundary matching and obtained the expression of $V_{O\!O}$ in terms of a recombination velocity at the metal semiconductor interface.

However, for the parameters that are commonly useful in solar cells, it is more likely that thermionic emission model rather than diffusion model would hold true, hence we would use eqn. (1.15) for $V_{\rm OC}$.

To complete the analysis, we want to obtain an expression for the efficiency of the cell. This can be done in the conventional manner using eqn. (1.14). The power output is given by P = IV and the voltage V_{mp} , at which the maximum power is available, is obtained by solving for $\partial P/\partial V = O$. This leads to a transcendental equation

$$(1 + \frac{qV_{mp}}{kT}) \exp(\frac{qV_{mp}}{kT}) = (1 + \frac{I_{SC}}{I_{O}})$$
 (1.16)

where I_0 is the reverse saturation current of the diode and I_{SC} is obtained by integrating eqn. (1.13) over the range of wavelength of interest.

Using the value of V_{mp} obtained from eqn. (1.16) in eqn. (1.14) the value of the current I_{max} at the maximum power point can be obtained. The expression for the efficiency (η) is now obtained as

$$\eta = \frac{I_{\text{max}} V_{\text{max}}}{aP_{in}} = (F.F.) \frac{I_{\text{SC}} V_{\text{OC}}}{aP_{in}}$$
(1.17)

where P_{in} is the intensity per unit area of the incident light and F.F. is the fill factor, which is given by the ratio

$$F.F. = \frac{I_{\text{max}} V_{\text{max}}}{I_{\text{SC}} V_{\text{OC}}}$$
 (1.18)

It is important to point out here that the theoretically calculated efficiency of the same system using eqn.(1.17) can vary between wide limits depending upon the assumptions made and the values of parameter assumed. For example, for cells made on N-type silicon the values of efficiency ranging from approximately 20% [11] (obtained for the equilibrium barrier height \emptyset_B of the order of the energy gap $\mathbf{E}_{\mathbf{C}}$ and assuming negligible recombination and unit quantum efficiency) to 5% [23] (in the case of gold silicon contact taking incomplete absorption and some recombination into account) has been Thus, caution must be exercised in completly reported. specifying the conditions under which a number for efficiency has been obtained from the theoretical calculations. It is also worthwhile to note here that during the earlier stages of the development of SBSC's, one very intriguing feature had appeared. It had been found that the experimentally obtained efficiencies where higher than theoretical efficiencies calculated taking realistic assumptions into account. It was soon realized that this situation had arisen because the experimental cells were not actually Schottky barrier cells for which the theoretical model was built. The presence of the thin oxide layer formed during processing, between the metal and silicon, had given rise to tunneling MIS solar cells which requires different modelling than SBSC's. A calculation of the efficiency for a SBSC made on P-type silicon and operating at 300°K has been done as follows:

- (i) $I_{SC}(\lambda)$ has been evaluated from eqn.(1.13) using the following values of parameters, $D_n=10~{\rm cm}^2/{\rm sec.}$, $L_n=100~{\rm \mu m}$, s = $10^4~{\rm cm/sec.}$, W = 200 ${\rm \mu m}$, a = 1 cm, b = 1 ${\rm \mu m}$. Q(λ) corresponding to AMO sunlight [24] and the values of $\alpha(\lambda)$ from Dash and Newman [25] have been used. The total short circuit current has been obtained by integrating $I_{SC}(\lambda)$ from $\lambda=0.4$ /m to $\lambda=1.1$ /m. This calculation gives $I_{SC}=25~{\rm mA/cm}^2$ for R = 0.1 and 16.5 mA/cm² for R = 0.4
- (ii) Before calculating V_{OC} from eqn. (1.15), we want to a note some of its features. If $(I_{SC}/I_0) >> 1$, and $I_0 = aJ_0$, where J_0 is given by eqn. (1.1a),

$$V_{OC} = n \beta_B + \frac{nkT}{q} \ln \left[\frac{I_{SC}}{aA * * T^2} \right]$$
 (1.19)

Taking $I_{SC}=25$ mA/cm², a=1 cm², A^{**} = 32 Amp/cm²/°K², n = 1, and T = 300°K, one gets:

$$V_{OC} = \emptyset_B - 0.5 \text{ volts}$$

If one takes $\emptyset_B = E_G = 1.12$ eV, then $V_{OC} = 0.62$ V and if $\emptyset_B = 0.8$ eV then $V_{OC} = 0.3$ V. Thus it is apparant that for realistic values of barrier heights the open circuit voltage of SBSC would be very small as compared to that of P-N junction solar cells. This is a serious limitation of SBSC and has limited its usefulness.

(iii) The calculated values of the efficiency of SBSC would depend upon the choice of \emptyset_B . If we take $\emptyset_B = \mathbb{E}_G$ we get $\eta = 6.5\%$ for R = 0.0 which is an upper limit on the efficiency in this case.

1.3 Variation of Parameters of SBSC with Temperature

The main reason for the interest in the study of temperature dependence of performance of a solar cell is due to the fact that in actual operation it has to undergo temperature cycling. Naturally this problem had attracted attention at an early stage of the development of solar cells Recently, Vernen and Anderson [15] have experimentally measured the temperature dependence of the short circuit current, open circuit voltage and some other parameters of silicon SBSC's. Let us consider first the variation of the short circuit current Isq. It has been found that it increases with increasing temperature [15] . The explanation given for this increase is that as temperature increases the bandgap $\mathbf{E}_{\mathbf{G}}$ decreases, thus making the absorption of some more photons of longer wavelengths, which were unutilized earlier, possible. Particularly for their data, Vernan and Anderson have suggested that "the increase in \mathbf{I}_{SC} can be accounted for by 100°C temperature increase producing a 0.03 eV decreased energy gap and 0.03 µm increased useful wavelength range". That this is not the case can be physically seen from the following arguments.

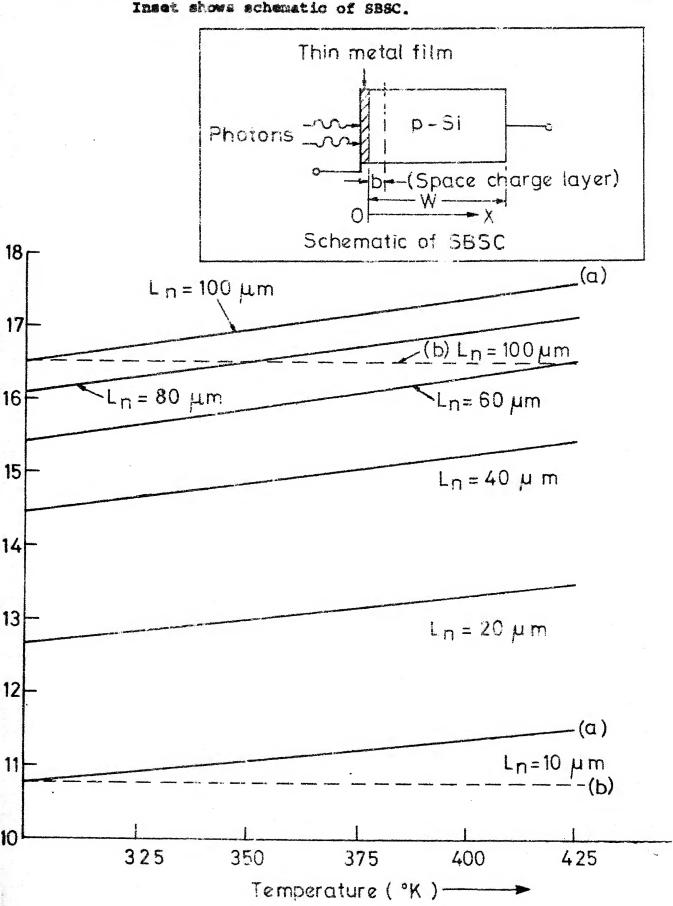
Let $\lambda_1^{T_1}$ be the wavelength of the photons corresponding to $\mathbf{E}_{\mathbf{G}}$ at temperature \mathbf{T}_1 and $\lambda_2^{T_2}$ be the wavelength of the photons corresponding to $\mathbf{E}_{\mathbf{G}}$ at temperature \mathbf{T}_2 .

For silocon: $\lambda_1^{T_1} = 1.1 \mu \text{ m at } 300^{\circ}\text{K}$ and $\lambda_2^{T_2} = 1.13 \mu \text{ m at } 400^{\circ}\text{K}$. Here use has been made of the expression [27]

$$E_{G}(T) = E_{G}(0) - \frac{\alpha T^{2}}{(T + \beta)}$$
 (1.20)

where for silicon $\alpha=7.02$ x $10^{-4}(\text{eV/oK})$; $\beta=1108\text{oK}$ and $E_G(0)=1.16$ eV. This expression for $E_G(T)$ is valid for 0° to 900oK.

The value of the absorption coefficient at $\lambda \approx 1.1 \, \mu \, \text{m}$ for silicon is around 10 cm^{-1} [25], which means that the photons at these wavelengths would be absorbed at a depth of 1000μm. For good silicon crystal the diffusion length is of the order of 100 \mu m. Hence it is evident that photocarriers generated at these wavelengths can not contribute to the short circuit current and thus do not account for the experimentally obtained value of $dI_{\rm SC}/dT$. Instead, in the present work, it has been found [1] that for the range wavelengths (λ) of solar radiation useful for photogeneration in silicon, the increase in the absorption coefficient α with increase in temperature is the dominant mechanism which gives rise to the increase of I_{SC} with temperature. To show this the expression for $I_{SC}(\lambda)$ as the sum of eqns. (1.7) and (1.11) is used. At each temperature, $I_{\rm SC}(\ \lambda)$ is integrated over the whole useful wavelength range. By repeating the process at different temperatures, the temperature dependence of I_{SC} is obtained. The results of the computations are shown in Fig. 1.4.



The computations for $I_{SC}(\lambda)$ have been done for an area a of 1 cm 2 and between the temperatures 300° and 425°K. D_n and S_n have been taken [28] to be 10 cm 2 sec $^{-1}$ and 10 4 cm sec $^{-1}$, respectively. I_n is treated as a parameter ranging from 10 to 100 μ m. The width W = 200 μ m and the width of the depletion region b = 1 μ m. The temperature variation of E_G for silicon is already given by eqn.(1.20). $Q(\lambda)$ corresponding to AMO sunlight has been used, and it has been assumed that the transmittance of the thin metal film is unity over the whole range and there is 40% reflection at the metal semiconductor interface. The value of the absorption coefficient α (λ) at different temperatures has been evaluated by using the equation $\{29,30\}$

$$\alpha = \sum_{i} \left[\frac{\left(h\nu - E_{G} + K \theta_{i}\right)^{2}}{\exp(\theta_{i}/T) - 1} + \frac{\left(h\nu - E_{G} - K \theta_{i}\right)^{2}}{1 - \exp(-\theta_{i}/T)} \right] C_{i} \quad (1.21)$$

Here hv is the energy of photons, KO_{i} is the energy of phonons, i is the index for different types of phonons participating in the process, and C_{i} is a constant. We have taken $C_{i} = 4.5 \times 10^{3} \text{ cm}^{-1} \text{ eV}^{-2}$ over the whole range of wavelengths and temperatures. This value of C_{i} has been obtained by comparing eqn.(1.21) with the data of Dash and Newmann [25] and by considering the proper threshold energies for different type of phonons as given by MeLean [31]. The value of θ_{i} in the range 1.175-1.21 eV has been taken to be 212°K corresponding to transverse accoustical phonons, and

in the range 1.21 - 3.0 eV to be 670°K corresponding to transverse optical phonons. Thus the absorption coefficient α has been computed in the range 300-425°K, which are also the respective ranges in the calculation of I_{SC} .

The calculated plot of I_{SC} versus temperature is shown in Fig. 1.4. The following features should be noted.

- (a) The dashed curves in Fig.1.4 do not show any variation with temperature. They have been calculated by changing the integration limit to take care of the lowering of E_G with increase in temperature, but the value of α (λ) is kept fixed to the value at 300°K. Thus, it is not true that "the increase in I_{SC} can be accounted for by 100°C temperature increase producing 0.03 eV decreased energy gap and 0.03 $\mu\,m$ increased useful wavelength range. This can be seen physically in the following way. The absorption coefficient in silicon for photons corresponding to E_G at 300°K is $^{\sim}10~cm^{-1}$. When E_G decreases with increasing temperature, the number of excess photons absorbed is negligible due to the extremely low value of α in this range.
- (b) The solid lines in Fig.1.4 show variation with temperature and dI_{SC}/dT ranges from 4 to $7\,\mu\,\mathrm{A}$ cm $^{-2}/^{\circ}\mathrm{K}$ for values of L_n from 10 to 100 $\mu\,\mathrm{m}$. In these calculations temperature variation of α , as described earlier, has been incorporated along with the proper change in the limits of integration to take care of the variation of E_G with temperature. The values of dI_{SG}/dT in Fig. 1.4 are comparable with

the experimental value [15] of $5 \,\mu\text{A} \,\text{cm}^{-2}/\text{oK}$. An exact agreement could only be sought if the parameters of the experimental samples were known exactly. It is to be noted that the considerations given here are not limited only to SBSC. We consider this to be an important contribution of the present work.

Having studied the temperature dependence of \mathbf{I}_{SC} , it would also be of interest to know the temperature dependence of the open circuit voltage which is given by eqn. (1.19). We observe that the evaluation of this equation at different temperatures requires a knowledge of the variation of \emptyset_R and n with temperature. A survey of the published literature has shown that (d $\phi_{\rm R}/{\rm dT}$) and (dn/dT) are sensitive to the method of fabrication and this has given rise to several conflicting This situation has been succinctly summarized reports. by Hackam and Haroop [32] and we reproduce some of their comments in Table 1.1. A perusal of this shows that $d\phi_R/dT$ and dn/dT should be found for a particular device and using these the value of (dV_{OG}/dT) should be calculated. The same uncertainties that affect the calculation of $\mathrm{dV}_{\mathrm{OC}}/\mathrm{dT}$ also affect the uncertainties in $(d\eta/dT)$, hence in these cases we have not carried out the computations any further.

To conclude, in this chapter, we have obtained the expressions for the current voltage characteristics of SBSCs' and have studied some aspects of their temperature

Table 1.1: Temperature dependence of ϕ_{B} and n in silicon.

Metal-Si systems	$d \phi_{ m B}/d T$ and $d n/d T$	References
Cr-nSi	Same values of \emptyset_B and n at 77°K, 196°K and 289°K are obtained by $\frac{1}{C^2}$ -V method	Cowley etal, IEEE Trans., ED-15,761,1968
Titanium-Si (both P and N-type)	The barrier heights were determined from measurements of the reverse current density and activation of reverse current. dØ/dT varies from 0 to -1x10 ⁻⁵ ev/°K near 300°K	Cowley, Solid- StElectron., 12, 403, 1970.
Au, Ag and Cu on n-Si	$dQ_B/dT = -(2.67\pm0.60) \times 10^{-4} \text{ eV } \circ \text{K}$ and n varies from 1.01 to 1.02.	Arizumi etal., Jap.J.Appl. Phys,8,749,190
Au-nSi	Equality of temperature dependence of \emptyset_B and E_G	Crowell etal., App.Phys.Lett. 4,91,1964
Au-nSi	$d\phi_B/dT \sim 0$ from capacitively determined ϕ_B ; $d\phi_B/dT \sim large$ for ϕ_B determined by photoelectric technique	Kahng, Solid st.Electron., 6,281,1963
NiCr-nSi	n depends on forward bias voltage. At low voltage, n decreased with increasing temperature while at higher bias n was independent of temperature	Yu and Snow, J.Appl.Phys., 39,3008,1968
Cr-nSi	Both $\emptyset_{\overline{B}}$ and n depend on bias voltage	Levine, J. Appl Phys., 42, 3991 1971
Ni-Si Au-Si	(i) dØ _B /dT > 0; C-V method used, Temperature range used is 77°K- 300°K. (ii) dØ _B /dT ○ 0 from activa energy plots. But this plot yields higher value of Richardson constant. When dØ _B /dT = -2x10-4/°K is invoked, accepted literature value of Richardson constant is obtained.	Padovani, J. Ap Phys., 38,891 1967.

dependence. As has already been mentioned, the SBSCs' have not lived upto their promise so far efficiency of energy conversion is concerned. This is mainly because of their low open circuit voltage. Tunneling MIS solar cells have shown better performance and are the subject matter of the next chapter.

CHAPTER 2

SCHOTTKY (MIS) SOLAR CELLS

2.1 Introduction

It has been found both experimentally [1-5] and theoretically [6-15] that interposition of a thin insulating layer between the metal and the semiconductor of a Schottky barrier solar cell increases the open circuit voltage, thereby the efficiency. This increase, however, critically depends on the thickness of the insulating layer, δ . A typical experimental curve, obtained by Lillington and Townsend [1] exhibiting the dependence of the open circuit voltage $V_{\mbox{OC}}$ and short circuit current $I_{\mbox{SC}}$ on δ , in the case of a Au-SiO2-nSi cell, is given in Fig.2.1. The notable features of this plot are the following:

- (i) I_{SC} remains constant with δ upto a critical thickness δ_{SC} and then decreases.
- (ii) V_{OC} increases with δ , reaches a maximum and flattens out and then at a critical thickness δ_{OC} starts decreasing.

Although some heuiristic arguments have been provided in the published literature to explain the behaviour of Fig.2.1, to the best of our knowledge no analytical attempt has been made to quantitatively obtain the behaviour of V_{OC} for $\delta > \delta_{OC}$ and I_{SC} for $\delta > \delta_{SC}$. In this chapter we attempt to develop such an analytical theory. This has been possible because of the inclusion of (a) The variation of the density

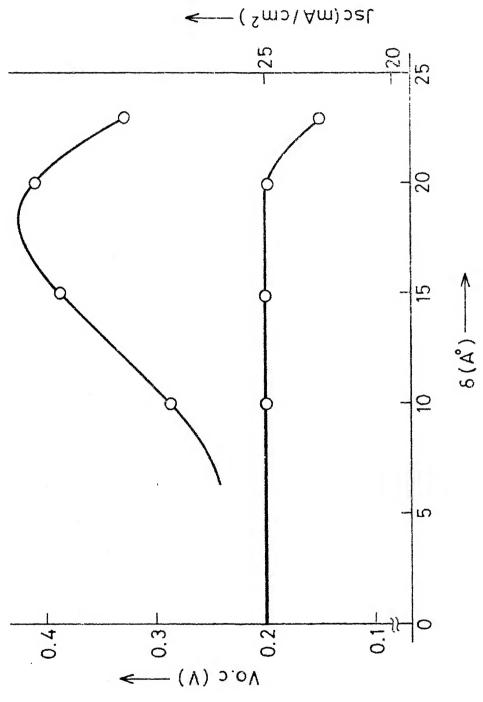


Fig.2.1 A plot of the **short** circuit current density Jsc and the open circuit voltage Voc versus the oxide thickness 8, taken from experiments {Lillington and Townsend [1] }

of surface states with δ , while calculating the interface recombination current and the barrier height and (b) The shift, under illumination, of the minority carrier quasi-Fermi level from the metal Fermi level.

In the published literature there are several [15] theoretical analysis of MIS solar cells. Each of these has emphasized different aspects of the problem. In particular, we would like to mention here the works of Landsberg and Klimpke [12], Buxo etal.[13], Card and Yang[11] and Card [14]. Landsberg and Klimpke have considered the effect of recombination at the interface in detail and have investigated the effect of the density of surface states on the efficiency of the cell, but they have ignored the splitting of the minority carrier quasi-Fermi level from the metal Fermi level. This latter effect has been taken into account by Buxo etal. 13 l. but these authors have ignored any recombination at the interface or any other effect due to the density of surface states. Card and Yang [11] were perhaps the first to point out the role played by the splitting of the quasi Fermi level of the minority carriers from the metal Fermi level, but they have restricted themselves to a qualitative [11] or a semi-quantitative [14] analysis. The work of some other workers in the area has already been reviewed by Olsen in a recent paper [15] hence is not being repeated here. In the present work attention has been restricted mainly to the analysis of the variation of the

short circuit current and the open circuit voltage with the oxide thickness. To do this both the factors (a) and (b) mentioned above have been included. Though several workers have considered them separately, their joint effect, to the best of our knowledge has not been investigated earlier. It is also to be pointed out that the importance of variation of the density of surface states with the oxide thickness in explaining the behaviour of MIS cells has not been realized in any of the earlier published works.

The expressions for V_{OC} and I_{SC} with the inclusion of the factors (a) and (b) mentioned above have been developed in Sec.2.3, where it has also been shown that with suitable approximation in the expression given here, the familiar expressions for V_{OC} given in the literature by other workers fall out. In order to obtain numerical values from these expressions one would need the value of the barrier height under illumination and the values of some other parameters. The expressions for these have been developed in Sec. 2.2. The chapter has been concluded by developing an iterative scheme, which though complicated, allows the calculations of the illuminated current voltage characteristics of the Schottky (MIS) solar cell.

2.2 Energy Band Diagram

Our main interest is in developing the expressions for the open circuit voltage and the short circuit current

of an MIS cell. Before doing it, it is necessary to discuss the features of the energy band diagram of an MIS solar cell. These band diagrams (i) in thermal equilibrium, (ii) under illumination (such that a forward voltage develops when a load is connected) and (iii) under forward bias (but without illumination), are given in Fig.2.2. The semiconductor is taken to be N-type but similar considerations would also hold for F-type semiconductor. In the following we consider the diagrams of Fig.2.2 one by one.

2.2.1 Thermal Equilibrium

In thermal equilibrium, the interest is in knowing the barrier height \emptyset_B . This has been calculated by Cowley and Sze [16] taking the occupation probability as a step function, i.e. a 0°K approximation; and by Landsberg and Klimpke [12] by taking the occupation probability as Fermi Dirac distribution function and is given below (see Appendix B, equation (B.16))

$$\emptyset_{B} \neq (\emptyset_{M} - \chi) - \frac{\delta^{2} \rho_{O}}{2 \epsilon_{i}} + \frac{qD_{S} \delta}{\epsilon_{i}} \quad [E_{G} - kT \ln \{\frac{1 + \exp(q\emptyset_{B}/kT)}{1 + \exp(\frac{q\emptyset_{B} - E_{G}}{kT})}\}]$$

$$- \frac{q^{2} \delta}{\epsilon_{i}} D_{S} \emptyset_{O} - \frac{\delta}{\epsilon_{i}} \{2 \epsilon_{S} qN_{D}(\emptyset_{B} - V_{n})\}^{\frac{1}{2}} \qquad (2.1a)$$

where the symbols ϕ_M , χ , ϕ_o , ϵ_i , ϵ_s , q, N_D , E_G , ϕ_B , V_n and D_s are described in the list of symbols in Appendix A and δ and ρ_o represent, respectively the thickness of the oxide layer and the fixed charge esntity in the oxide layer under thermal equilibrium.

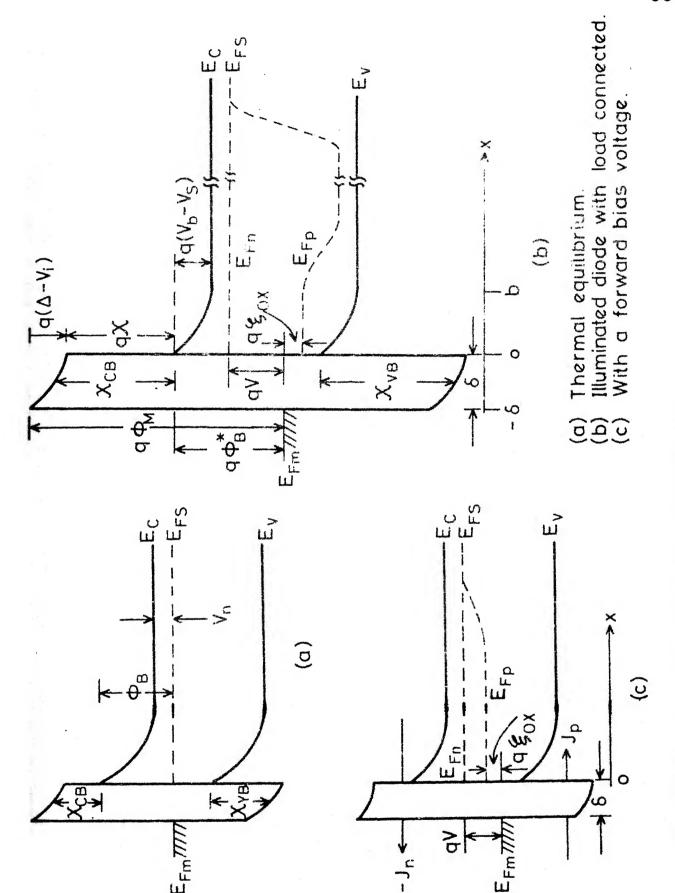


Fig. 2.2 Energy band diagram of MIS diode.

Let us consider the role of ρ_0 in determining the barrier height $\emptyset_{R^{\bullet}}$. There are four possibilities that can arise; these are positive and negative ρ_{Ω} in the case of either N type or P type semiconductor. Let us consider the case of positive oxide charge first. For an M-I-N semiconductor cell a perusal of eqn. (2.1a) shows that with positive ρ_0 , $oldsymbol{\emptyset}_{\mathsf{R}}$ would decrease. Similar considerations show that with increases. Thus, since a large value of $\emptyset_{ extbf{B}}$ is desirable one would like to obtain if possible, positive oxide charge in a P type semiconductor and negative oxide charge in N type semiconductor. Technological difficulties in silicon, at the present perclude the presence of negative oxide charges, thus leaving the only case of interest as positive oxide charge in P type semiconductor. An analysis of this has been done by Pulfrey [9].

In the case that $ho_0=0, \exp(q\phi_B/kT)>>1$ and $\exp\{\cdot(q\phi_B-E_G)/kT\}<<1$, eqn. (2.1a) reduce to the basic quadratic equation in ϕ_B of Cowley and Sze (see eqn. 21, p.374 of [17]). As is well known, Cowley and Sze have further obtained that in the case—that a constant C_1 is given as

$$C_1 = \{ 2q \epsilon_s N_D \delta^2 / \epsilon_i^2 \}$$

is negligible, the barrier height is given by

$$\emptyset_{Bn} = C_2(\emptyset_M - X) + (1 - C_2)(\frac{E_G}{q} - \emptyset_0)$$
where $C_2 = (1 + \frac{q^2 \delta D_S}{\epsilon i})^{-1}$.

It is interesting to note here that the neglect of the term containing C_1 is in effect equivalent to ignoring the space charge in the semiconductor, which means that a biased case such that a flat band occurs is being considered. If this consideration is introduced in the beginning itself, i.e. in the charge neutrality equation, then eqn.(2.1b) falls directly without requiring the solution of a quadratic [18]. Once \emptyset_B is known, the equilibrium potential drop $V_b(=\emptyset_B-V_n)$ across the semiconductor, can be easily calculated by knowing V_n which depends on the doping and the temperature.

2.2.2 <u>Illuminated Cells</u>

When the cell is suitably illuminated from the metal side and a load is connected, the band diagram of Fig.2.2(b) ensues. The following points regarding this diagram should be noted.

(i) Under illumination and with a load connected, the MIS cell develops a potential difference V such that

$$V = V_{g} + V_{i}$$
 (2.2)

where (V_b-V_g) and $(\Delta-V_i)$ are respectively the potential drops across the semiconductor and the oxide layer. Here V_b is the diffusion potential. Expressions for Δ and V_i are developed in Sec. 2.2.3. Knowing V_i , a value of V_s

can be obtained from eqn. (2.2) for a given value of V.

(ii) The barrier height in this case gets modified and is denoted by \emptyset_B^{\bigstar} where

$$\emptyset_{B}^{\star} = (V_{b} - V_{s}) + V_{n} + V = (V_{b} + V_{n}) + (V - V_{s})$$

$$= \emptyset_{B} + V_{i}$$
(2.3)

(iii) Due to photogeneration of carriers in the semiconductor two quasi-Fermi levels, one for electrons (E_{Fn}) and another for holes (E_{Fp}) have been shown in Fig.2.2(b). It has been assumed that the majority and minority carrier quasi-Fermi levels are constant in the depletion region. A justification of this is given later. Here we note that at a interface the minority carrier quasi-Fermi level $\mathbf{E}_{\mathbf{Fp}}$ has been shown to be separated from the metal Fermi level $\mathbf{E}_{\overline{\mathbf{F}m}}$ by an amount of $q\xi_{ox}$. The physical necessity of ξ_{ox} is due to the fact that its gradient across the insulator layer provides the driving force for the minority carriers to cross this layer. Thus one would expect that as the thickness of the oxide layer (δ) increases, ξ_{ox} would increase if it is required that the same number of photogenerated carrier should cross the insulating layer. But note that ξ_{ox} increases, the number of minority carriers at the interface increases, which in turn increases the number of minority carriers at the semiconductor edge of the depletion region. then modifies the boundary condition for the solution of the diffusion equation needed to obtain the profile of photogenerated carriers. The net effect of this modification

is to reduce the short circuit current J_{SC} . This happens because with E_{Fp} constant through the depletion region one gets $E_{Fp}(\mathbf{b}) = \xi_{ox}$, which when used in eqn. (1.11b) of J_{diff} , shows the J_{diff} increases with increasing δ . Since J_{diff} subtracts from J_{T} , J_{SC} decreases with increasing δ .

(iv) Let us now consider the position-dependence of $E_{Fn}(x)$ and $E_{Fp}(x)$ in the depletion region. If the transport of the majority carriers is governed by thermionic emission then $E_{Fn}(x)$ remains constant in the depletion region [19]. The nature of $E_{Fp}(x)$ can be obtained by recalling the behaviour of eqn. (1.9b), which we rewrite in a modified form for N type semiconductor.

$$\exp \left[-\left(\frac{E_{Fp}(b) - E_{Fp}(o)}{kT}\right)\right] - 1$$

$$= J_{p} N_{d}^{\frac{1}{2}} (1/n_{i}^{2} \mu_{p}) (\pi \epsilon_{s}/2q^{2} kT)^{\frac{1}{2}} \exp(E_{Fp}(o)/kT)$$
(2.4)

Note that $E_{Fp}(o) = q \xi_{ox} < 0$. It is apparent from eqn. (2.4) that as ξ_{ox} increases, the difference between the Fermi level at x=0 and x=b would decrease. Thus $E_{Fp}(x)$ becomes flatter and flatter in the depletion region as ξ_{ox} increases. In Sec. 2.3.1, we would show that the range of our calculations is such that taking $E_{Fp}(x)$ constant in the depletion region becomes valid.

(v) The potential difference V at the terminals of the cell is equal to $|E_{Fs}-E_{Fm}|/q$, where $E_{Fs}=E_{Fh}$ in the bulk of the semiconductor. In the conventional situation where $\xi_{ox}=0$

note that $|E_{Fn}-E_{Fp}|/q = V$. Since the split $E_{Fn}-E_{Fp}$ is controlled by photogeneration of carriers, it is obvious that a non-zero value of ξ_{ox} entails a loss in available V. Thus ξ_{ox} is a "necessary" evil for $\delta < \delta_{SC}$ in as much as it keeps J_{SC} constant with increasing δ but entails a loss in the developed voltage available at the external terminals. In the case that $\delta > \delta_{SC}$ such that J_{SC} starts falling with δ the presence of ξ_{ox} becomes completely disadvantageous.

2.2.3 Charge Balance Equation

The relation $\emptyset_B^* = \emptyset_B + V_i$ given by eqn. (2.3) exhibits that to know \emptyset_B^* one has to know \emptyset_B and V_i . An expression for \emptyset_B is given in eqn.(2.1). Here we setforth to obtain an expression for V_i . This can be obtained by considering the charge balance equation in dark,

$$Q_{M} + Q_{OX} + Q_{i} + Q_{SC} = 0$$
 (2.5a)

and under illumination

$$Q_{M}^{*} + Q_{OX}^{*} + Q_{i}^{*} + Q_{SC}^{*} = 0$$
 (2.5b)

Here Q_M , Q_{OX} , Q_i and Q_{SC} are the charges per unit area in the case of thermal equilibrium respectively in the metal, the oxide layer, the surface states and the space charge region of the semiconductor. Those with asterisk superscripts are the corresponding charges under illumination. In the following discussion we would consider $Q_{OX} = \rho \delta$, $Q_{OX}^* = \rho^* \delta$, where ρ and ρ are the charge densities in the oxide in

thermal equilibrium and under illumination, respectively, and are assumed to be constants. The functional dependence of Q_i , Q_i^* , Q_{SC} and Q_{SC}^* has been given in Appendix B.

Here we proceed to obtain an expression for V_i in terms of ρ , ρ^* , Q_i , Q_i^* , Q_{SC} and Q_{SC}^* , so that when the functional dependences of these are determined, a value of V_i may be obtained. The first task is the determination of the potential drop Δ across the oxide layer in thermal equilibrium.

Solving the Poisson's equation in the oxide, $a^2\Psi$

$$\frac{d^2\Psi}{dx^2} = -\frac{\rho}{\epsilon}$$
; one obtains

$$\Delta = \Psi (o) - \Psi (-\delta)$$

$$= \frac{\delta}{\varepsilon_{i}} \left[\frac{1}{2} \delta \rho + Q_{i} + Q_{SC} \right]$$
 (2.6)

Since Δ is the difference of potentials at two points, only one boundary condition $\varepsilon_i \frac{d\Psi}{dx} = (Q_i + Q_{SC})$ at x = 0 has been utilized in deriving eqn. (2.6). Following a procedure similar to the one used for the derivation of eqn.(2.6), under illumination one obtains the potential drop across the oxide (Δ - V_i) as:

$$\Delta - V_{i} = \frac{\delta}{\epsilon_{i}} \left[\frac{1}{2} \delta \rho^{*} + Q_{i}^{*} + Q_{SC}^{*} \right]$$
 (2.7)

From equations (2.6) and (2.7) one obtains

$$-V_{i} = \frac{\delta}{\varepsilon_{i}} \left[\frac{1}{2} (Q_{OX}^{*} - Q_{OX}) + (Q_{i}^{*} - Q_{i}) + (Q_{SC}^{*} - Q_{SC}) \right]$$
 (2.8)

Once V_i is known V_s can be obtained from eqn.(2.2) for a given value of voltage V developed under illumination for a given load.

So far we have considered V_i under illumination. In the case that the diode is not illuminated but is forward biased by an applied voltage, let us replace V_i by a corresponding V_i^f ; the expression for which can be written in analogy with eqn.(2.8) as

$$-V_{i}^{f} = \frac{\delta}{\varepsilon_{i}} \left[\frac{1}{2} \left(Q_{OX}^{f} - Q_{OX} \right) + \left(Q_{i}^{f} - Q_{i} \right) + \left(Q_{SC}^{f} - Q_{SC} \right) \right]$$
 (2.9)

Here Q_{OX}^f , Q_i^f and Q_{SC}^f are the respective charge density in the oxide, surface states and depletion layer under forward bias.

Thus if the expressions for \mathbb{Q}_i , \mathbb{Q}_i^* , \mathbb{Q}_i^f , \mathbb{Q}_{SC} , \mathbb{Q}_{SC}^* and \mathbb{Q}_{SC}^f are developed, one can obtain the values of \mathbb{V}_i and \mathbb{V}_i^f . These expressions have been given in Appendix B. Note that here we have taken a constant charge in the oxide layer. In the case that this is not true, one would also require the expressions for \mathbb{Q}_{OX} , \mathbb{Q}_{OX}^* and \mathbb{Q}_{OX}^f . To summarize, it is now possible to obtain the distribution of a developed voltage \mathbb{V} in the oxide region (\mathbb{V}_i) and in the semiconductor depletion region (\mathbb{V}_s) . With this distribution known, we can now proceed to consider the current voltage relation of the Schottky (MIS) solar cell. Before concluding let us also note that the expressions for charges may themselves depend

upon the current voltage characteristics in which case an iterative analysis would be required. Two cases where this iteration is simpler correspond to the short-circuited and open-circuited conditions of the diode. Since the analysis in these two cases is simpler and provides physical insight in the operation of the device, we have considered them in detail in the following sections.

2.3 I-V Characteristics

Our interest is in the calculation of the illuminated I-V characteristics of an MIS solar cell. Particular attention has been paid to two specific cases corresponding to the open circuited and short circuited conditions of the cell. But before considering these, let us consider the mechanism of current transport through an MIS solar cell made on an N type semiconductor. Let $J_n(x)$ and $J_p(x)$ be the majority and minority carrier current densities, respectively, flowing through an illuminated cell. The majority carrier current density J_n is governed by the same equation as in electrically biased case under dark and has been discussed by Card and Rhoderick [19]. They obtain:

$$J_{n} = A_{n}^{**} T^{2} \alpha_{n} \exp(-q p_{B}^{*}/kT) [\exp(qV/kT) -1]$$
 (2.10)

where A_n^{**} is the Richardson constant, $\alpha_n = \exp[-\chi_{CB}(\delta)^{\frac{1}{2}}\delta]$, $\chi_{CB}(\delta)$ is the barrier height for majority carrier across the oxide layer as shown in Fig. 2.2, V is the developed

voltage and \emptyset_B^* is the barrier height under illumination. Note that in the case of a dark but forward biased diode, \emptyset_B^* is replaced by \emptyset_B^f .

The minority carrier component is given as

$$-J_{p} = J_{L} - J_{diff} - J_{R1} - J_{R2}$$
 (2.11)

The component J_L is the light generated current density and is the same as in the case of SBSC as given in eqn.(1.13). Note that J_L contains the sum of the effect of photo-generated carriers in the depletion layer and the quasi-neutral region. The component $J_{\rm diff}$ is due to the flow of some of the photogenerated minority carriers in a direction opposite to the flow of J_L as explained in Sec. 1.2.2. There the expression for $J_{\rm diff}$ is given by eqn. (1.11b) which we rewrite for convenience:

$$J_{diff} = J_{diff} [exp { \frac{q(V-\xi_{OX})}{kT} } -1]$$
 (2.12)

where

$$J_{diff}' = qD_p P_{nO}/L_p$$
 (2.12a)

Note that we have used the relation $E_{pp}(b) = \xi_{OX}$ and have also introduced the effect of the developed voltage in this expression.

The component J_{R1} is due to the recombination at the interface layer and an expression for this, using Schockley-Read-Hall (SRH) theory [20,21], has been developed by Landsberg and Klimpke [12]. The steps of its derivation has been outlined in Appendix B and lead to the expression

$$J_{R1} = J_{R}^{'} \left[\exp \left\{ q(v - \xi_{OX})/kT \right\} - 1 \right]$$
where
$$J_{R}^{'} = n_{i}^{2} \frac{kT D_{S}H(o)}{n_{O}(o)(A-B)} \ln \left[\frac{q\emptyset_{B}^{*}}{kT} - A \right] \left\{ \exp(\frac{q\emptyset_{B}^{*} - E_{G}}{kT}) - A \right\} \left\{ \exp(\frac{q\emptyset_{B}^{*} - E_{G}}{kT}) - A \right\}$$

$$\left\{ \exp(\frac{q\emptyset_{B}^{*} - E_{G}}{kT}) - B \right\} \left\{ \exp(\frac{q\emptyset_{B}^{*} - E_{G}}{kT}) - B \right\}$$
(2.14a)

and

$$\frac{A}{B} = \frac{I}{2G(0) n(0) + H(0) p(0)} + I \frac{I}{2G(0)n(0) + H(0)p(0)} = \frac{2H(0)P_0(0)}{G(0)n_0(0)}$$
(2.14b)

where

$$G(o) = T_1^S + T_1 n(o) + T_2 p(o)$$

 $H(o) = T_2^S + T_3 n(o) + T_4 p(o)$

The reaction constants T_1^S , T_2^S , T_1 , T_2 , T_3 and T_4 are defined in Appendix B and will be taken to be the same for all interface states [12]. n(o) and p(o) are respectively electron and hole concentration at x=0 and expressions for them are given later in eqns. (2.17a) and (2.17b). $n_0(o)$ and $p_0(o)$ are relevant carrier concentrations in thermal equilibrium.

The component J_{R2} is due to the recombination of the photogenerated carriers in the depletion region and its expression is well known [17]. It varies as $\exp[q(V-\xi_{OX})/2kT]$ as compared to the $\exp[q(V-\xi_{OX})/kT]$ variation of J_{R1} . Also the values of preexponential factors in J_{R1} and J_{R2} are such that for the range of our calculations $J_{R1} >> J_{R2}$. Hence the effect of J_{R2} has been ignored in the following analysis.

Before concluding the considerations of the current components, it is important to note that the minority carrier density J_p given by eqn. (2.11) must also be the minority carrier current density that tunnels through the oxide layer, i.e. J_p can also be written as

$$-J_{p} = A_{p}^{**}T^{2} \alpha_{p} \exp\left[\frac{-E_{g} + q \beta_{B}^{*} - q \xi_{OX}}{kT}\right] \left[1 - \exp\left(\frac{q \xi_{OX}}{kT}\right)\right] \quad (2.15)$$

$$= J_{tunnel}^{\prime} [exp(-q \xi_{OX}/kT) -1]$$
 (2.15a)

where

$$\alpha_{p} = \exp \left[-\chi_{pp}(\delta)^{\frac{1}{2}} \delta\right]$$
 (2.15b)

and

$$E_g - q \phi_B^* + q \xi_{OX} = E_{Fp} - E_v$$
 (2.15c)

Here $\chi_{TR}(\delta)$ is the barrier height across the oxide for the minority carriers as shown in Fig. 2.2. In the following sections we use these equations of current transport to obtain the short circuit current, the open circuit voltage and then the I-V characteristics of the MIS cells. The values of parameters that have been used are given in Appendix 3.

2.3.1 Variation of I_{SC} with δ :

The experimental features of $I_{\mathrm{SC}}(\delta)$ in an MIS solar cell is that it remains constant upto some $\left.\delta < \delta \right|_{\mathrm{SC}}$ and then starts: falling off [1]. In the following, we have attempted to explain this feature.

The short circuit current for an MIS cell on N type semiconductor is given as $I_{SC} = aJ_p$ where a is the area of the cell and taken as 1 cm², and J_p is the minority carrier current density given by eqn. (2.11), which we rewrite for convenience

$$-J_{p} = J_{L} - J_{diff} - J_{R1} - J_{R2}$$
 (2.11)

In the following we have neglected the term J_{R2} due to the reasons given earlier. The expression for J_L is the same as in the case of Schottky barriers and is given by eqn.(1.13). We take the value $J_L=25~\text{mA/cm}^2$ in the present calculations. To evaluate J_{diff} and J_{R1} one needs the value of ξ_{OX} for the short circuited case. The general expression for ξ_{OX} can be obtained by using eqn. (2.12) and (2.13) in eqn. (2.11) and then equating it to eqn. (2.15). The resulting expression for ξ_{OX} is

$$-\xi_{OX} = \frac{kT}{q} \ln \left[\frac{J_{L}^{+}J_{diff}^{+} + J_{R}^{+} + J_{tunnel}^{+}}{(J_{diff}^{+}J_{R}^{+}) \exp(\frac{qV}{kT}) + J_{tunnel}^{+}} \right]$$
 (2.16)

In the case of short circuit, i.e. V = 0, one gets,

$$-\xi_{OX} = \frac{kT}{q} \ln [1 + (\frac{J_{L}}{J_{diff}^{i} + J_{R}^{i} + J_{tunnel}^{i}})]$$
 (2.16a)

Here J_{diff}^{i} , J_{R}^{i} and J_{tunnel}^{i} are defined by eqns. (2.12a), (2.13a) and (2.15a), respectively.

We would start the calculations by making two simplifications:

- (i) The effect of the component J_{R1} due to recombination at the interface is initially neglected. The effect of its inclusion is discussed later.
- (ii) The simplified expression for the barrier height \emptyset_B in thermal equilibrium, as given by Cowley and Sze [16], is used:

$$\emptyset_{B} = \mathcal{C}_{2}(\emptyset_{M} - \chi) + (1 - \mathcal{C}_{2})(\frac{\mathbb{E}_{G}}{q} - \emptyset_{O})$$
where

$$C_2 = (1 + q^2 \delta D_s / \epsilon_i)^{-1}$$

The effect of taking the more general expression for \emptyset_3 as given by eqn.(2.1a) has also been discussed later.

We note from eqn.(2.1b) that for the range of δ considered and for $D_{\Sigma} \gtrsim \times 10^{11}$ per eV per cm² one gets $q\emptyset_B \simeq \emptyset_M - \chi$. We have chosen $(\emptyset_M - \chi) = 0.69$ eV and 0.5 eV; a comment on this choice is given later. ξ_{OX} is plotted from eqn.(2.16a) and is shown in Fig. 2.4(c). In short circuited case J_p^{SC} (or J_{SC}) represents the total current density and has been calculated using the values of ξ_{OX}^{SC} (i.e. ξ_{OX} at short circuit) in eqn.(2.11). The plot of J_{SC} versus δ is given in Fig.2.3(a) for \emptyset_M - χ = 0.5 eV and 0.69 eV. Note that starting from δ = 20 A° a drop in current takes place for $(\emptyset_M - \chi) = 0.5$ eV but not for $(\emptyset_M - \chi) = 0.69$ eV. The physical reason for this can be seen as follows.

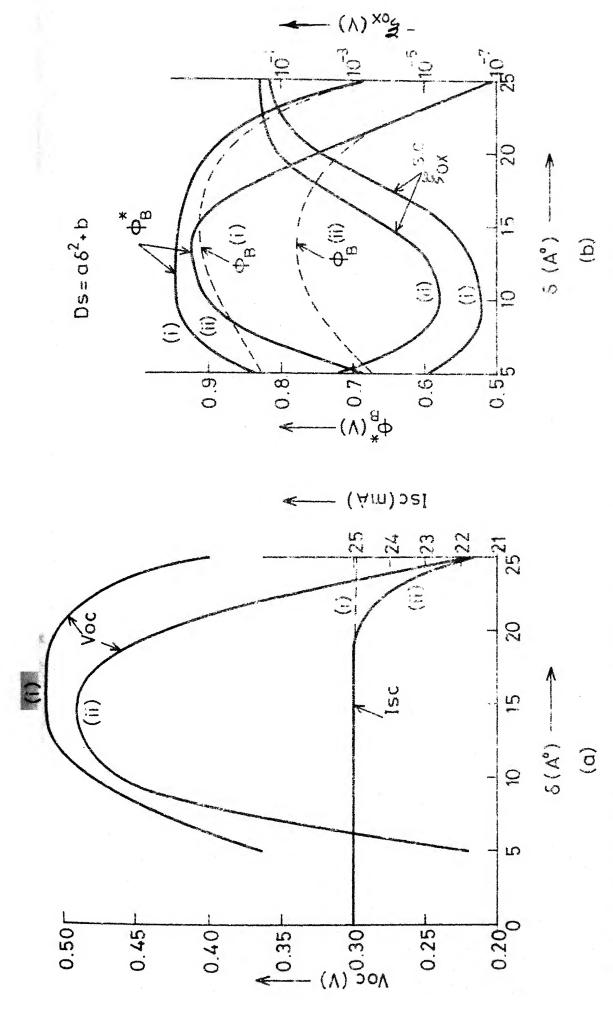
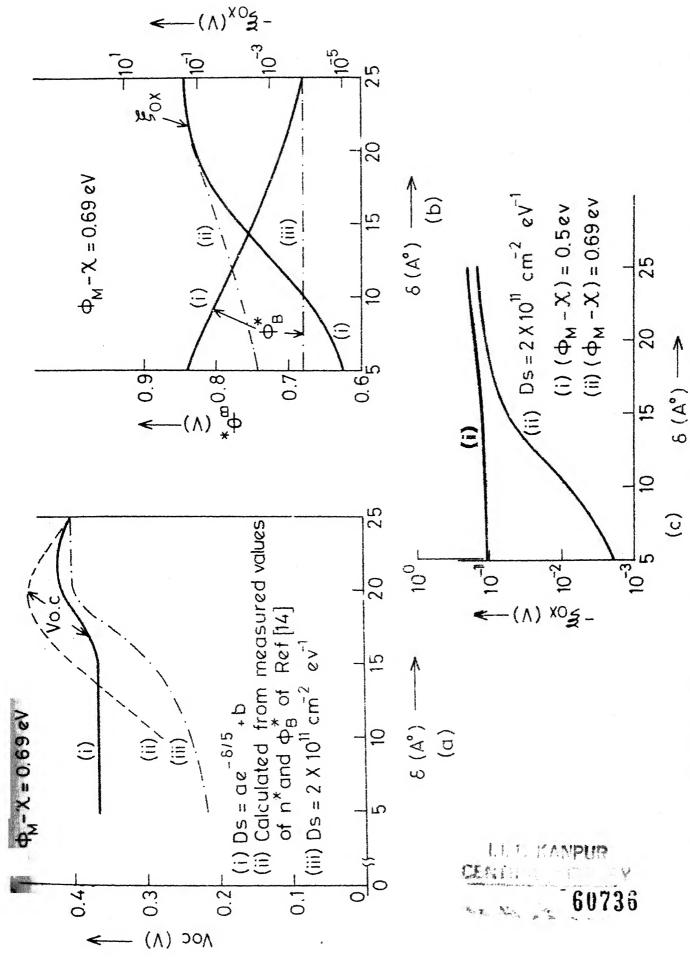


Fig. 2.3 Label (i) Corresponds to $(\phi_M - \chi) = 0.69$ eV and label (ii) to $(\phi_M - \chi) = 0.5$ eV.



Plots of the open circuit voltage Voc versus 6. & Plots of the barrier height $\phi_{\rm B}^*$, and $\xi_{\rm 0x}$ Fig. 2.4

- (i) Let us consider the behaviour of $J_{diff}(\delta)$ defined in eqn.(2.12) for V = 0. To start the discussion let us calculate the value of $\xi_{OX}(\delta)$ that is needed to to get, say, $J_{diff}(\delta) = 1 \text{ mA/cm}^2$. For the parameters chosen one gets -q ξ_{OX} = 0.434 eV. We reiterate that as long as -q $\xi_{\rm OX}$ < 0.434 eV, the value of $J_{\rm diff}(\delta)$ will not exceed 1 mA/cm². Note from Fig.2.4(c) that ξ_{OX} , for $(\emptyset_{M} - \chi) = 0.69 \text{eV}$ and in the range 0 < δ < 25 A°, remains below -q ξ_{OX} = 0.434 eV, resulting in almost constant value of $J_{SC}(\delta)$. In the case of $(\emptyset_{M} - \chi) = 0.5 \text{ eV}, -q \xi_{OX} \text{ reaches a value of 0.434 eV at}$ $\delta = 22^{\circ}5 \, \text{Ågiving J}_{\text{diff}}(\delta_{\text{SC}}) = 1 \, \text{mA.}$ This choice of δ_{SC} defined above is arbitrary. Here we take it to be that values of δ where current has falled by 1 mA/cm². Also note that in this case at $\delta = 25 \text{A}^{\circ}$, $J_{\text{diff}} = 4 \text{ mA/cm}^2$, which is comparable to the drop experimentally obtained by Lillington and Townsend [1].
- (ii) The discussion in (i) has exhibited the sensitivity of the fall of $J_{SC}(\delta)$ to the value of \emptyset_B , which in the present case of low value of D_S is given by $(\emptyset_M \chi)$. The value of $Q\emptyset_B = 0.69$ eV corresponds to the workfunction $\emptyset_M = 4.7$ eV for gold vacuum interface—and electron affinity $\chi = 4.01$ eV for silicon. The value $(\emptyset_M \chi) = 0.5$ eV has been chosen to match the experimental results of barrier height for $\delta > 20$ A° in the case of Au-SiO₂-nSi diodes [14].

It is obvious that it is desirable that J_{SC} should not fall with δ . The discussion given above points out that for this to happen, $\emptyset_B(\delta)$ should be larger than a certain threshold value. This can be obtained by either choosing larger value of $(\emptyset_M^-\chi)$ and/or large value of $D_S(\delta)\delta$ product. In order to meet the requirement of large barrier height at a chosen δ a large value of $D_S(\delta)$ is desirable if high values of $(\emptyset_M^-\chi)$ can not be obtained. Care, however, has to be taken in choosing a large value of $D_S(\delta)$ because it also affects—the current J_{R1} due to recombination at the interface, which adversely affects the open circuit voltage [12]. Hence, we would return to the choice of $D_S(\delta)$, after discussing the behaviour—of the open circuit voltage.

In the beginning we have ignored the effect of J_{R1} . Let us now include it and see its effect on $J_{SC}(\delta)$. To include the effect of J_{R1} from eqn.(2.13), the value of J_{R}^{i} is needed. J_{R}^{i} is evaluated from eqn. (2.14a). This needs evaluating n(o), p(o), $n_{O}(o)$, $p_{O}(o)$ and the values of n_{I} , n_{I} , n

$$n(o) = N_C \exp[-\frac{q(p_B^* - V)}{kT}] = N_C \exp[-\frac{E_C - E_{Fn}}{kT}]$$
 (2.17a)

$$p(o) = N_v \exp \left[\frac{-E_{G} + q(\phi_{P}^* - \xi_{OX})}{kT} \right] = N_v \exp \left[\frac{E_v - E_{Fp}}{kT} \right]$$
 (2.17b)

 $n_0(o)$ and $p_0(o)$ are obtained, respectively, from eqns.(2.17a)

and (2.17b) by putting $\xi_{OX} = 0$ and replacing ϕ_B^* by ϕ_B . that \emptyset_B^* with illumination but for V=0 is almost equal to \emptyset_B^* . n_i is the intrinsic concentration in silicon at T = 300°K. We have assumed G(o) = H(o) following Landsberg etal [12]. The expression for G(o) is given in Appendix B. calculation of J_R^1 is started by taking ξ_{OX} = 0. With this value of J_{R}^{τ} , ξ_{OX} is calculated from eqn. (2.16a). This value of $\xi_{||X|}$ is now used to calculate $J_{R}^{\,t},$ and the iteration is continued till ξ_{OX} converges within a limit of error. Using the values of \emptyset_B and ξ_{OX} at V=0, $J_{R1}(\delta)$ at short circuit is calculated. The maximum value of $\boldsymbol{J}_{\text{R1}}(\boldsymbol{\delta}$) under short circuit is of the order of 10^{-6} amps/cm², hence it is justified to ignore its effect on $\boldsymbol{J}_{\mathrm{SG}}(\boldsymbol{\delta}$) since it contains $J_{\rm L}($ $_{\delta}$) which has been taken to be 25 mA/cm 2 . Also note that when the more general expression for \emptyset_R given by eqn.(2.1a) was used, instead of eqn. (2.1b), no significant change in $J_{SC}(\delta)$ was found.

While discussing the behaviour of the energy band profile at the beginning of this chapter, we had assumed that the minority carrier quasi-Fermi level $\mathbb{E}_{Fp}(x)$ would remain constant throughout the depletion region. We now set out to seek the justification for this assumption. Let us rewrite eqn. (2.4) in a modified form as $-\mathbb{E}_{Fp}(b) = -q \xi_{OX} + kT \ln \left[1 + M \exp(q \xi_{OX}/kT)\right] \qquad (2.4)$ where $M = J_p N_D^{\frac{1}{2}} (\frac{1}{n \cdot p}) (\frac{\pi \varepsilon_s}{2q^2 kT})^{\frac{1}{2}}$

We consider the following cases:

- (i) If M $\exp(q \xi_{OX}/kT) <<1$, then $E_{Fp}(b) = \xi_{OX}$; thus $E_{Fp}(x)$ is flat in the depletion region. To get the limit on ξ_{OX} for this to be true, we can use the relation $\xi_{OX} = \frac{kT}{q} \ln(k/M)$ where k <<1. Taking k = 1 and M calculated for the parameters mentioned above, we get a typical value of $q\xi_{OX} = -0.036$ eV, above which E_{Fp} becomes flat.
- (ii) If M $\exp(q \, \xi_{OX}/kT) >> 1$, the $E_{Fp}(b) = -kT \ln(M)$, which is the case of SBSC (where $\delta = 0$). There we have found $E_{Fp}(b) = -0.33$ eV; which is the worst case of the bending of $E_{Fp}(x)$. We have already noted an important fact that for $J_{diff}(\delta)$ to equal 1 ma/cm², the amount of $E_{Fp}(b)$ needed is -0.434 eV. This leads us to the conclusion that in this case though $E_{Fp}(x)$ is not constant, the worst case value is such that it does not affect our calculation.

2.3.2 The Open Circuit Voltage (V_{OC}) :

In this particular case the sum of the majority and minority carrier components of current densities has to be zero, i.e.

$$J_n(x) + J_p(x) = 0$$
 (2.18)

In order to use eqn.(2.18) to obtain V_{OC} one needs to get an expression for ξ_{OX} . This is given by eqn.(2.16) with $V=V_{OC}$. Note that J_R^* in eqn. (2.16) depends on ξ_{OX} , hence the value of ξ_{OX} can only be obtained by iteration. The

next task is to obtain V_{OU} . This is done by using eqn.(2.18) with $J_n(x)$ taken from (2.10) and $J_p(x)$ taken from (2.15) and ξ_{OX} taken from (2.16). This results in a quadratic equation in $\exp(qV_{OV}/kT)$ given as follows:

$$\exp(2qV_{OU}/kT) + \mu_{1} \exp(qV_{OV}/kT) - \frac{J_{L} \alpha p \exp(\frac{-E_{q} + 2q\emptyset_{B}^{*}}{kT})}{(J_{diff}^{*} + J_{R}^{*}) \alpha_{n} n^{A**}} = 0$$
(2.19)

where

$$\mu_{1} = \frac{J_{\text{tunnel}}}{(J_{\text{diff}}^{\dagger} + J_{\text{R}}^{\dagger})} + \exp(-\frac{-E_{\text{G}} + 2q \emptyset_{\text{B}}^{*}}{kT}) \frac{\alpha_{p} A_{p}^{**}}{\alpha_{n} A_{n}^{**}}$$
(2.20)

Hence one obtains

$$V_{OC} = \frac{kT}{q} \ln \left[-\frac{\mu_{1}}{2} + \frac{1}{2} \left[\mu_{1}^{2} + \frac{4J_{L}^{\alpha} p \exp(-\frac{E_{G}^{+2q} \emptyset_{B}^{*}}{kT})}{(J_{diff}^{!} + J_{R}^{!})_{\alpha_{n}} A_{n}^{**}} A_{p}^{**} \right]^{1/2}$$
(2.21)

Before using eqn. (2.21) for determining $V_{\rm OC}$, let us digress to simplify this expression and compare the simplified expression with the results existing in the published literature.

Let us consider the case where the currents $J_{\mbox{diff}}$ and $J_{\mbox{R}}$ are negligible. In this case eqn. (2.19) simplifies to

$$\exp(qV_{OC}) [J_{tunnel}^* \exp(-q\emptyset_B^*/kT)] = \frac{\alpha_p J_L}{\alpha_n} \exp(-\frac{E_g + q\emptyset_B^*}{kT}) \frac{A_p^{**}}{A_n^{**}}$$
(2.22)

or

$$V_{OC} = \emptyset_{B}^{*} + \frac{kT}{q} \ln \left(\frac{J_{L}}{A_{n}^{**T}^{2} \alpha_{n}} \right)$$
 (2.23)

Using $\emptyset_B^* = \emptyset_B + V_i$, and the relation $n = V_{OC} / (V_{OC} - V_i)$, which is the value of the ideality factor for the open circuit case; one can rewrite eqn. (2.23) as

$$V_{OC} = n \mathcal{D}_{B} + \frac{n k T}{q} \ln(\frac{J_{L}}{A_{n}^{**} T^{2} \alpha_{n}})$$
 (2.24)

If α_n is taken to be unity, eqn. (2.24) is the same equation as the one given by Anderson etal [22] which they have correlated with several expressions of $V_{\rm OC}$ available in literature at that time. Before proceeding further, let us consider the nature of variation of \textbf{V}_{OC} with δ as prediceed by eqn. (2.23). Here \emptyset_B^* and α_n are functions of δ . As δ increases α_n monotonically decreases, thereby the second term on right side of eqn. (2.23) monotonically increases. If one now demands that $V_{\rm CC}$ fall with δ , in any range of δ it becomes necessary that p_{R}^{\star} must decrease with δ in that range; the rate of change being of proper amplitude to annul the effect of the increase in the second term. We know that $\varphi_{B}^{*} = \varphi_{B}^{+}V_{i}$, and one possibility for decrease of ${f \emptyset}_{
m B}^{m{\star}}$ with ${f \delta}$ is that both ${f \emptyset}_{
m B}$ and ${f V}_{
m i}$ decrease with ${f \delta}$. Perusal of eqn. (2.1a) and (2.8) for \emptyset_B (for $(\emptyset_H - \chi) < (E_G/q - \emptyset_O)$ and V_i (for $Q_{SC}=Q_{SC}^*$), respectively leads to the following conclusions.

(A) If $(\not\! D_M - \chi)$ is constant with δ then both $\not\! D_B$ and V_i would decrease if the product D_s δ decreases with increasing δ .

This leads to a very important conclusion, that $\mathbb{D}_{\mathbf{s}}$ with constant value, under this model, cannot explain the experimental feature that $V_{O,3}$ decreases with increase of δ for $\delta > \delta_{OC}$; rather it is incumbent that a $D_s(\delta)$ function be chosen which decreases faster than linearly, for $\delta > \delta_{\infty}$. It is also important to note that to explain the experimentally observed initial increase of $\boldsymbol{V}_{\mbox{\scriptsize OC}}$ with δ , the product $D_s(\delta)\delta$ must increase in this range. These then are the guide lines for choosing a proper variation of $D_{s}(s)$. The experimentally observed fact that D is lower for Si-SiO2 system than for bare silicon [23] is conductive to physical existance of such $D_{_{\mathbf{S}}}(\delta$). The only problem is in choosing the proper functional variation, since to the best of our knowledge no experimental results in this direction are available. To get a physical feel we have decided to study two functional dependences (i) $D_s = a \delta^2 + b$ and (ii) $D_s = C \exp(-\delta/\delta) + d$ which, as is obvious, have two extreme natures of variation of $D_{s}(\delta)\delta$. For the sake of comparison the results for a constant value of $\mathbb{D}_{\mathbf{q}}$ $(= 10^{11}/eV/cm^2)$ have also been calculated and are given in Fig. 2.4(a).

(B) So far we have considered $(\emptyset_M^- \chi)$ to be constant with δ and required D_s to be a function of δ . The values of \emptyset_B and V_i would also decrease if $D_s = 0$, but $(\emptyset_M^- \chi)$ be a function of δ . However, this model would require that $(\emptyset_M^- \chi)$ initially increases with δ and then starts decreasing, which seems rather

contrary to the physical situation. In an actual situation, both $(\not\!\!\!D_M^--\chi)$ and D_S can become monotonically decreasing function of δ , such that the initial increase of V_{OC} with δ is governed by the increase in $D_S(\delta)\delta$ and constancy of $(\not\!\!\!D_M^--\chi)$, whereas the fall of V_{OC} for $\delta >\!\! \delta_{OC}$ is due to a combined effect of fall of $D_S(\delta)\delta$ and $(\not\!\!\!D_M^--\chi)$. However, for the sake of simplicity we have only concentrated on the case where $(\not\!\!\!D_M^--\chi)$ is constant and $D_S(\delta)\delta$ varies in the fashion mentioned earlier.

To obtain a plot of V_{OC} versus δ , using eqn.(2.21) one needs to know J_L , J_R^i , J_{tunnel}^i and \emptyset_B^* . For this an iterative process has been used using the following steps:

- (i) J_L and J_{diff}^\prime have the same values as in the case of the calculation of I_{SC} in Sec. 2.3.1.
- (ii) Taking \emptyset_B and ξ_{OX} at V=0, as calculated in Sec. 2.3.1, J_R^i and J_{tunnel}^i are calculated. Using these values in eqn. (2.21) a value of V_{OC} is obtained.
- (iii) Using this value of V_{OC} for V, V_i is calculated from eqn. (2.8) and the relevant expressions of Appendix B. Thus \emptyset_B^* for this value of V_{OC} is obtained.
- (iv) n(o) and p(o) are calculated from eqns.(2.17a) and (2.17b) for this new $\phi_{\rm R}^*$.
- (v) ξ_{OX} at this $V=V_{OC}$ is obtained from eqn. (2.16). Then step (iv) is repeated for this new ξ_{OX} until p(o) converges within given accuracy.

(vi) J_R^* and J_{tunnel}^* are calculated for \emptyset_B^* and ξ_{OX} obtained from step(iii) and (v) and used in eqn. (2.22) to obtain V_{OC} . Steps (iii) to (v) are repeated until desired accuracy is obtained.

The plots of V_{OC} versus δ using this procedure are given in Figs.2.3(a) and 2.4(a).Let us note the following features.

- (i) First of all let us consider the cases for $(///_{M} \chi)$ = 0.69 eV with $D_s = a \delta^2 + b$, $D_s = C \exp(-\delta/\delta^*) + d$ and $D_s = 10^{11}/\text{eV/cm}^2$ which have been shown in Fig. 2.3a(i), Fig. 2.4a(i) and (iii), respectively. Note that whereas in the first two cases V_{OC} falls off at large values of δ , in the third case there is no such fall off as would be anticipated from the discussion following eqn.(2.24). Also note that these features are supported by the respective plots of $///_{B}$ versus δ , given in Fig. 2.3(b) and Fig. 2.4(b).
- (ii) The values of V_{OC} have also been calculated for $(\emptyset_M \chi) = 0.5$ eV and different distributions of $D_S(\delta)$. The features of the results are very similar to the previous case (e.g. see 2.3(ii)); thus from the consideration of V_{OC} alone one may not realize the importance of choosing the proper value of $(\emptyset_M \chi)$. However, if the choice of parameters is to be such that the experimental nature of both $I_{SC}(\delta)$ and $V_{OC}(\delta)$ is simultaneously explained, as they must be, there is no choice but to discard the value of $(\emptyset_M \chi) = 0.69$ eV.

(iii) Regarding the choice between the variation $D_{_{\rm S}} := a \, \delta^{\, 2} + b \quad {\rm and} \ D_{_{\rm S}} = C \, \exp(-\delta/\delta^{\, 1}) + b \, , \, {\rm one} \, {\rm notes} \, \, {\rm that}$ from Fig. 2.3a(i) and Fig.2.4a(i), that the variation of $V_{\rm OC}(\,\delta\,) \, {\rm in} \, \, {\rm the} \, \, {\rm previous} \, \, {\rm case} \, \, {\rm is} \, \, {\rm more} \, \, {\rm akin} \, \, {\rm to} \, \, {\rm the} \, \, {\rm experimental} \, \, {\rm experimental} \, \, {\rm than} \, \, {\rm the} \, \, {\rm latter} \, \, {\rm one} \, \, \, \, \, {\rm This} \, \, {\rm suggests} \, ,$ based on the experimental results of Lillington and Townsend [1] that there is a great likelihood that $D_{_{\rm S}}(\,\delta\,)$ would be nearer to a parabolic variation in this case. We have also calculated $I_{\rm SC}(\,\delta\,)$ with different functional dependences of $D_{_{\rm S}}(\,\delta\,)$ and have found that there is no perceptible difference between the different cases. Hence while discussing $I_{\rm SC}(\delta\,)$, only the case with constant $D_{_{\rm S}}$ was mentioned.

2.3.3 Illuminated I-V Characteristics:

So far we have concentrated on two particular cases, the short circuited tand open circuited conditions, of the illuminated I-V characteristics of an MIS cell. But from the point of view of efficiency a knowledge of the complete I-V characteristics is needed. The basic equations needed for this calculation have already been developed in the earlier sections; as a matter of fact these have been used in the calculation of I_{SO} and V_{OC} . While calculating the complete I-V characteristics, the difference from the calculation of I_{SC} and V_{OC} appears in the form of more elaborate iterative procedure. This is given below.

i) Consider a given V at which I is desired. Assume $\xi_{OX}=0$.

- ii) Calculate $\emptyset_B^* = \emptyset_B + V_i$, by obtaining \emptyset_B from eqn.(2.1a) and V_i from eqn. (2.8). Since $V = V_i + V_s$, V_s is now known.
- iii) Calculate J_L from the method of Chapter 1 and $J_{\rm diff}$, $J_{\rm R1}$ and $J_{\rm tunnel}$ using eqns. (2.12), (2.13) and (2.14). Thus the minority carrier component of current is known.
 - iv) Calculate ξ_{OX} from eqn.(2.16).
 - v) Repeat steps (ii) to (iv) till convergence within required limit of error is obtained.
- vi) Obtain the minority current from step (iii) and the majority carrier one from eqn. (2.10). Thus the total current is known for the given V.
 - vii) At each V repeat the steps from (i) to (vi).

Also, note that if ξ_{OX} is taken to be zero, then, obviously no iteration is needed for ξ_{OX} and this is the case treated by Landsberg and Klimpke [12] for computing the efficiency in an MIS solar cell. In the case that there is interest in the efficiency for the non-zero value of ξ_{OX} , the iterative procedure given here can be pursued, but we have not carried out this calculation.

2.4 Summary:

In this chapter an analysis of Schottky (MIS) solar cell has been given. The effect of charges due to interface states and the effect of the splitting of the minority carrier quasi-Fermi level from the metal Fermi level have been

included in the model. This has been utilized to explain the experimentally observed features of an MIS cell (taking Au-SiO2-nSi cell as example) that the short circuit current remains constant upto some & and then starts falling, and that the open circuit voltage initially increases with δ , reaches a maximum, flattens out and then starts dropping. It is worthwhile to compare the present analysis with that of Buxo etal [13]. They have found that in the range of where \boldsymbol{I}_{SC} is falling with δ , \boldsymbol{V}_{OC} remains constant (see Fig. 3 and 4 of [13]). This result seems to be unphysical because this can only happen if ϕ_{R}^{*} increases with δ at a required rate; but this is the region where Buxo etal [13] have, in essence, assumed $extstyle{\emptyset}_{\mathtt{R}}^{m{*}}$ to be independent of δ . This discrepancy has been removed in the present chapter. In the next chapter we undertake to study an alternate method for increasing the open-circuit voltage of a Schottky-barrierbased solar cell.

CHAPTER 3

SCHOTTKY BARRIERS WITH OFFOSITELY DOPED INTERFACE LAMER

A method for increasing the open-circuit voltage of a Schottky barri∈r solar cell (SBSC) is to introduce a thin insulating layer between the metal and the semiconductor resulting in an MIS solar cell. This has already been described in the previous chapter. In this chapter we consider another recent technique which increases the opencircuit voltage of a SBSC, but as yet has not found wide prevalence in the solar cell literature. Due to this reason we would elaborate the basic principles of the method in some detail. The method consists of oppositely doping a thin layer of the semiconductor substrate before depositing the metal, thus giving rise to a metal-F-N or metal-N-P structure. Of course, one can extend the idea to jointly incorporate this thin oppositely doped layer along with a thin insulating layer resulting in a metal-(thin) insulator-P-N or metal(thin) insulator-N-F structure. A perusal of the published literature shows that so far there has been only one experimental attempt in this direction by Pai et al [1], where they have obtained the oppositely doped layer by ion implantation and then grown thin SiO_x before evaporating a thin layer of metal. cell provides some unique advantages which have been described later.

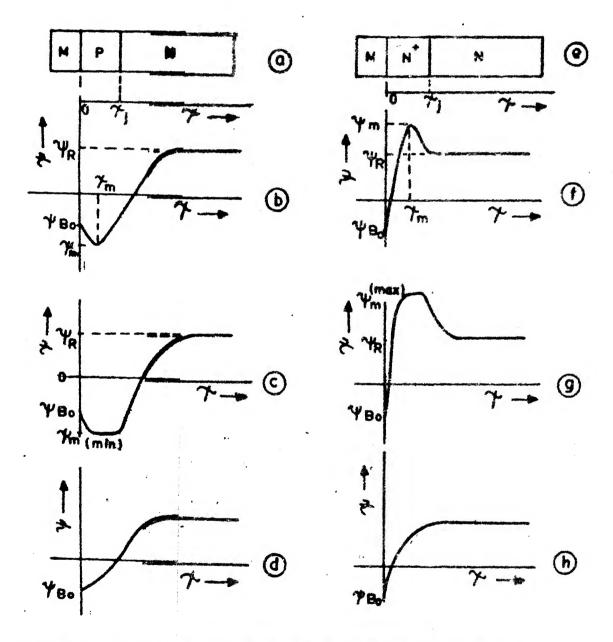
Before proceeding further, it is important to note that the usefulness of the M-F-N or M-N-P structures, which arises due to their ability to increase the effective barrier height, is not limited to solar cells only. As a matter of fact, they form a part of the class where an effective control, either decrease or increase of the barrier height is desired. Hence, in this chapter, we would keep the initial discussions at a general level so that these are applicable to many devices and later return to solar cells.

Schottky barriers are employed in a variety of semiconductor devices (for example, Schottky-gate field effect transistor [2], Schottky-barrier solar cells [3,4], injection controlled transferred electron devices [4] etc.) and in all of these it is desirable to control the height of the barrier to optimize the device performance. However, it is well known that in commonly employed semiconductors like Si, GaAs etc., this control becomes difficult because the barrier height cannot be appreciably varied by choosing metals with different work functions; rather it is largely controlled by the interface surface-state-density which is To obviate this limitation, several workers [5-10] fixed. have experimentally as well as theoretically demonstrated that the presence of a thin doped semiconducting layer at the interface can be used to control the effective barrier height. If the surface layer is of the same type as the

bulk semiconductor (e.g. metal-N+(thin)-N structure) then a decrease in effective barrier height is obtained [5,8]. A limiting case of this is obtained when the doping and thickness of interfacial layer are large so that ohmic contact is formed [5]. On the other hand, for structures like $m \in tal - (thin) F - N$ where the interface layer is oppositely doped to the bulk, an increase in the barrier height ensues. Shannon has obtained the thin interfacial layer, for both these cases by ion-implantation [6,7] and has compared the experimental and theoretical results [8]. Recently, Van-der-Ziel [9] has theoretically calculated the barrier height for epitaxial metal-F-N structure. The purpose of the analysis in the present chapter is to obtain the potential profile and thereby the range of geometrical and material parameters which would provide the control of the barrier height and then apply these to the case of solar cells. calculation includes the effect of mobile carriers which allows the determination of some of the parameters which would not have been possible otherwise. But before doing this, in the next section we give a physical description of the role of the interface layer in changing the potential profile, briefly review the work of Van-der-Ziel [9]; and then give the potential profile calculation including the effect of mobile carriers.

3.1 Fotential Frofile of Doped Interface-Layer Structure

Let us consider a metal-semiconductor Schottky diode which is characterized by the barrier height $\emptyset_{\mbox{\footnotesize{Bo}}}$ and the type and doping of the bulk semiconductor. In the following we take the bulk semiconductor to be of N type with a doping density Ng. The calculations can be easily modified for P-type bulk semiconductor. When an interface-layer (P or N type) is metallurgically interposed between the metal and the bulk semiconductor, the potential profile Ψ (x) in the vicinity of the metal contact is modified as shown in Fig. 3.1. If the interfacial layer is of opposite type to the bulk and its doping and width are suitably chosen (as discussed in Sec. 3.2), a minimum Ψ_{m} in potential appears at a distance x_m from the metal (Fig. 3.1b). Thus an effective increase in the barrier-height is obtained. If the width of the interfacial layer, keeping the doping constant, is further increased, there is a flattening of the potential profile at the minimum point and the structure behaves as a metal-Psemiconductor Schottky diode in series with a P-N junction (Fig. 3.1c). It is also possible that the width and doping of the interfacial layer is such that a minimum in potential profile does not appear, i.e. no barrier height increase takes place, as is the case in Fig. 3.1(d). When the interfacial layer is of the same type as the bulk, but is more heavily doped, then depending upon the width and doping of



Pig.3.1 Metal=P-N and Metal-N+-N structures and the potential profiles (see text for description).

this layer one may obtain an ohmic or an injecting contact. This distinction depends on two features, the first bring the condition whether the space-charge at the high-low interface is wiped out or not, and the second being the mechanism of current transport, field-emission or thermionicfield emission, at the metal contact as discussed in [5]. When the interfacial layer is heavily doped and is sufficiently thick such that potential profile of Fig. 3.1(g) ensues then the contact behaves as ohmic. If keeping the doping constant, the width of this layer is reduced to an optimum value, then the flattening at the maximum of the potential profile vanishes as shown in Fig. 3.1(f). This width of the interfacial layer is the minimum width which must be exceeded to form an ohmic contact. In the case that the potential profile is monotonic and the doping of interfacial layer is such as to lead to thermionic field-emission, an injecting contact is obtained.

We would calculate the general profiles including the effect of mobile carriers in Sec. 3.1.2. In the following section we consider an M-F-N structure and follow the treatment of Van-der-Ziel[9] where the effect of mobile carriers has been ignored.

3.1.1 Potential profile of M-P-N diode in depletion approximation

An M-P-N structure is shown in Fig. 3.1(a). Let the width of the player be $\rm W_p$ and $\rm W_n$ be the width over

which the space charge region extends into the n-region and let x=0 be at the metal contact. Further, assume that an abrupt junction has been made. Then in the depletion approximation Poisson's equation are

$$\frac{d^2 \Psi}{dx^2} = \frac{q N_a}{\epsilon s o} \quad \text{for} \quad 0 < x < W_p$$
 (3.1a)

and

$$\frac{d^{2}\Psi}{dx^{2}} = -\frac{qN_{d}}{\varepsilon_{s}\varepsilon_{o}} \quad \text{for } W_{p} < x < (W_{p} + W_{n})$$
 (3.1b)

where q is the charge of the electron, $\epsilon_{_{\rm S}}$ is the dielectric constant of the semiconductor and $\epsilon_{_{\rm O}}$ is the permittivity of the free space.

The initial conditions are:

(a)
$$\Psi$$
 (o) = 0, Ψ ($W_p + W_n$) = $\emptyset_{m1} - \emptyset_n - V$ (3.2)

where $\binom{9}{m1}$ and $\binom{9}{n}$ denote the work functions of the metal electrode and the n type semiconductor and V is the applied voltage.

(b)
$$\Psi(x)$$
 and $d\Psi/dx$ are continuous at $x = W_p$.

(c)
$$\frac{d\Psi}{dx}\Big|_{0} = \frac{qN_{d} W_{n} - qN_{a}W_{p}}{\varepsilon_{s} \varepsilon_{o}}$$
 (3.3)

$$\frac{d\Psi}{dx} \mid (W_{p} + W_{n}) = 0$$
 (3.4)

The solution for $0 \le x \le W_p$ is

$$\Psi^{V}(x) = \Psi_{1}(x) = \frac{q^{N}a}{\varepsilon_{s}\varepsilon_{o}}(\frac{1}{2}x^{2} - x W_{p}) + \frac{q^{N}d}{\varepsilon_{s}\varepsilon_{o}} W_{n}x$$
 (3.5)

whereas for $W_{p} \le x \le W_{p} + W_{n}$.

$$\Psi(\mathbf{x}) = \Psi_{2}(\mathbf{x}) = -\frac{qN_{d}}{\varepsilon_{s}\varepsilon_{0}} \left[\frac{1}{2}\mathbf{x}^{2} - \mathbf{x}(W_{n} + W_{p})\right] - \frac{1}{2}\frac{q(y_{a} + N_{d})}{\varepsilon_{s}\varepsilon_{0}}W_{p}^{2}$$
(3.6)

The width of the space-charge in the N-region is obtained from the second boundary condition of eqn. (3.2a), that is

$$\emptyset_{m1} - \emptyset_n - V = \frac{1}{2} \frac{q^N_d}{\varepsilon_S \varepsilon_O} (V_p + V_n)^2 - \frac{1}{2} q (\frac{N_a + V_d}{\varepsilon_S \varepsilon_O}) V_p^2$$
 (3.7)

When N_d W_n < $N_a W_p$, a potential minimum exists in front of the metal electrode. The position x_m follows from the condition dy/dx = 0 at $x = x_m$, which gives

$$\frac{qN_{a}}{\varepsilon_{s}\varepsilon_{o}}(x-W_{p}) + \frac{qN_{d}}{\varepsilon_{s}\varepsilon_{o}}W_{n} = 0$$
or
$$x = x_{m} = W_{p} - \frac{N_{d}}{N_{a}}W_{n}$$
(3.8)

whereas its depth $\Delta \emptyset_B(V)$ is determined by substituting $x = x_m$ in eqn. (3.5).

Using some assumed values of the relevant parameters, Van-der-Ziel [9] has computed the amount of increase of barrier height which gives physical results. However, we have found that though the computations of [9] are valid for the range of parameters given in that paper, great caution must be exercised when extending this to a different combination of the values of parameters. This is mainly because of the reason that in [9] only a necessary condition

for the increase of barrier height has been taken into account, whereas another condition needed for sufficiency of this has been ignored. This would be discussed in Sec.3.2. Further, note that Van-der-Ziel has noted that in order to get meaningful results for a given N_a and N_d , the width of the F-layer should have a lower bound $W_p(\min)$ and an upper bound $W_p(\max)$. But his analysis not amenable to direct calculations of $W_p(\min)$ and $W_p(\max)$, rather a trial and error method has to be adopted. A method which includes the effect of mobile carriers and allows the direct calculation of $W_p(\min)$ and $W_p(\max)$ has been developed in this thesis and is given in Sec. 3.2. But before giving this the general calculations including the effect of mobile carriers (but in thermal equilibrium) for both $M-N^+-N$ and M-P-N are given in the following section.

3.1.2 Potential profiles of M-P-N and M-N+-N Structures:

The potential profile $\Psi(x)$ can be obtained by solving the Poisson's equation:

$$\frac{\mathrm{d}^2 \Psi}{\mathrm{d} x^2} = -\frac{\mathrm{q}}{\varepsilon} \left[\mathbb{N}(x) + p - n \right] \tag{3.9}$$

where N(x) is net doping density and n and p are, respectively the electron and the hole concentrations. The symbols q, ϵ_s , ϵ_0 have been described in the previous section. The following cases where a solution of eqn. (3.9) can be obtained are of our interest.

- (a) The effect of mobile carriers is ignored, i.e. p=n=0. This is the case discussed in the previous section. The calculations done there has inherent limitations as would become clear from the following discussion. As barrier height increases, for a P-type interface the valence band approaches the Fermi level and the number of minority carrier increases. Thus a limit is reached where the calculations done under depletion approximation become meaningless. One would be interested in knowing this limit below which the depletion approximation can be used. It is obvious that this limit can only be obtained if minority carriers are included in the calculation and the point where departure from the results of depletion approximation occurs, is noted. This has been our motivation for including the effect of mobile carriers in the calculation given below. To the best of our knowledge such an approach has not been taken earlier.
- (b) The effect of mobile carriers are included but only thermal equilibrium condition is considered. In this case a closed-form expression for n and p can be obtained either by making Ehrenburg's [11,12] or Boltzman's approximation to the Fermi-Dirac distribution function. In the case that one makes Ehrenburg's approximation, one gets [11,12]

$$p = 4N_v \left[4 \exp(\frac{E_G}{2} + q \Psi)/kT + 1\right]$$
 (3.9a)

and

$$n = 4N_{C} \left[4 \exp(\frac{E_{G}}{2} - q \Psi)/kT_{+}1\right]^{-1}$$
 (3.9b)

where E_G is the bandgap, and N_C and N_V are, respectively, the effective density of states of the conduction and valance band. These expressions for p and n are valid even for degenerate semiconductors in case the excursion of the Fermi-level in the bands does not exceed 2kT. Hence these equations are to be used if any of the semiconductors are degenerately doped. Here the reference potential corresponds to the Fermi-level in the metal.

In the case that Boltzmann approximation is used to express p and n, one obtains

$$p = n_i \exp(-q\Psi/kT)$$
 (3.9c)

$$n = n_i \exp(q\Psi/kT) \tag{3.9d}$$

where n_i is the intrinsic carriers concentration. Here the reference of Ψ is the point where $p=n=n_i$. The solutions of eqn. (3.9) with Ehrenburg's approximation are given in this section. Those with Boltzmann approximation can be easily obtained following similar analysis.

(c) The effect of mobile carriers are included and either reverse biased or forward biased devices are considered. In these cases, ideally, the current continuity equations and the Poisson's equation should be simultaneously solved. However, since the equations are coupled and nonlinear, it becomes extremely difficult to get closed form or simple

numerical methods of solution. A simplification can be brought in by considering the reverse-biased case where negligible current flows. Since in this case the potential profile can be obtained by solving Poisson's equation alone. Furthermore, one can simplify the situation by considering either only p or n and not both; for an example in the case of M-P-N diode, in the depletion region only p, and not n, need be considered. This point would be further elaborated at the end of Section 3.2. In the case that a diode is forward biased there is no choice but to solve the coupled equations mentioned earlier. The only exception is the case of an open circuited solar cell, using this structure, since in this case again no current flows.

Let us now solve eqn. (3.9) using (3.9a) and (3.9b) for the case of thermal equilibrium. We would take the doping to be abrupt such that $N(x) = N_1$ for $x < x_j$ and $N(x) = N_2$ for $x > x_j$, where x_j denotes the metallurgical junction. Eqn. (3.9) is normalized such that $\psi = (q\psi/kT)$, $\chi = x/L_D$ where L_D is the Debye length for doping N_1 , i.e. $L_D = [kT \in_S \varepsilon_0/(q^2 N_1)]^{\frac{1}{2}}$ and the impurity and carrier densities are normalized with respect to N_1 . We now restrict our attention exclusively to the potential profiles of the form of either Fig. 3.1(b) or 3.1(f). In these cases, to the right of χ_j the electric field is zero for $\psi = \psi_R$ and to the left of χ_j it is zero at $\psi = \psi_M$. Using these values to

eliminate the constant of integration, we integrate the normalized form of eqn. (3.9) for $\chi < \chi_j$ and $\chi > \chi_j$ to obtain

$$\frac{d\psi}{d\chi}\Big|_{\chi<\chi_{\bar{j}}}^{2} = \pm 2^{\frac{1}{2}} \left[-\frac{N_{2}}{N_{1}} (\psi - \psi_{m}) - 4(\frac{N_{v}}{N_{1}}) \ln \frac{F(\mu = \psi_{m})}{F(\mu = \psi)} \right]$$

$$- 4(\frac{N_{c}}{N_{1}}) \ln \frac{F(\mu = -\psi_{m})}{F(\mu = -\psi)} \Big]^{\frac{1}{2}}$$
(3.10)

$$\frac{d\psi}{d\chi}\Big|_{\chi>\chi} = \pm 2^{\frac{1}{2}} \left[-(\psi - \psi_R) - 4(\frac{N_V}{N_1}) \ln \frac{F(\psi = \psi_R)}{F(\psi = \psi)} - 4(\frac{N_C}{N_1}) \ln \frac{F(\psi = -\psi_R)}{F(\psi = -\psi)} \right]^{\frac{1}{2}}$$
(3.11)

where

$$F(\mu) = 1 + 0.25 \exp(-\frac{E_{G}}{2k\pi} - \mu)$$
 (3.12)

and ψ_R is obtained by solving $N_1+p-n=0$ in the normalized notation and is given as

$$\Psi_{R} = \ln \left[\left(A_2 + \left(A_2^2 + 4A_1 A_3 \right)^{\frac{1}{2}} \right) / 2A_1 \right]$$
 (3.13)

where
$$A_1 = 4 \exp(+E_G/2kT) [1 + (4N_v/N_1)]$$

 $A_2 = 16 \exp(+E_G/2kT) + 1 + (16/N_1)(N_v-N_C)$
 $A_3 = 4 \exp(+E_G/2kT) [(4N_C/N_1) - 1]$

The signs in eqn. (3.10) are chosen as follows. For metal P-N diode (Fig. 3.1b) the negative sign is taken for $\chi_m < \chi < \chi_j$ and positive for 0 < χ < χ_m . The case for metal N⁺-N diode (Fig. 3.1f) is just opposite. In eqn. (3.11), the negative sign is taken for metal-P-N diode and positive one for metal-N⁺-N diode. Using the proper signs and noting that the

electric field and the potential are continuous at metallurgical junction $X = X_j$, one obtains the potential ψ_j at χ_j by equating eqns. (3.10) and (3.11) as:

$$x_{j} = \left(\frac{N_{2}}{N_{1}} - 1\right)^{-1} \left[\left(\frac{N_{2}}{N_{1}}\psi_{m} - \psi_{R}\right) + \left(\frac{4N_{v}}{N_{1}}\right) \ln \frac{F(\mu = \psi_{R})}{F(\mu = \psi_{m})} + \left(4N_{c}/N_{1}\right) \ln \frac{F(\mu = -\psi_{R})}{F(\mu = -\psi_{m})}\right]$$

$$(3.14)$$

The use of eqns. (3.9) to (3.14) allows the determination of . . the potential profile in the following manner:

- (i) If the doping N_1 of the bulk semiconductor is known then Ψ_R is determined from eqn. (3.13). Note that N_1 is a positive quantity for donor impurities.
- (ii) A knowledge of N₂ and ψ_m , along with the value of ψ_R , allows the determination of ψ_j from eqn. (3.14). Here N₂ is a positive quantity for donor impurities and a negative quantity for acceptor impurities. Methods for choosing the value of ψ_m in particular cases are given in Sections 3.2 and 3.3.
- (iii) Starting from the value of $\boldsymbol{\psi}_{\,j},$ the next step is to use the Taylor-expansion:

$$\Psi_{i+1} = \Psi_{i} + (X_{i+1} - X_{i})\Psi_{i}^{t} + \frac{(X_{i+1} - X_{i})^{2}}{2!}\Psi_{i}^{"} + \cdots$$
(3.15)

where the primes denote differentiation with respect to χ . It is to be noted that the expansion eqn. (3.15) also determines the optimum step-size at each step to obtain a

desired amount of accuracy [13]. This is so because at each step ψ_1^* is known from eqn. (3.10) or eqn. (3.11) and ψ_1^* is known from eqn. (3.9). Thus taking the ratio of the third term to the second one on the right of eqn. (3.15) and equating it to a fixed value, depending on desired accuracy, one can obtain the value of $(x_{i+1} - x_i)$ at that step.

- (iv) Now the potential profiles in three different regions $0 < x < x_m$, $x_m < x < x_j$ and $x > x_j$ are obtained separately. Starting from ψ_j , eqn. (3.15) is used to the left till the chosen value of ψ_m is reached. This gives the potential profile for $x_m < x < x_j$. It is important to note that the distance $(x_j x_m)$, which was unknown, has also been determined. Repeating the steps to the right of ψ_j till the potential reaches ψ_R , i.e. the neutral regions, the potential profile and the corresponding width of the space charge are obtained for $x > x_j$.
- (v) The solution for the region 0 < χ < χ_m requires the value $\psi = \psi_{Bo}$ at $\chi = 0$. This can be obtained by knowing the barrier height \emptyset_{Bo} without the interfacial layer. For the reference of potential chosen here, one obtains (see inset of Fig. 3.2):

$$\Psi_{Bo} = (E_g / 2 - \emptyset_{Bo}) / kT$$
 (3.16)

Starting from ψ_{30} at $\chi=0$, expansion in eqn. (3.15) is used to the right till the potential ψ_m is reached. Thus the

potential profile for the region 0 < $\chi < \chi_m$, along with the unknown distance χ_m , is determined.

(vi) A knowledge of $(\chi_j - \chi_m)$ and χ_m allows the determination of χ_j , the metallurgical width of interface layer, for given values of N₁, N₂ and ψ_{Bo} so that a desired value of ψ_m is obtained. It is to be emphasized that the determination of this width is a significant advantage of the present method of calculation and is of help in designing the interfacial layer as is shown in the following sections.

So far we have considered the potential profiles which have an extremum but there is no flattening of the profile there. Next, let us consider the profiles given in Figs. 3.1(c) and -3.1(g). To determine the profiles in these cases the metallurgical width of the interface layer, along with the values of N₁, N₂ and ψ_{BO} , should be known, because the present method cannot determine the width of the flat region near the extremum. The problem becomes basically of finding the potential-profile and the width of spacecharge layer for Schottky barrier between the metal and the interface layer, and those of the high-low (or F-N) junction between the interface layer and the bulk semiconductor. All of these can be easily obtained by the present method. Subtraction of the sum of widths of space charge layers of Schottky:barrier and high-low (or P-N) junction from the metallurgical width of the interface layer determines the

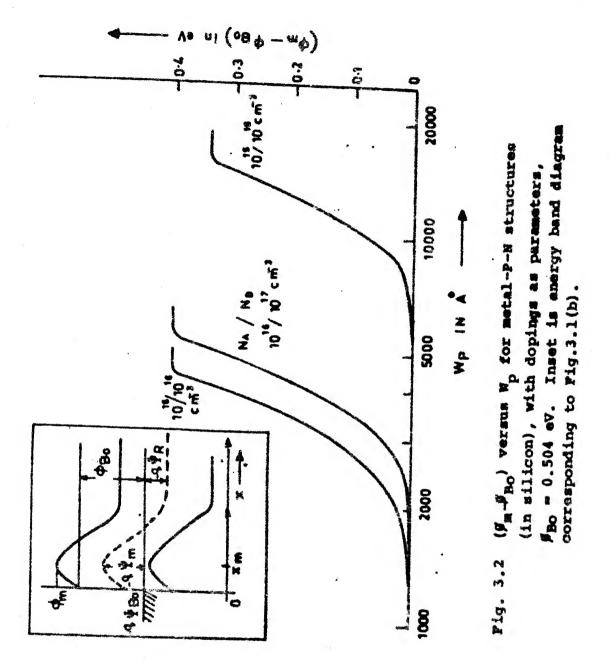
width of the flat region at the extremum. Thus the potential profiles of the type shown in Figs. 3.1(c) and 3.1(g) can be determined. It should be mentioned here that this method, in a different context and with Boltzman's rather than Ehrenb rg's approximation of Fermi-Dirac integral, has been used earlier for high-low (or P-N) junctions with all the impurity atoms ionized [13] and with incomplete ionization of impurities [14]. However, in each of these cases the doping of high side is large enough that Boltzman approximation is not valid and the present method should be used to get accurate results.

The remaining profiles where there is no extremum but the interface layer is present cannot be obtained by the present method. This is because the constant of integration in obtaining eqn. (3.10) cannot be determined now.

In the following sections, use is made of the calculations given above to determine the parameters of the interface layer.

3.2 Barrier Height Increase in Metal-F-N Structures:

It has already been mentioned that an interfacial layer which is oppositely doped to the bulk semiconductor increases the barrier height, provided the width and doping of this layer are properly chosen. This is shown in the inset of Fig. 3.2. The considerations that help the determination



of these parameters for a metal-P-N structure are discussed in this section. First we would consider the case of thermal equilibrium and then the cases with applied bias.

3.2.1 Thermal equilibrium conditions:

The aim is to determine the parameters such that a profile of the type of Fig. 3.1(b), and not of type of Fig. 3.1(c) where a P-N junction is formed or of type Fig. 3.1(c) where no barrier increase is available, is obtained. This constrains the value of ψ_{m} , which was taken as a parameter in Sec. 3.1 to lie between $\psi_{BO}^{<\psi} \psi_{m}^{<\psi}$ (min). The fact that ψ_{m} has to be less than ψ_{BO} for barrier height in crease is obvious. The value of $\psi_m(min)$ is shown in Fig. 3.1(c) and is determined only by doping N_a of the P-layer at a given temperature. It can be obtained by solving $(-N_a+p-n) = 0$ in the normalized notation and is given by eqn. (3.13) with N_1 replaced by $-N_a$. The fact that $^{\Psi}$ m(min) is determined only by N_a at a given temperature leads to an important conclusion, i.e. the value of $N_{\mathbf{a}}$ corresponding to $\psi_{m}(\min) = \psi_{Bo}$ is the minimum value, $N_{a}(\min)$, which must be exceeded to obtain an increase in barrier height.

Theoretical calculations without recognising the existence of $N_a(min)$ can lead to misleading conclusions as would be evident from the following numerical example. Van-der-Ziel [9] has obtained the potential profile for a

metal-p-n structure without including the effect of mobile carriers. He has concluded that for a barrier height increase to take place, the inequality:

$$N_{a} W_{p} > N_{d} W_{n}$$
 (3.17)

must be satisfied, where \mathbb{W}_{n} is the width of the space-charge layer on N-side of the metallurgical junction. For example, silicon this is the case for $N_d = 10^{15} \text{ cm}^{-3}$, $\phi_{RO} = 0.907 \text{ eV}$, $N_a = 10^{16} \text{ cm}^{-3} \text{ and } W_D = 1000 \text{ Å, where} \qquad W_n \text{ from [9] is}$ 8800 Å. For this case, Van-der-Ziel's calculation predicts that a barrier height increase of 2 m eV would be obtained and the peak in the potential-energy profile of electron would be located 120 Å in front of the metal. Actually this conclusion is misleading because for this case $N_a(\min)$, using eqns. (3.16) and (3.13) with N_1 representing $-N_2$ (min), is 1.29×10^{16} cm⁻³ which is larger than the value of N_a chosen here; hence there is no possibility of obtaining a barrier height increase. Thus the inequality $N_a > N_a$ (min) along with the inequality eqn. (3.17) forms the necessary and sufficient condition for a barrier height in crease to take place. Note that the inequality (3.17) is useful when the effect of mobile carriers is neglected, however, the requirement $N_a > N_a(min)$ is valid in all the cases.

Let us choose a value of $N_a > N_a(\min)$. The considerations that help in determination of N_a in a particular case are given later. Presently our concern is to determine the

range $W_p(\text{min}) < W_p < W_p(\text{max})$ of the width of p-layer, for a given N_a such that an increase of barrier height, but without the formation of a P-N junction, is obtained. This can be done by following the method of Sec. 3.1. The value of $W_p(\text{min})$ is obtained when eqn. (3.9) is solved for $\psi_m = \psi_{B0}$. Similarly, the value of $W_p(\text{max})$ is obtained for $\psi_m = \psi_m(\text{min})$ for given value of N_a . It is expected that the determination of $W_p(\text{min})$ and $W_p(\text{max})$ would be of help in the proper fabrication of these devices.

The general nature of the barrier height increase $\Delta \emptyset = \emptyset_{m} - \emptyset_{Bo}, \text{ as a function of } \mathbb{W}_{p} \text{ with the doping } \mathbb{N}_{a} \text{ treated}$ as a parameter for silicon at 300°K. is shown in Fig. 3.2. The following features of this figure should be noted.

- (a) For increasing value of N_a , the maximum attainable $\Delta \emptyset$ increases. However, the largest usable value of N_a may be limited by the solubility limit of the dopant, or by the fact that as N_a increases the required value of W_p gets smaller making the fabrication difficult, or that $(d\Delta \emptyset / dW_p)$ becomes sharper so that more precise control of thickness is needed.
- (b) For $W_p > W_p(\text{max})$, in each case, a constant value of $\Delta \emptyset$ has been shown. This is the region where P-N junction forms which is generally undesirable. In conventional calculations [9], this saturation cannot be obtained; rather a monotonic increase in $\Delta \emptyset$ would continue with increasing W_p .

This can be misleading, in as much as instead of improving the performance by increasing the barrier height the performance would deteriorate due to formation of P-N junction.

Before concluding this section, it should be mentioned that the general analysis given in the previous section which has been used to analyse M-P-N structures in the present section can also be used to analyse M-N⁺-N structures. Here there are two cases of interest; one of ohmic contact and the other of injecting contact.

A. Ohmic Contacts: In this case the potential profile is that of Fig. 3.1(g) where the space charge at the high-low junction is present and provides space-charge-limited current to the bulk semiconductor. Since the metal-N+ depletion layer is separated by a flat potential from the high-low depletion region, the presence of the interface layer does not modify the barrier for tunneling, hence the value of doping required for field-emission would be the same as given in Ref. 15. Regarding the width of the interface layer, it should be noted that it must be larger than a critical width, tmin, to ensure the separation of the depletion layer of metal-N+ layer from that of the high-low junction by a flat profile. The width t_{min} corresponds to the case of Fig.3.1(e), where the flat region has just disappeared, i.e. the value of the peak in potential is still at Y corresponding to Nd2. It is expected that a knowledge of the value of t_{\min} would be

of interest during the fabrication of Ohmic contacts, since it must be exceeded to provide ohmic behaviour. The calculation of t_{\min} is analogous to that of $W_p(\max)$ in Sec. 3.2, hence is not repeated here.

B. <u>Injecting Contacts</u>: To ensure injecting contacts, the doping and the width of the interface layer are chosen so that the effective barrier height is decreased by a controlled amount. A systematic study of these contacts is of recent origin [5,8] and experimental results to achieve injecting contacts, particularly in N-InP by epitaxial growth [16] and by controlled diffusion of sulfur [17] have been recently reported. Unfortunately, the present method of calculation of potential-profile fails in this particular case, which corresponds to Fig. 3.1(h), as has already been mentioned in Sec. 3.1.

Before concluding this section it must be mentioned that the behaviour of the ohmic and injecting contacts alike that of the MPN structure, is critically sensitive to the applied voltage, hence the present method of analysis which is only valid in thermal-equilibrium is of limited interest in these cases. In the next section we give an approximate method of analysis to study the MPN structure in non-equilibrium situation. Similar analysis, with some changes, can also be used for the study of ohmic contacts; but for reasons mentioned earlier it cannot be used for injecting contacts.

3.2.2 Barrier Height increase in M-P-N structure in non-thermal equilibrium

The barrier height increase given in Fig. 3.2 would be only valid when no voltage is applied. In the case that the device is forward biased the following situation arises.

The barrier height would increase with increasing forward bias. Due to this the number of holes in the P-layer would increase and beyond a point one can no longer assume that the P-layer is completely depleted; rather a current due to minority current injection starts flowing. Thus the major advantage of a Schottky barrier diode of being a majority carrier device is lost. This limits its main advantage of fast switching in switching applications. In solar cell applications this means an increased forward current at a given voltage which would lead to deterioration in performance. Thus it is clear that the useful barrier height increase would be much less than the P-N junction limit given in the case of thermal equilibrium.

The quantitative information about this cannot be obtained by solving the Poisson's equation alone but current continuity also has to be solved. This gets to be an involved problem due to the coupling of these equations. A decoupling can be obtained in the case that the imrefs ϕ_p and ϕ_n are assumed to be constant in the space charge region. The constancy of ϕ_n follows from the assumption of majority

carrier current transport by thermionic emission and that for \emptyset_p follows from the assumption of minority carrier current transport by diffusion model [18]. It is important to note that since the profiles of \emptyset_p and \emptyset_n are already assumed, the problem can be solved only by solving the Poisson equation and noting that $\emptyset_p - \emptyset_n = qV$.

The solution of Poisson equation itself can be simplified by further approximations that p >>n, which remains to be valid excepting at a distance of a few Debye lengths in the vicinity of the edge of the space charge layer. Thus eqn. (3.9), using Boltzmann approximation can be written as

$$\frac{d^2 \Psi}{dx^2} = -\frac{q}{\epsilon_0 \epsilon_0} [N(x) + n_i \exp(-q \Psi / kT)] \qquad (3.18)$$

It is important to note the simplicity of eqn. (3.18) which has resulted by taking the imref of minority carriers (holes) to be constant throughout the space charge region and coincident with the metal-Fermi level even when the bias is applied. The majority carrier (electron) imref is displaced from the metal Fermi level by qV, but since the relation p>> n has been used, the applied voltage does not appear in eqn. (3.18). The effect of applied voltage is taken by modifying the boundary condition in the bulk of the semiconductor.

Let us now solve eqn. (3.18) for an MPN diode where the doping of P and N layers is taken to be abrupt such that

$$N(x) = -N_A$$
 for $x < x_j$
= N_D for $x > x_j$

where x_j is the metallurgical width of the P-layer taking the metal semiconductor interface as the origin. Let us also normalize eqn. (3.18) such that

$$\psi = q\psi/kT$$
 , $\chi = x/L_D$

where

$$L_{D}^{2} = \left(\frac{\varepsilon_{s} \varepsilon_{o} kT}{q^{2} n_{i}}\right),$$

and the dopings are normalized with $\boldsymbol{n_i}\text{,}$ such that

$$N_1 = -N_A/n_i$$
 for $x < x_j$
 $N_2 = N_D/n_i$ for $x > x_j$

We assume a potential profile such that a minima ψ_m appears. This gives a boundary condition $d\psi / d\chi = 0$ where $\psi = \psi_m$. The other boundary condition is obtained in the bulk of the semiconductor such that $d\psi/d\chi = 0$ where $\psi = \psi_R - V$, where ψ_R is the diffusion potential in the bulk and is given by eqn. (3.21). V is the applied voltage which is taken to be positive for forward bias.

Integrating eqn. (3.18) once with ψ and using the above boundary conditions in the proper regions, one obtains:

for $\chi < \chi_j$;

$$\frac{1}{2}(d\psi/d\chi)^2 = [-N_1(\psi - \psi_m) + \exp(-\psi) - \exp(-\psi_m)] \quad (3.19)$$

for $\chi > \chi_{i}$;

$$\frac{1}{2}(d\psi/d\chi)^{2} = [-N_{2}(\psi-\psi_{R} + V) + \exp(-\psi) - \exp\{-(\psi_{R}-V)\}]$$
(3.20)

The diffusion potential in the bulk can be determined from the charge neutrality condition as

$$\Psi_{R} = \ln \left[\frac{N_2}{2} \left\{ 1 + \left(1 + \frac{4}{N_2^2} \right)^{\frac{1}{2}} \right\} \right]$$
 (3.21)

Using the fact that $d\psi/d\chi$ and ψ have to be continuous at $\chi=\chi_j$; also using eqns. (3.19) and (3.20) we get

$$\psi_{j} = \frac{N_{1} \psi_{m} + N_{2} (V - \psi_{R}) + \exp(-\psi_{R} - V) - \exp(-\psi_{m})}{(N_{1} - N_{2})}$$
(3.22)

Now all the relations for obtaining the potential profile have been obtained. The calculations can proceed exactly (see steps (i) to (v) after eqn. 3.14) as in the case of thermal equilibrium given in Sec. 3.1.2.

It has already been mentioned that the advantage of a barrier height increase using a P-layer in M-P-N structure gets nullified if minority carrier current gets

dominant. An idea about the range where the effect of mobile carrier starts dominating can be easily obtained by considering eqn. (3.19). Using this equation, we have plotted $(d\psi/d\chi)^2$ at $\chi=0$, versus ψ_m in Fig. 3.3. The plot has been given for three values of $N_1=-N_A$, which along with other parameters of interest is given in Fig.3.3. The solid curve is for the ease when mobile carriers have been ignored, i.e. the exponential terms in eqn.(3.19) have been neglected. The dotted curves are with mobile carriers taken into account and the points where they depart from the solid curve demark the values of ψ_m above which the neglect of mobile carriers would lead to erroneous results. Also note that the points A(i), A(ii) and A(iii) on the ψ_m axis denote the upper limits on ψ_m for the respective dopings due to the formation of P-N junction.

3.2.3 Open circuit voltage of solar cells using MPN structure:

From the point of view of solar cells the main advantage of M-P(thin)-N Schottky barriers over M-N Schottky barriers is due to the increased open circuit voltage ensuing from the increase in barrier height. The open circuit voltage is obtained by equating the diode forward current to the light generated current and solving for the resulting voltage.

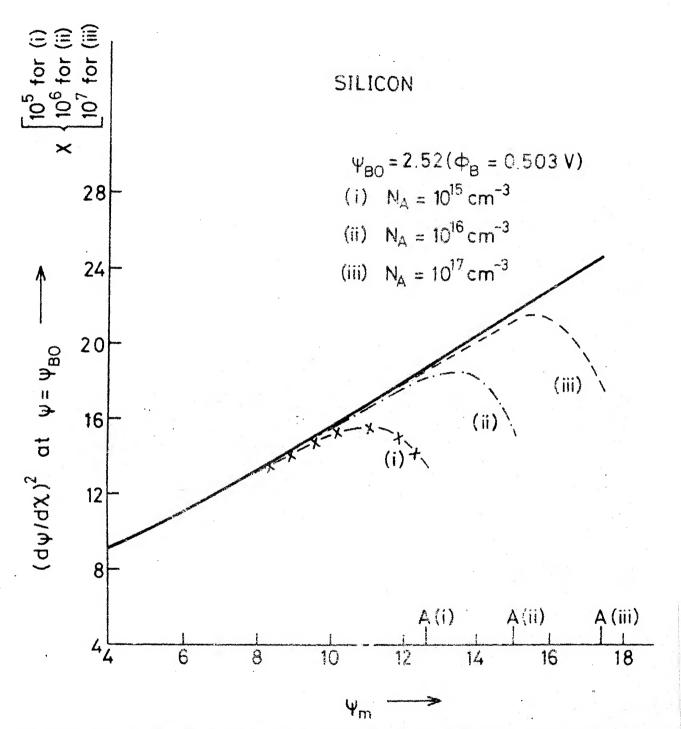
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3.3 Deviation from deplection approximation (solid line) with mobile carriers (dotted line): Note the scale change in both the cases

I =
$$aA^{**} T^2 \exp[-q(\frac{\emptyset_{Bo} + \Delta \emptyset_{B}(V)}{kT})][\exp(qV/kT)-1]$$
 (3.23)

where \emptyset_{Bo} is the barrier height of M-N structure and $\Delta\emptyset_B(V)$ is the barrier height increase at voltage V due to the presence of P-layer. Other symbols have their usual meaning. We assume that V>> (kT/q) so that unity can be neglected compared to $\exp(qV/kT)$. Let us Taylor expand $\Delta\emptyset_B(V)$ around $\Delta\emptyset_B(v)$, where $\emptyset_B(v)$ is the barrier height increase in thermal equilibrium due to the P-layer. One gets

Using equation (3.24) in (3.23) and rearranging one gets

$$I = aA^{**} T^{2} \exp\left[-\frac{q(\emptyset_{BO}^{+\Delta} \emptyset_{B}(o))}{kT}\right] \exp(qV/kT)$$
 (3.25) where

$$n = \frac{1}{1 - \frac{d(\Delta \emptyset_B(V))}{dV} \Big|_{V=0}}$$
 (3.26)

If the value of $\frac{d(\Delta \phi_B(V))}{dV}\Big|_{V=0}$ is small compared to unity such that n = 1, one can use $\Delta \phi_B(o)$ calculated for thermal equilibrium to obtain the open circuit voltage. If I_L is the light generated current in this case one gets:

$$V_{OC} = \emptyset_{Bo} + \Delta \emptyset_{B}(0) + \frac{kT}{q} \ln(\frac{I_{L}}{aA^{**}T^{2}})$$
 (3.27)

Using the values of $\Delta \phi_{\rm B}(\rm o)$ from Fig.3.2, the values of $V_{\rm OC}$ has been obtained for $\phi_{\rm Bo} = 0.503$ V, $I_{\rm L} = 25$ mA/cm², a = 1 cm²,

A** = 120 Amp/cm²/°K² and T = 300 °K. The plot of V_{OC} versus W_p , for $N_D = 10^{15}$ and 10^{16} cm⁻³ and N_A = 10¹⁵ and 10¹⁶ cm⁻³ is given in Fig. 3.4(a).

Recently Card [18] has done an experimental study where he has done a 'solid-state-epitaxial' deposition of the thin P-layer on N-type silicon by heat treating evaporated aluminium layers. The experimental results of Card [18] are shown in Fig. 3.4(b). The abscissa is the temperature of heat treatment, which in effect determines N_A and W_p . Whereas a quantitative comparison of Figs. 3.4(a) and 3.4(b) is not possible due to lack of knowledge of the exact experimental parameters, the striking similarity of the plots is noteworthy.

3.3 Metal-(thin)Insulator-P-N Structures

A major disadvantage of the tunneling MIS solar cell discussed in the previous chapter is that its open circuit voltage varies critically with the thickness of the insulating layer. Thus the control of the open circuit voltage from the point of view of reproducibility from run to run needs stringent control on processing. It will be shown in this section that if thin oppositely doped layer is grown on the semiconductor substrate before growing the oxide, then the advantage of the increase of open circuit voltage is maintained but its critical dependence on the thickness of the insulating layer is obviated.

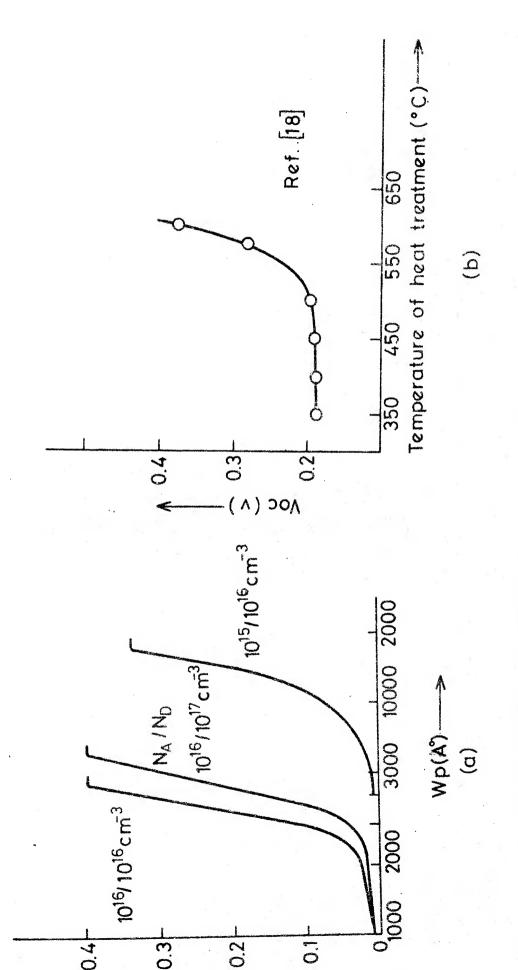


Fig. 3.4 Effect of interfacial layer on Voc.

In the following we would consider a metal-(thin) insulator-P-N structure (MIPN); the considerations for a metal-(thin)insulator-N-P structure (MINP) are analogous and can be easily followed. A band diagram of MIPN solar cell is shown in Fig. 3.5(a).

It is obvious that there are two ways of analysing this type of cell. One can either start with MPN structure and study the effect of increasing the oxide layer or one can start with an MIS cell and study the effect of the width and doping of the P-layer. We have taken the latter approach, i.e. we have modified the equations of the MIS cells given in Chapter 2, but used the same analysis of MPN structure as given earlier in this chapter. While considering MPN structure, for simplicity, we have ignored the mobile carriers.

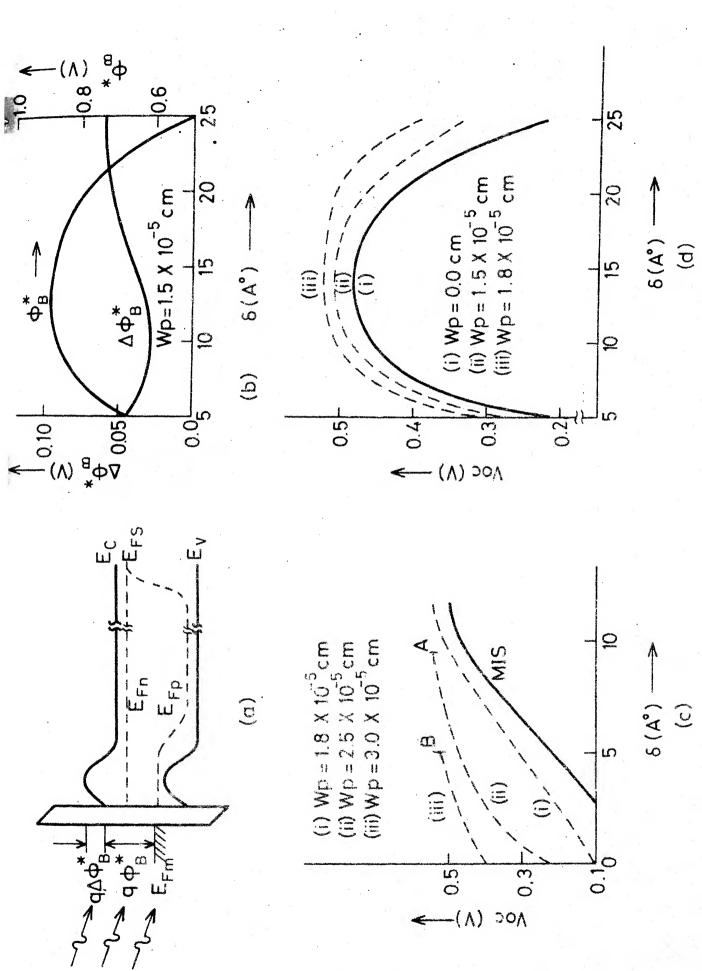
Let us consider the open circuit voltage of the cell shown in Fig.3.5(a). This can be obtained by solving for V from $J_n+J_p=0$, where J_n and J_p are the majority and minority carrier components of current. The modified expression for J_n is

$$J_{n} = A^{**}T^{2} \alpha_{n} \exp\left(-\frac{q(\emptyset_{B}^{*} + \Delta \emptyset_{B}^{*})}{kT}\right) \left[\exp(qV/kT) - 1\right] \qquad (3.28)$$

Note that this equation is the same as in the case of MIS cell excepting the presence of the term $\Delta \ p_B^*$ which has been added to p_B^* . The value of $\Delta \ p_B^*$ for a given doping and width



Fig. 3.5 For details see text.



(3.31)

of the P-layer can be obtained from Van der-Ziel's analysis given in Section 3.1.1. Regarding the minority carrier current J_p , we have assumed it to be the same as in the case of the MIS cell. The expression for the open-circuit voltage of the MIPN cell is now obtained following steps which are similar to those in the case of MIS cell. The resulting expression for $V_{\rm OC}$ is

$$-\mu_{3} + [\mu_{3}^{2} + \frac{4J_{L}\alpha_{p} \exp{\{(-E_{g} + 2q\beta_{B}^{*} + q\Delta\beta_{B}^{*})/kT\}}]^{\frac{1}{2}}}{\alpha_{n}(J_{diff}^{!} + J_{R}^{!})}$$

$$V_{OC} = \frac{kT}{q} \ln{[\frac{\alpha_{p} \exp{[(E_{g} + 2q\beta_{B}^{*} + q\Delta\beta_{B}^{*})/kT]} + J_{tunnel}^{!}/(J_{diff}^{!} + J_{R}^{!})}}{2}$$
 (3.29) where $\mu_{3} = \frac{\alpha_{p}}{\alpha_{n}} \exp{[(E_{g} + 2q\beta_{B}^{*} + q\Delta\beta_{B}^{*})/kT]} + J_{tunnel}^{!}/(J_{diff}^{!} + J_{R}^{!})}$ (3.30) and all other terms excepting β_{B}^{*} have been defined in Chapter 2. Note that if the diffusion and recombination components are small such that J_{diff} and J_{R} are negligible, then eqn. (3.29) reduces to

Computations have shown that the values of V_{OC} from eqns.(3.29) and (3.31) are in very good agreement for low values of δ .

 $V_{OC} = \frac{kT}{a} \ln(J_{L}/A^{**}T^{2}\alpha_{n}) + (\emptyset_{R}^{*} + \Delta \emptyset_{R}^{*})$

The open circuit voltage of the MIPN structure as a function of the thickness of the insulating layer with width of the P-layer as a parameter is shown in Fig. 3.5 (c and d). The calculations have been done using eqn. (3.19) and the steps are given below.

Let us consider Fig. 3.4(d) first.

- (a) The curve (i) with $W_p=0.0\text{A}^{\circ}$ is the same as that of the MIS cell given in Fig. 2.3a(ii). The material and the geometrical parameters that have been used in the calculation of Fig. 2.3a(ii) have been also used in the following.
- (b) The values of the doping N_a of the P layer and N_d of the N layer are taken to be 10¹⁶ cm⁻³ and 10¹⁵ cm⁻³ respectively. The width W_p of the P layer has been taken as a parameter and the values are shown in figure.
- (c) ϕ_B at V = 0 is taken from Fig. 2.3. $\Delta \phi_B$ is calculated using eqn. (3.5), (3.7) and (3.8) for V = 0.
 - (d) V_{OG} is calculated using eqn. (3.29).
- (e) Then \emptyset_B^* at $V=V_{OC}$ from eqns. (2.3) and (2.8) and also $\Delta\emptyset_B^*$ (V_{OC}) from eqns. (3.5), (3.7) and (3.8) are calculated.
- (f) Steps (d) is repeated to obtain V_{OC} for the new values of \emptyset_B^* and $\Delta \emptyset_B^*$.
- (g) Steps (e) and (f) are repeated until the desired accuracy is obtained.

Using this method the curves of Fig. 3.5(c) and (d) have been obtained. In Fig. 3.5(d) the values of W_p are low so that the limit of barrier height in crease due to P-N junction formation is not reached. In these cases one observes that V_{OC} increases with increasing W_p for all values of δ . But the initial rise of V_{OC} is still sensitive to the value of δ . Thus the advantages of insensitivity of V_{OC} to δ has not been achieved.

The plots (ii) and (iii) of V_{OC} in Fig. 3.5(c) are for larger values of $^{
m W}_{
m p}$, in which case it is apparant that the initial rise of \textbf{V}_{CC} has become less sensitive to δ as compared to the MIS cells; thus providing the technological advantages mentioned in the beginning of this section. But there is one more important point which should be noted here. As larger values of W_p are used, the limit of barrier height increase due to P-N junction formation is reached at lower values of δ (see point A on plot (ii) and point B on plot (iii) in Fig. 3.5(c)) thereby nulling the advantages of barrier height increase. A calculation of Voc beyond this point will not be meaningful. The analysis given above provides an explanation and elaboration of the experimental observation of Pai et al [1] that \textbf{V}_{OC} becomes insensitive to δ if MINP or (MIPN) structures, instead of MIS structure, are used. Let us reiterate that this is only true for low values of δ . Pai et al [1] have obtained the N layer of MINP structure by ion-implantating a group V impurity in P type substrate and have formed the metallic contact using titanium.

3.4 Summary

In this chapter the role of an oppositely doped interface layer in increasing the barrier height of a Schottky barrier diode has been considered. This property would be of use in almost all the devices where Schottky barriers are employed e.g. power diodes, microwave diodes, MesFets, solar

cells etc. However, the advantage of the increase of barrier height is only available until the minority carrier effects start dominating. These limitations have been discussed.

From the point of view of solar cells, Schottky barriers have two disadvantages. One is due to the low open circuit voltage. This can be obviated by the use of (MIS) solar cells or by using structures like MPN or MIPN. These have been subject-matters of the previous and the present chapters. The other disadvantage of the Schottky barrier solar cells, which is also present in the case of MIS, MPN, MIPN and analogous cells, is due to the presence of a thin metallic layer through which light may pass. Thus the metallic layers have to be chosen to meet the conflicting optical, electrical, mechanical and metallurgical requirements. A design of the cell, so that some of these stringent requirements are relaxed would be discussed in the next chapter.

CHAPTER 4

LATERAL SOLAR CELLS

In the previous chapters we have studied the Schottky barrier, MIS, MPN and MIPN solar cells. The difficulties inherent in them due to the presence of a thin metallic layer (70 A°) on the top has already been mentioned earlier. In particular, deterioration of these thin metal films due to temperature cycling in actual operation may seriously affect the durability of these cells, thereby more than offsetting the advantages offered by them. Recently, a modified structure for SBSC has been proposed by Green [1] in which the requirement of a thin metal film has been obviated by using the structure shown in Fig. 4.1. This structure is analogous to the grating type of photovoltaic cells proposed by Loferski et.al.[2] and analysed by other workers [3]. It consists of several unit cells, each one of which has an exposed region of semiconductor of width 2L and a metal strip of width 2B = (m-1)L. For brevity, the regions of width 2L and 2Bare called the lighted and the collecting regions respectively. Carriers are photogenerated in the lighted region and are laterally collected by the Schottky barrier in the collecting region. Hence this structure is designated as lateral SBSC. The intent of the present chapter is to

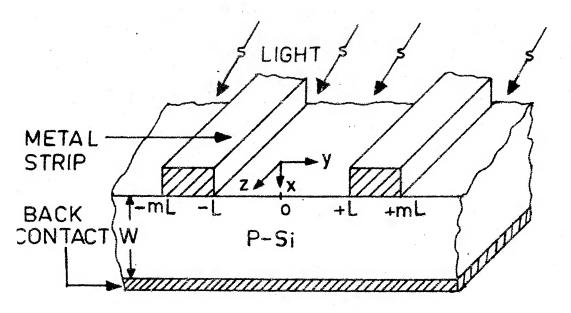


Fig.4.1 The schematic of lateral SBSC is shown. The width of the metal strip is 2B = L(m-1) and the extent of lighted region is 2L. The cell consists of several units like this where the metallic strips are connected together.

calculate analytically the short circuit current by solving a two-dimensional continuity equation and thereby obtain the efficiency of this cell. The calculated results show some interesting features. One of them is that the efficiency does not increase monotonically with increase in L/B as reported earlier [1]. As a matter of fact, it has been found that L/B is not a meaningful parameter for this cell, rather both L and B have to be separately specified for uniquely specifying the efficiency of the cell.

The calculation of efficiency proceeds in the following manner. The two dimensional continuity equation for the minority carriers in both the lighted and the collecting regions is first solved. This is done in the following section. These solutions are then used to obtain the spectral response, the short circuit current and the conversion efficiency of the cell.

4.1 Continuity Equation

In this section the profile of photogenerated minority carriers for the lateral SBSC, shown in Fig. 4.1 is determined. To do this let us consider the mechanism of collection in a lateral SBSC, bringing out the assumptions under which the present calculation has been done.

(i) Carriers are photogenerated in the lighted region.

In general, these are transported by drift and diffusion in the presence of recombination to the edge of the space charge

region (below the metal) which is formed due to the Schottky-barrier. However, if it is assumed [4] that the electrostatic field is confined entirely to the narrow space-charge region, even in the presence of photogenerated carriers, then the rate-controlling process in current flow is the diffusion of minority carriers. In order to ensure this field-free diffusion, the non-equilibrium concentration of minority carriers must always be much smaller than the equilibrium concentration of majority carriers. This low-level generation needed to neglect the drift component of transport, is obtained in the case of irradiation of silicon by uncentrated solar light. We confine our attention to this ease.

charge layer (below the metal) are transported to the metal by drift. Some of the carriers may also recombine in this region. We note, however, that [4] the width (W_{SC}) of this space charge region is negligibly small compared with the diffusion length (L) of minority carriers and with the width (W) of the cell. Typically, in a silicon solar cell W_{SC} is of the order of a few microns whereas L is of the order of a hundred microns and W is of the order of two hundred microns. Hence, on the scale of Fig.4.1, the edge of the space charge region below the metal has been taken at x=0 and any fringing of this region in the lighted region has been ignored. In other words, it has been assumed that all the photogenerated carriers

reaching the edge of the space charge layer are collected by the metal.

Under the assumptions given above the profile of photogenerated minority carriers (electrons), in the steady state, can be obtained by solving the two-dimensional continuity equations

$$D_{n}\left(\frac{\partial^{2} n_{j}}{\partial x^{2}} + \frac{\partial^{2} n_{j}}{\partial y^{2}}\right) - \frac{n_{j}}{\partial x^{2}} = F(x, \lambda)$$
 (4.1)

where for the lighted region $n_j = n_L$ and

$$F(x, \lambda) = -Q(\lambda) \alpha(\lambda) \exp[-\alpha(\lambda)x]$$
 (4.2)

whereas in the collecting region $n_j = n_c$ and F = 0. Here the reflection losses have been neglected and the quantum efficiency has been taken to be unity. The boundary conditions (BC's) in both the lighted and the collecting regions are given in Table 4.1. The cell has been considered to be short-circuited giving rise to the condition $n_C = 0$ at x = 0 in the collecting region. The determination of the BC's in the y-direction poses some problems. This is due to the fact that at y = L, -L, mL and -mL the BC's are not known. To obviate this, it is assumed that at these values of y one has $n_j = f(x)$, and the symmetry of the structure is utilized to put some restraining conditions given in Table 4.1. Use of these conditions allows one to solve eqn. (4.1) by standard method [5] as shown in Appendix C in terms of the coefficients which

Table 4.1 Table 4.1: Boundary conditions.

Serial Number	Boundary	Lighted Region	Collecting Region
(i)	x =0	$D_{n} \frac{\partial n_{L}}{\partial x} = Sn_{L}$	$n_{C} = 0$
		$(-L \le y \le L)$	$-mL \leq y \leq -L$
(ii)	x= W	$n_{L} = 0$ $(-L \le y \le L)$	$n_{C} = 0$ $(-mL \le y \le -L)$
(iii)	Boundary condition in y-direction	$n_{L} = f(x)$ at $y = +L$	$n_{C} = f(x)$ at y=-L and -mL
(iv)	Restraining condition	$\frac{\partial u}{\partial x} = 0$ at $x = 0$	$\frac{\partial n_{C}}{\partial y} = 0$ at $y = -(m+1)L/2$
(v)	Restraining condition	$\frac{\partial n_{L}}{\partial y} > 0$ at $y = -L$	$\frac{\partial u}{\partial x} > 0$ at $y = -L$
(vi)	Restraining condition	$\frac{\partial n_{L}}{\partial y} < 0$ at $y = L$	$\frac{\partial n_{C}}{\partial y} < 0$ at $y = -mL$

are to be iteratively determined. The solution in the collecting region is obtained as

$$n_{C}(x,y) = \sum_{q=1}^{\infty} C_{q} \sin(\beta_{q}x) \cosh(P_{q}(y+(m+1)L/2)/\cosh(P_{q}(m-1)L/2))$$
(4.3)

where β_q are obtained from the solution of $\beta_q W = n\pi$, n being an integer and $P_q^2 = \beta_q^2 + L_n^{-2}$. To determine the coefficients C_q 's in eqn. (4.3), one would need the solution of eqn. (4.1) in the lighted region.

The expression that satisfies eqn.(4.1) and the boundary conditions (ii), (iv), (v) and (vi) of Table 4.1 in the lighted region is:

$$n_{L}(x,y) = g_{1}(x)+g_{2}(x) - \sum_{p=1}^{\infty} B_{p} \sin x p(x-W) [\cosh Q_{p}y/\cosh Q_{p}L]$$
(4.4)

$$g_1(x) = A \sinh[(x-W)/L_h]$$

$$g_2(x) = \frac{Q(\lambda)\alpha(\lambda)}{D_n(\alpha^2 - L_n^2)} [\exp(-\alpha W) \exp[-(x-W)/L_n] - \exp(-\alpha x)]$$

$$Q_p^2 = X_p^2 + L_n^{-2}$$

where χ_p is the root of the equation:

$$\chi_p \text{ W Cot } \chi_p \text{ W + } (SW/D_n) = 0$$

The expression for A in $g_1(x)$ is obtained by substituting eqn. (4.4) in the boundary condition (i).

$$A = \{ Q(\lambda) \alpha(\lambda) / [D_n(\alpha^2 - L_n^{-2})] \} (R/T)$$
 (4.5)

where
$$R = [(D_n/L_n) + S] \exp [W(L_n^{-1} - \alpha)] - (S + \alpha D_n)$$

$$T = (D_n/L_n) \cosh(W/L_n) + S \sinh(W/L_n)$$

The coefficients of expansion B_p , in eqn. (4.4) are determined by using the boundary condition (iii) in the following way.

The coefficients of expansion B in eqn. (4.4) and C in eqn. (4.3) are determined as follows. At y=-L, one has $n_C=n_L=f(x)$, i.e.

$$\sum_{q=1}^{\infty} C_q \sin \beta_q x = g_1(x) + g_2(x) - \sum_{p=1}^{\infty} B_p \sin \chi_p(x-W)$$
 (4.6)

Multiplying both sides of eqn. (4.6) by $\sin \beta_n$ x and integrating between zero and W, we get:

$$C_n = (2/W) \left[-Z_1 + Z_2 (Z_3 - Z_4) - \sum_{p=1}^{\infty} (B_p \beta_n \sin \chi_p W) / (\chi_p^2 - \beta_n^2) \right]$$
(4.7)

where
$$Z_1 = A \beta_n [sinh(W/L_n)]/(L_n^{-2} + \beta_n^2)$$

 $Z_2 = Q(\lambda) \alpha(\lambda) \beta_n / [D_n(w^2 - L_n^{-2})]$
 $Z_3 = \{exp[W(L_n^{-1} - \alpha)] - (-1)^n exp(-\alpha W)\}/(\beta_n^2 + L_n^{-2})$
 $Z_4 = [1 - (-1)^n exp(-\alpha W)]/(\alpha^2 + \beta_n^2)$

Thus equation (4.7) provides a relation between \mathbf{C}_n and \mathbf{B}_p 's. An expression for \mathbf{B}_t in terms of \mathbf{C}_q 's is obtained by using the relation

$$\partial n_{j} / \partial y = \partial n_{C} / \partial y$$
 at $y = -L$

which gives

$$\sum_{p=1}^{\infty} B_p Q_p \sin x_p (x-W) \tanh(Q_p L) = \sum_{q=1}^{\infty} C_p P_q \sin \beta_q \times \tanh(P_q (m-1)L/2)$$
(4.8)

Multiplying both sides of eqn. (4.8) by $\sin\chi_{t}(x-W)$ and integrating between zero and W, we get

$$B_{t} = Z_{6} \sum_{q=1}^{\infty} (C_{p}P_{q}\beta_{q}\sin x_{t} W/[x_{t}^{2} - \beta_{q}^{2}]) \tanh [P_{q}(m-1)L/2]$$
(4.9)

where $Z_6 = -4 \times t / \{ (sin2 \times t W-2 \times t W)Q_t tanh [Q_tL] \}$

Equations (4.7) and (4.9) are iteratively solved to obtain the coefficients of expansion B_p and C_q in equations.(4.4) and (4.3) respectively. For the range of parameters for which the calculations have been done it has been found necessary during the numerical calculation to keep five terms in B_p and fourteen terms in C_q for reasonable accuracy.

Once these coefficients are known, one can obtain the short-circuit current. But before doing this, we would digress to consider the case when the surface recombination velocity in the lighted region at x = 0 is infinite, i.e., $n_{\rm L}$ = 0 at x = 0. Boundary condition (i) for the lighted region in Table 4.1, for infinite surface recombination velocity, changes to $n_{\rm L}$ = 0 at x = 0 for $-{\rm L} \le y \le {\rm L}$. The expression that satisfies eqn. (4.1) and the boundary conditions is given by

$$n_{L}(x,y) = g_{3}(x) + g_{2}(x) - \sum_{q=1}^{\infty} B_{q} \sin \beta_{q} \times \frac{\cosh P_{q}y}{\cosh P_{q}L}$$

$$\text{where } g_{3}(x) = A_{1} \sinh(\frac{x-W}{L_{n}})$$

$$(4.10)$$

and
$$A_1 = \frac{Q(\lambda)\alpha(\lambda)}{D_n(\alpha^2 - L_n^{-2})} \left[\frac{\exp(-\alpha W)\exp(W/L_n) - 1}{\sinh(W/L_n)}\right].$$

For infinite surface recombination velocity (i.e. for the case $n_L = 0$ at x = 0) the expansion of c_q can be obtained in closed form by using the boundary conditions:

$$n_C = n_L$$
 and $\frac{\partial n_C}{\partial y} = \frac{\partial n_L}{\partial y}$; at $y = -L$.

$$C_{q} = \frac{(2/W) [-Z_{1} + Z_{2}(Z_{3} - Z_{4})] \tanh P_{q}L}{(\tanh P_{q}L + \tanh P_{q}\frac{L(m-1)}{2})}$$

Thus in this case no iteration is required, this simple calculation has been used as a check on the trends that have been obtained in the general case of finite surface recombination velocity in the lighted region at x = 0.

Before concluding this section, it should be mentioned that recently Hu and Edelburg [3] have also solved the continuity equation (4.1). They have used a method of Fourier expansion and their analysis has been briefly summarized in Appendix D. There we have also summarized a difference equation technique which has been used by Loferski et.al.[2] to numerically selve eqn. (4.1).

4.2 Short Circuit Current

The short circuit current $I_{SC}(\lambda)$ of a unit cell is calculated using the expression for n_C from eqn. (4.3) as follows:

$$I_{SC}(\lambda) = qD_n \int_{-mL}^{-L} \frac{\partial n_C}{\partial x} \Big|_{x=0} dy \qquad (4.12a)$$

$$= 2qD_n \sum_{q=1}^{\infty} C_q (B_q/P_q) \tanh \{ P_q(m-1)L/2 \} \qquad (4.12b)$$

Here unit length in z-direction has been taken. Note that the symbol q has been used to denote charge of the electron as well as an index of summation. The derivative in the integral sign of (4.12a) should actually be evaluated at the edge of the depletion region in the collecting region rather than at x=0. However, the evaluation at x=0 has been done as a consequence of assumption (ii) of the previous section.

The spectral response of the unit cell as calculated from eqn. (4.2) is shown in Fig. 4.2 for $2B = 12 \mu$ m and $2L = 20 \mu$ m and 200μ m. The curve for $2L = 20 \mu$ m is shown for two values (10 and 10^4 cm/sec.) of the surface recombination velocity. The values of D_n , L_n and W for which the calculations have been done are also shown in Fig. 4.2. It is obvious from Fig. 4.2 that the surface recombination velocity at the front surface of the lighted region would play an important role in the performance of these cells.

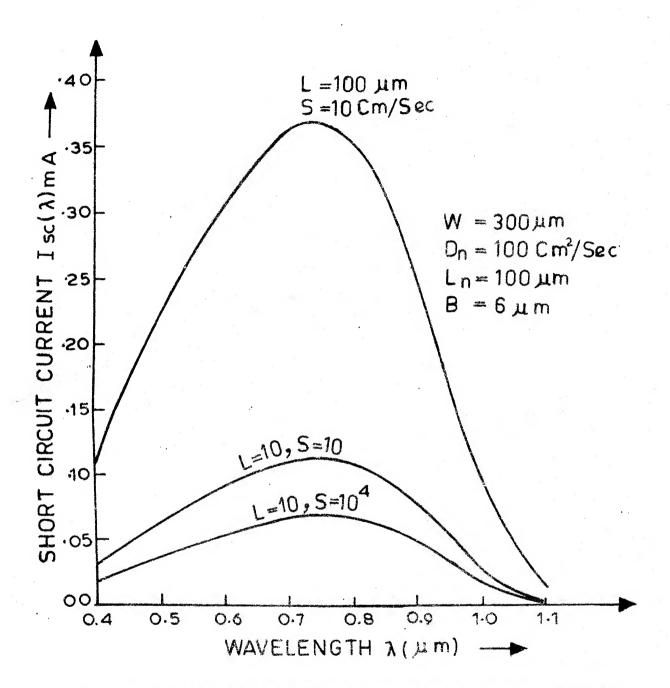


Fig. 4.2 Plot of the spectral response of lateral SBSC for $L=10~\mu m$ and $L=100~\mu m$ both for $B=6\mu m$. Note that the areas of unit cell with $L=10~\mu m$ and $L=100~\mu m$ are different.

To obtain the total short circuit current I_{SC} , of the unit cell, eqn. (4.12) is integrated for AMO sunlight using the data of Thekaekara[6]. A plot of I_{SC} versus the width 2B of the collecting region is shown in Fig. 4.3. Here L has been taken as a parameter for different plots. The values of D_n , L_n and W are the same as given in Fig. 4.2 and S=10cm/sec.

In the earlier literature [1], it has been implicitly assumed that I_{SC} is only dependent on L and not on B. This is at variance with the results shown in Fig.4.3 where I_{SC} is also dependent on B. This can be physically explained as follows. When B is zero, none of the photogenerated carriers are collected and obviously I_{SC} is zero. When B is small, for a given L, some but not all the photogenerated carriers are collected and I_{SC} increases. When B is sufficiently large so that all the photogenerated carriers can be collected, then any further increase in B does not increase I_{SC} .

So far we have considered L as fixed and have varied B. It is also of interest to consider the variation of I_{SC} with fixed B and varying L. This is shown as an inset in Fig.4.3. Initially, as L increases, I_{SC} increase because photogenerated carriers become available. Eventually I_{SC} saturates when L becomes of the order of or greater than the diffusion length of the minority carriers. These considerations of the results in Fig.4.3 and its inset would be of considerable help in explaining the behaviour of the conversion efficiency in the next section.

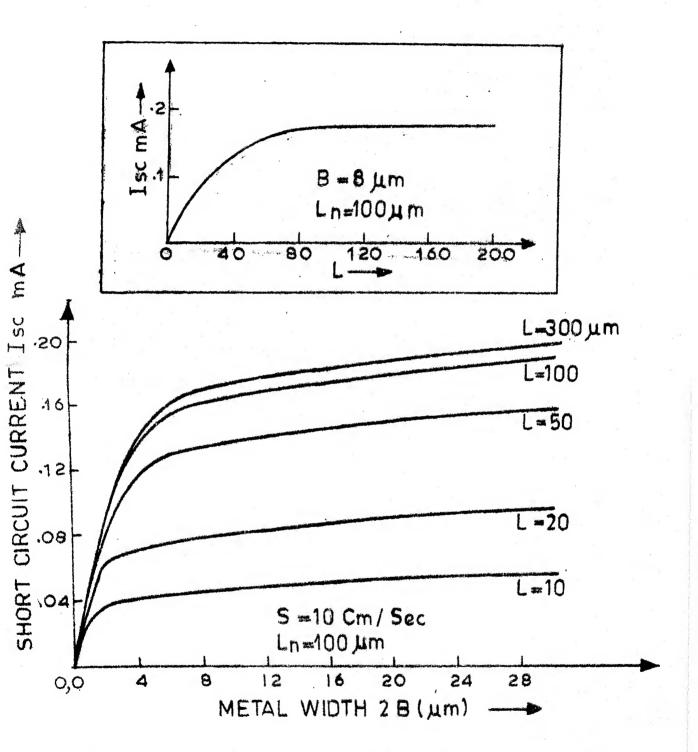


Fig. 4.3 Plot of the short-circuit current I_{SC} versus the width of metal for several values of L. In the inset I_{SC} versus L is plotted for a fixed B.

4.3 Conversion Efficiency

The conversion efficiency of the cell has been calculated in the conventional manner [7] as given in Chapter 1. The only care to be taken is that the area, for unit length in z-direction, for the calculation of the reverse saturation current per unit cell is 2B, whereas the total area of the unit cell is 2(L+B). Thus the conversion efficiency (7) at a load where maximum power is delivered is:

$$\eta = (V_{mp}I_{mp}) \text{ per unit cell/((P}_{in}2(L+B)))$$
 (4.13)

where for AMO solar radiation $P_{in} = 135.3 \text{ mw/cm}^2$. V_{mp} is obtained from the solution of the transcendental equation

$$\left(1 + \frac{qV_{mp}}{nkT}\right) \exp\left(\frac{qV_{mp}}{nkT}\right) = \left(1 + \frac{I_{SC}}{I_{S}}\right) \tag{4.14}$$

where the short circuit current I_{SC} has been calculated in Section 4.2, and

$$I_S = (2B) A^{**}T^2 \exp(-q \phi_R/kT)$$
 (4.15)

is the saturation current, per unit width, in the collecting region. The calculations have been done at room temperature and for P-type silicon where A** = 32 amp/cm²/°K². I_{mp} is the current of lighted SBSC at the voltage V_{mp} . The values of the barrier height \emptyset_B and the diode quality factor n which are needed for the calculation cannot be precisely

determined because they depend on the method of fabrication. Hence these have been treated as parameters and several calculations have been done. A plot of the efficiency versus the width of the metal strip 2B for various values of L is plotted in Fig. 4.4 for $\emptyset_{\rm R}=1.1$ eV and n = 1.0.

In order to design a lateral SBSC one would like to choose the optimum value of L and B. In this regard the following reatures of Fig. 4.4 should be noted:

1. For a fixed L and with increasing B, the efficiency increases. reaches a maximum and then falls off. The maxima is sharp for smaller values of L and broadens for higher value of L. It was thought earlier [1] that increasing L/B ratio would monotonically lead to higher efficiency. Thus for a given L one may think that it would be advantageous to reduce B as much as technologically feasible. Fig. 4.4 shows that this is only true in the region past the maxima; in the initial portion of the curves the behaviour is just the opposite. Thus, for a given L, there is a minimum value of B beyond which it should not be reduced even if technologically feasible. We consider that this is an important results of the present work. The general feature of this aspect of Fig. 4.4 can be understood by considering the variation of I_{SC} , I_{S} and 2(L+B) with increasing value of B. When B is zero the conversion efficiency is zero because Ign is zero. When B increases all the three quantities I_{SC} , I_{S} and 2(L+B) increase. Eqns.(4.13)

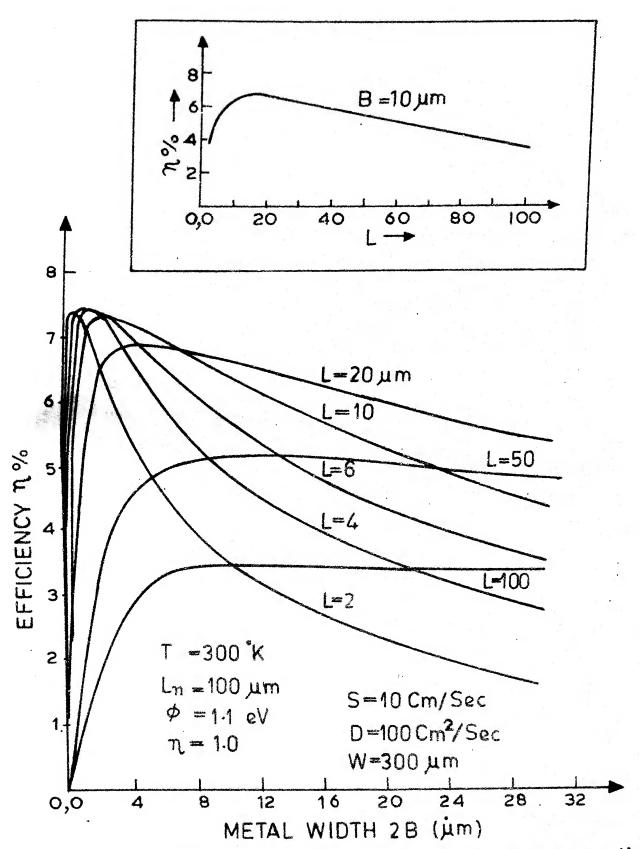


Fig. 4.4 Plot of the efficiency of the lateral SBSC versus the width of metal 2B = L(M_l), for several values of L.

The plot of the efficiency versus L for a fixed B is the inset.

and (4.14) show that an increase in I_{SC} is desirable whereas the increase in I_{S} and 2(L+B) lowers the efficiency. The variation of I_{SC} has been considered in Fig. 4.3 and shows a saturation, whereas both I_{S} and 2(L+B) increase linearly with B. These relative changes are such that the conversion efficiency, for a fixed L, shows a maxima as seen in Fig.4.4.

2. It is also of interest to consider the variation of efficiency with L. We confine our attention to that region of Fig. 4.4 where the efficiency decreases with increasing B. For a fixed B, the efficiency increases with increase in L, reaches a maximum and then falls off as shown in the inset of Fig. 4.4. The physical reason for this behaviour can be understood by considering the nature of variation of I_{SC} with L as given in the inset of Fig.4.3 and by noting that the area 2(L+B) of the unit cell increases linearly with L. It should be noted that again there is a region where the efficiency decreases with increasing value of L/B, thus for a given B there is an upper limit on L for obtaining maximum efficiency. Earlier we have seen that for a given L there is a lower limit on B for getting the best efficiency. In general, Fig.4.4, provides a guideline for the choice of L and B while designing these cells and it has to be used keeping the technological constraints in mind.

It is worthwhile to compare the efficiency of lateral SBSC with those of conventional Schottky barrier solar cells discussed in Chapter 1. Before doing this, it should be

Landsberg and Klimpke [8]) there is a very wide range of effeciencies that have been reported for these conventional cells. For example, theoretically calculated values of efficiency for conventional silicon SBSC range between 5% to 20%. Such a wide variation is due to the choice of barrier height, inclusion or neglect of recombination in the calculation, and similar other factors. Hence any comparison between the efficiencies of two different types of cells should be done, as far as possible under similar conditions. This is done below.

Let us consider the lateral SBSC shown in Fig. 4.1.

If the whole cell is covered by a very thin metallic coating instead of the gridded structure, then a conventional SBSC ensues. In this case the problem is one-dimensional and the solutions, taking recombination into account, have been given in Chapter 1. Considering all the relevant parameters to be the same as in Fig. 4.4 and assuming complete transmission through the thin metal film, the conversion efficiency of the conventional SBSC comes out to be approximately 6.5 percent.

A comparison of this value with those given in Fig. 4.4 shows that in some ranges the efficiency of lateral SBSC is larger than that of the conventional cell, The physical reason for this is as follows [1]. In the lateral SBSC the light available for photogeneration of carriers is less because of the presence of opaque metallic layers. Also the total

recombination for carriers is high because of the longer collection path. These factors lower the efficiency. However, the reverse saturation current of the Schottky barrier is also lower because of the reduced metallic area and this effect enhances the efficiency. Thus it is possible that in some range the lateral SBSC has higher efficiency than the conventional SBSC.

Before concluding this section, let us consider two more effects which are of interest in the fabrication of these devices. (a) As already discussed in Chapter 2, the inclusion of a thin interfacial layer in conventional SBSC which in effect forms a MOS solar cell, gives rise to increased efficiency. If this is done during fabrication of lateral SBSC also, it may be possible to obtain experimental values of efficiency which are higher than those of Fig.4.4. In this case, the theoretical calculation would have to be modified to account for the presence of the interfacial layer as shown in Chapter 2. (b) The efficiency of a lateral SBSC is dependent on the value of the surface recombination velocity (s) at the front face of the lighted region. Care should be taken to keep this value as low as possible.

4.4 Summary

The conversion efficiency of lateral SBSC has been calculated and guidelines to choose the geometrical parameters of this cell have been provided. The deleterious effect of

the surface recombination velocity has been pointed out. Perhaps the main advantage of these cells as compared to the conventional SBSC would not be in providing better efficiency but in their greater durability. In conventional cell a very thin homogeneous metallic film is required which should have good optical properties, a large barrier height and should adhere well to the semiconductor. There are all the chances that a thin metallic film which has different lattice constant and temperature coefficient of expansion than the substrate would catastrophically deteriorate when subject to periodic temperature cycling in actual operation. In case of lateral SBSC the metallic film can be made quite thick. even an intimate contact using silicides can be utilized. These would also improve the series resistance. In the light of these observations, it is expected that lateral SBSC would be more useful than the conventional SBSC in terrestrial applications.

CHAPTER 5

CONCLUSION

The photovoltaic properties of metal semiconductor (Schottky barrier) and related devices like:

- (i) Metal-(thin)insulator-semiconductor tunneling MIS diodes,
- (ii) Metal-(thin)P-N semiconductor and metal-(thin)N-P semiconductor devices.
- (iii) Metal-(thin)insulator-(thin)P-N and metal-(thin)insulator -(thin)N-P semiconductor diodes, and
- (iv) Lateral Schottky barrier solar diodes

have been studied in the previous chapters. An analysis of the short circuit current and the open circuit voltage for these cells has been given. From the knowledge of the complete I-V characteristics in the fourth quadrant (the fill factor) the efficiencies of the different cells can be calculated as has been demonstrated in some cases.

It has been pointed out that the temperature variation of the parameters of a solar cell are of importance from the point of view of actual operation of the cell. Therefore, the mechanisms that lead to this temperature variation have been studied. Attention has been first given to the study of temperature variation of the short-circuit current. It is commonly found that the short circuit current increases with temperature. Two mechanisms can be responsible for it.

- (a) The energy band gap in commonly used semiconductors decreases with increasing temperature. Due to this decreased band gap some more long wavelength photons are absorbed and photogenerate electron-hole pairs thereby increasing the short circuit current. Note that this excess of photocarriers is due to long wavelength photons which get absorbed deep into the base of the semiconductor. Hence, this mechanism would only be operative if the diffusion length of the minority carriers are exceedingly large.
- (b) The absorption coefficient of the semiconductor itself is a function of temperature and it increases with increasing temperature at all wavelengths in the case of silicon. Thus with increasing temperature, there is extra photogeneration of carriers at all the depths in the cell and this also causes the increase of short circuit current with increasing temperature. Since this mechanism is operative at all the sections of the cell, it would be important even in the case of materials with small diffusion lengths.

In actual situation, both the mechanisms mentioned above would contribute to the increase of short circuit current with temperature. However, in the case of a typical silicon solar cell, we have found that the contribution of the mechanism (a) is almost negligible. Since we have concentrated only on cells made of silicon, the above consideration is valid for all the cells studied in this thesis,

hence has not been given for each cell separately; rather the numerical results for only the Schottky barrier and lateral cells (Appendix D) have been given. Once the temperature variation of the short circuit current is known, that of the open circuit voltage can be computed by knowing the temperature variation of the ideality factor and the saturation current which depends on the barrier height. A review of the published literature has shown that the temperature variations of the ideality factor and the barrier height are extremely sensitive to the method of fabrication of the devices, hence the numerical computations have not been carried any further in th se cases.

A consideration of the Schottky barrier solar cells has shown that their biggest disadvantage is the low value of the open circuit voltage. This is obviated by using either the metal(thin)-P-N and analogous devices or tunneling MIS diodes. In the latter case one finds that both the open circuit voltage and the short circuit current, hence the efficiency are controlled by the thickness of the oxide-layer and fall when the thickness of the oxide layer exceeds a critical value.

An understanding of the mechanisms that cause these falls would suggest some methods to control the critical thickness mentioned above thus help in avoiding the low efficiency region. For example, it has been proposed that

the fall of the open circuit voltage for thicker diodes is primarily caused due to the decrease of the density-of-surface states with increasing oxide thickness in the case of MIS cells made on N type semiconductor. Thus if this fall is to be avoided the rate of decrease of the density-of-surface states with increasing oxide-thickness should be kept as small as possible. Similarly, the mechanism that controls the constancy of the short circuit current with oxide thickness is the split of imref of the minority carriers from the metal Fermi level, and this should be kept below a critical value by obtaining larger barrier heights, to keep the current constant.

The other mechanism to increase the open-circuit voltage is to interpose a thin oppositely doped semiconducting layer between the metal and the base semiconductor. This mechanism is of very general nature and its uses are not limited to photovoltaic devices only. If proper design is done, this technique provides a method for increasing the effective barrier height which is advantageous in most devices where Schottky barriers are employed. Some examples of such devices are Schottky gate, field effect devices, Schottky clamped transistors, etc. Hence, the methods developed for the design of increase of the barrier height in solar cells can also be used in the design of several other devices. For this purpose, the graph given in the text, showing the increase in the barrier height with the width

of the interfacial semiconducting layer and with the dopings as parameters can be utilized. Furthermore an analogous method can also be used by interposing a thin similarly doped semiconductor layer between the metal and the base semiconductor to obtain an effective decrease of barrier height. This aspect is of interest in designing the injecting and ohmic contacts. In the case of solar cells, injecting contacts are not interest, but a consideration for the understanding of the behaviour of ohmic contacts based on the above principle has been given. Lastly the effects of both a thin insulating layer and an oppositely doped semiconducting interfacial layer in increasing the barrier height have been amalgamated. The advantageous effect of this has been to reduce the sensitivity of the open circuit voltage on oxide thickness while keeping the value high.

In all the cells mentioned so far a very thin metal layer is required on the illuminated side so that the light can go through. The disadvantages of a thin metallic layer from the point of view of long-duration-operation of a solar cell under atmospheric conditions are obvious. It has been shown that a way of obviating this disadvantage is to use lateral cells. The analysis of these cells has required a two dimensional calculation. The results have shown that the efficiency of these cells are dependent on the choice of the areas of both the exposed region of the

semiconductor and the metallic collecting region. A design graph for this purpose has been plotted in the text.

From the summary of the work presented in the present thesis, we come to the following conclusions:

- (a) Schottky barrier solar cells are not promising because of their low open circuit voltage.
- (b) The potential of tunneling MIS solar cells has not been completely realized so far because these are complex devices, in as much as their performance depends on cumulative behaviour of several parameters which are simultaneously operative. There have been developments in this area, but as would appear, the role of all the parameters are not yet well understood. For example, the important role played by the variation of the density of surface states with oxide thickness has only been pointed out in this thesis. This makes it incumbent that different methods of oxide growth which give different variation of the -density-of-surface states on oxide thickness be experimentally investigated and the suitable one chosen.
- (c)Solar cells based on metal (thin)-insulator-(thin)-P
 -N semiconductor and analogous structures seem to be
 promising, but so far very little attention, both theoretically and experimentally, has been paid to these. The
 most advantageous features of these cells is that they keep
 the open circuit voltage high, but decrease the sensitivity

of the open circuit voltage on the oxide thickness as compared to MIS cells. Thus, these cells would be tolerant to less critical manufacturing processes than MIS solar cells.

(d) The manufacture of the lateral cells provide an advantage in as much as the choice of the metal for collecting junction only depends on the electrical and mechanical properties and not on the optical properties as in the case for all other cells considered above. Thus in the case of lateral cells using MIS contacts, the barrier height and the effective ideality factor would remain to be the ones in dark which is advantageous in most of the cases.

To conclude, it must be mentioned that none of the cells mentioned above can have an ideal maximum efficiency larger than the ideal maximum efficiency available in P-N junction solar cells. However, as mentioned in the beginning of this thesis the processing of P-N junction cells is expensive and there is a search on to locate viable alternative structures. We have presented some discussions in this direction in this thesis.

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APPENDIX A

LIST OF SYMBOLS

A**	Effective Richardson constant (Amp cm ⁻² o _K ⁻²)
a	Area of the cell (cm ²).
ъ	Width of the depletion layer (cm).
D_n, D_p	Diffusion constants of electron and hole, respectively (cm ⁻² /sec ⁻¹).
Ds	Density of surface states (states/cm ² /eV)
$\mathbf{E}_{\mathbf{G}}$	Band gap (eV).
kT	Thermal energy (ev).
L _n ,L _p	Diffusion lengths of electron and holes respectively (cm).
n	Ideality factor.
nj,np	Excess minority carrier (electron) concentration (cm ⁻³).
$_{ m M}^{ m G}$	Effective density of states in conduction band (cm^{-3}) .
N^{Λ}	Effective density of states in valance band (cm^{-3}) .
$N_{ extbf{A}}$	Acceptor impurity density (cm^{-3}) .
$^{ m D}$	Donor impurity density (cm^{-3}) .
P_{in}	Input radiation power density (W/cm^2) .
Q(\lambda)	Photon flux density (cm^{-2}/sec^{-1}) per unit wavelength (λ).
ď	Charge of the electron (coulomb).
S,s	Surface recombination velocity (cm/sec.)

```
\mathbf{T}
               Absolute temperature (°K).
v_{mp}(I_{mp})
               Voltage (current) for maximum power output
                (V(amp)).
qV_n
               Energy difference between conduction band
               and Fermi level (eV).
\mathfrak{q}^{\mathbb{V}_p}
               Energy difference between Fermi level and
               Valance band (eV).
               Open circuit voltage (V)
\Lambda^{\rm OG}
               Potential drop across the semiconductor (V)
v_{s}
               Potential drop across the insulator
Vi
              Width of the cell (cm)
W
               Free space permitivity (Farad/cm)
E 0
ε,
               Relative permitivity of the insulator
               Relative permitivity of the semiconductor
              Fixed charge in the oxide (Coulimb/cm<sup>-3</sup>).
              Oxide thickness (cm).
δ
              Absorption coefficient (cm<sup>-1</sup>).
α (λ)
\phi_{M}
              Workfunction of metal (eV)
              Barrier height (V).
ØR
              Electron affinity (eV)
 χ
              Potential drops across the oxide in thermal
 Δ
               equilibrium (V).
              Energy level at surface (V).
 Ø0
```

APPENDIX B

CHARGE RELATIONS IN SCHOTTKY (MIS) SOLAR CELL

In Chapter 2, while discussing the characteristics of Schottky (MIS) solar cell the expressions for the barrier height and for various charges were required. These are given here following an analysis of Landsberg and Klimpke (Proc. R. Soc. Lond., A 354, 101-118, 1977). The symbols used here are defined in Appendix A.

B.1 Charges Per Unit Area

Surface state charge: Let us first consider the surface state charge, Q_i in thermal equilibrium. This is given as

$$Q_{i} = q \left[\int_{0}^{\phi_{o}} D_{s}(1-f_{to}) dE_{to} - \int_{\phi_{o}}^{E_{G}} D_{s}f_{to} dE_{to} \right]$$
 (B.1)

where D_s is the density of surface states, E_{to} is the energy of a recombination level at the surface and f_{to} is the corresponding Fermi-Dirac distribution function. If the density of surface states D_s is constant then Q_i becomes

$$Q_{i} = qD_{s}kT \left[ln \left\{ \frac{1 + exp(q0_{B}/kT)}{1 + exp \left(q0_{B} - E_{G}\right)/kT} - \frac{E_{G}}{kT} \right] + qD_{s}0_{o}$$
(B.2)

Under illumination or when a bias is applied the MIS diode would be in non-equilibrium condition. In the case of low injection, the departure from equilibrium is not large and the system is said to be in quasi-equalibrium. A

quasiequlibrium distribution is completely specified by three quasi fermi levels associated with electrons, holes and the recombination level. Even for moderate departure from equilibrium the simplicity of quasi-equalibrium is lost and one has to consider recombination kinetics. The analysis of one-recombination- center model without trapping and for low-injection has been carried out in detail by Schockley and Read (Phys.Rev. 87, 835, 1952) and by Hall (Phys.Rev.87, 387, 1952) and is called the SRH theory.

They have obtained the expression for the probability of occupation of the recombination level as

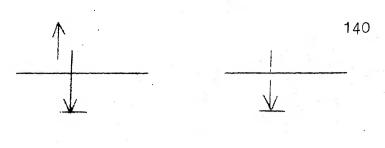
$$f_{t} = \frac{G(o)n(o) + H(o) p_{1}(o)}{G(o) [n(o)+n_{1}(o)] + H(o) [j(o)+p_{1}(o)]}$$
(B.3)

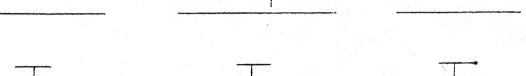
Here we have used the notation of Landsberg etal (Op.Cit.) n(o) and p(o) are, respectively, the electron concentration in the conduction band at the interface x=0 and the hole concentration in the valence band at the interface x=0; $n_1(o)$ and $p_1(o)$ are the electron and hole concentrations respectively, when the Fermi level is at the trap energy in thermodynamic equilibrium. G(o) and H(o) are given by

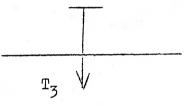
$$G(o) = T_1^{S} + T_1 n(o) + T_2 p(o)$$

$$H(o) = T_2^{S} + T_3 n(o) + T_4 p(o)$$
(. B.4)

where reaction constants T_1^s , T_2^s , T_1 , T_2 , T_3 and T_4 are defined in Fig. B.1 and their values are given in Table







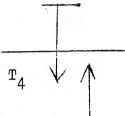


Fig.B.1

Definition of reaction constants occurring in eqn.(B.4). The surface state charge under illumination Q_i^* is given by

$$Q_{i}^{*} = q \int_{Q}^{E} D_{s} f_{t} dE_{t}$$
 (B.5)

In case, the tunneling from interface states to the metal are ignored, f_t in eqn. (B.5) can be obtained from eqn. (B.3). The resulting form of Q_1^* is:

$$Q_{i}^{*} = \frac{qD_{g}kT}{2} \left[ln \begin{cases} H(o)p_{o}(o)exp(-2q\emptyset_{B}/kT) + exp(-q\emptyset_{B}/kT) \\ (G(o)n(o) + H(o)p(o)) + G(o)n_{o}(o) \\ H(o)p_{o}(o)exp(2(E_{g}-q\emptyset_{B})/kT) + exp(q(E_{g}-q\emptyset_{B}/kT)) \\ (G(o)n(o) + H(o)p(o)) + G(o)n_{o}(o) \\ - \frac{(G(o)n(o) - H(o)p(o))}{(A-B)G(o)n_{o}(o)} ln \left\{ \frac{(exp(q\emptyset_{B}/kT) - A)(exp((q\emptyset_{B}-E_{g})/kT) - B)}{(exp(q\emptyset_{B}/kT) - B)(exp((q\emptyset_{B}-E_{g})/kT) - A)} \right\} \right] \\ + qD_{g}\emptyset_{0}$$
 (B.6)

With

$$\frac{A}{B} = -\frac{(G(o)n(o)+H(o)p(o))}{2G(o)n_{o}(o)} + [\{-\frac{G(o)n(o)+H(o)p(o)}{2G(o)n_{o}(o)}\}^{2} - \frac{H(o)p_{o}(o)}{G(o)n_{o}(o)}\}^{\frac{1}{2}}$$
(.B.7)

Although the general expression for calculations Q_1^* is given by eqn. (B.6), the lack of availability of experimental values of the reaction parameters and their variation with oxide thickness in both the cases of an 'illuminated' and 'biased' MIS diode, makes it difficult to obtain me ningful quantitative values. Here for the special cases of G(0) = H(0) expression for Q_1^* has been developed. The advantage of the approximation G(0) = H(0) is that the unknown recombination parameters cancel out. If we further make an approximation $\left[\frac{n(0)+p(0)}{2n_0(0)}\right]^2 >> \left[\frac{p_0(0)}{n_0(0)}\right]$, eqn. (A.B.6) reduces to:

$$Q_{i}^{*} = \frac{qD_{s}kT}{2} \left[\ln \left[\frac{\exp(q\emptyset_{B}^{*}/kT) + (p(o)+n(o))/n_{o}(o)}{\exp((q\emptyset_{B}^{*}-E_{g})/kT) + (p(o)+n(o))/n_{o}(o)} \right] - \frac{E_{g}}{kT} \right]$$

$$\left[1 + \frac{n(o)-p(o)}{n(o)+p(o)} \right] + qD_{s}\emptyset_{o} \qquad (B.8)$$

It is interesting to note that if p(o) >> n(o), then eqn.(B.8) simplifies to:

$$Q_i^* = qD_s \phi_o$$

Let us now consider the interface charge $\mathbb{Q}_{\hat{\mathbf{1}}}^{\hat{\mathbf{f}}}$ in the case that the diode is forward biased, but there is no

illumination. The expression for Q_i^f is the same as that of Q_i^* in eqn. (B.6) excepting that \emptyset_B^* should be replaced by \emptyset_B^f and n(o), p(o) should be accordingly calculated. Also note that the reaction constants would be different in the two cases.

Space charge in depletion region: The space charge is the depletion layer Q_{SC}^* is

$$Q_{SC}^* = qN_D^W = [2 \epsilon_S \ q \ N_D(V_b - V_S)]^{\frac{1}{2}}$$
 (B.10)

by the depletion approximation with $w = [(2_{s}/2N_{D})(V_{b}-V_{s})]^{\frac{1}{2}}$. In equilibrium $V_{s} = 0$ and Q_{SC} is given by

$$Q_{SC} = [2 \epsilon_{S} qN_{D} V_{b}]^{\frac{1}{2}} \qquad (B.11)$$

.B.2: Potential drops and Barrier Height

The potential drop $V_b - V_s$ across the depletion layer is given under illumination by

$$\Delta - V_{i} = \int_{-\delta}^{0} E_{i}(x) dx = \frac{\rho \delta 2}{2 \epsilon_{i}} + (Q_{i} + Q_{SC}) \frac{\delta}{\epsilon_{i}} \qquad (B.12)$$

Thus,

$$(\epsilon_{i}/\delta)(\Delta - V_{i}) = \frac{1}{2}\delta\rho + Q_{i} + Q_{SC}$$
 (B.13)

becomes in equilibrium, !

$$(\epsilon_i/\delta) \Delta = \frac{1}{2} \delta \rho_0 + Q_{i0} + Q_{SGO}$$
 (B.14)

Subtracting,

$$-(\epsilon_{i}/\delta)V_{i} = \frac{1}{2}(\rho - \rho_{0}) + (Q_{i}-Q_{i0}) + (Q_{SC}-Q_{SCO})$$
 (B.15)

Now from $\emptyset_B = \emptyset_M - \chi - \Delta$, (B.11), (B.2) and (B.13), the equilibrium barrier height is given by the solution of

$$\emptyset_{\rm B} = \emptyset_{\rm M} - \chi - \frac{\delta^2 \rho_{\rm o}}{2 \epsilon_{\rm i}} + \frac{D_{\rm s} \delta q}{\epsilon_{\rm i}}$$

$$[E_{G}-kT \ln \{\frac{1+\exp(q\emptyset_{B}/kT)}{1+\exp(\frac{q\emptyset_{B}-E_{G}}{kT})}\}] - \frac{\delta q^{2}}{\epsilon_{i}} \mathbb{D}_{s}\emptyset_{o}$$

$$-\frac{\delta}{\varepsilon_{i}} \left\{ 2 \varepsilon_{s} q N_{D}(\emptyset_{B} - V_{n}) \right\}^{\frac{1}{2}} \qquad (B.12)$$

The values of the parameter used in eqn. (B.12) are given in Table B.1. Also note the values of tunnel exponent used are given in Table B.2.

Table B.1: Data Adopted for MIS Solar Cell*.

		The state of the s		
Parameter	Numerical value	Dimensions		
\mathbf{E}_{G}	1.12	eV		
T	4.01 300	eV K		
$\ddot{\rho}_{O}$	3x10 ¹⁷ q	$.0^{\circ}\mathrm{cm}^{-3}$		
$T_1^S = T_2^S$	1.12x10 ⁻⁸	cm^3s^{-1}		
$T_1 = T_2 = T_3 = T_4$	3.66x10 ⁻²⁵	cm6s-1		
$A^{**} \simeq A_p^{**} \simeq A_n^{**}$	120	$A cm^{-2}K^{-2}$		
ε i	11.8 ε ο	F/cm		
ε	3.9 € ₀	F/cm		
$\mathbb{D}_{\mathbf{p}}$	12.5	cm^{-2} sec ⁻¹		
$\mathtt{L}_{\mathtt{p}}$	100	<u>um</u>		
$^{ m N}^{ m D}$	10 ¹⁵	_{cm} -3		
ni	1.6x10 ¹⁰	cm ⁻³		

^{*} Taken from Landsberg and Klimpke (Up.Cit.).

Table B.2: Tunnel Exponent $\chi^{\frac{1}{2}}$ δ

δ (A°)	5	10	15	20	25
χ ² δ	0	2 '	4	8	14

APPENDIX C

SOLUTION OF TWO DIMENSIONAL CONTINUITY EQUATION

C.1 Solution in Dark

Let the carrier concentration in the collecting region be $n_{\mathbf{C}}(\mathbf{x},\mathbf{y})$ where

$$n_{C}(x,y) = XY (C.1)$$

Let the separation constant be $\lambda = \pm \beta^2$. Then one obtains:

$$\frac{1}{X} \frac{d^2X}{dx^2} = \pm \beta^2 \tag{C.2}$$

$$\frac{1}{Y} \frac{d^2 Y}{dy^2} - \frac{1}{I_h^2} = \pm \beta^2$$
 (C.3)

It can be easily checked that for $\lambda = \beta^2$ there is no solution for eqn. (C.2). For $\lambda = -\beta^2$, we have

$$X = \tau \cos \beta x + \tau^{\dagger} \sin \beta x \qquad (C.4)$$

$$Y = C \exp \{ \sqrt{P} x \} + D \exp \{ -\sqrt{P} x \}$$
 (C.5)

where

$$P = \frac{1}{L_h^2} + \beta^2 \tag{0.6}$$

Use of B.C.'s X = 0, at x = 0 and W shows that the solution of eqn. (C.4) is

$$X = \sum_{q=1}^{\infty} \tau^{q} \sin \beta_{q} x \qquad (C.7)$$

Use of the B.C.'s $dn_{C}/dy = 0$ at $y = -\frac{L}{2}(m+1)$ shows that

$$Y = K \frac{\cosh[\sqrt{P} \{ y + \frac{L}{2}(m+1) \}]}{\cosh[\sqrt{P} \frac{L}{2}(m-1)]}$$

where $K = D \exp(\sqrt{P} \frac{L}{2}(m+1)) \cosh(\sqrt{P} \frac{L}{2}(m-1))$

It has been checked that the complete solution in the collecting region, i.e. $n_{\mathbb{C}}(x,y)$ is obtained as the product of (C.7) and (C.8) and is given as eqn. (4.3) of the main text.

C.2 Solution in the Lighted Region

Let the carrier concentration in the lighted region be $n_{T_i}(x,y)$ and expressed as

$$n_{T_1}(x,y) = X_1(x) Y_1(y)$$
 (C.9)

In this case let the separation constant be $\lambda=\pm\chi^2$. It can be shown that for $\lambda=\chi^2$ there is no solution. In the case $\lambda=-\chi^2$ one obtains

$$X_1(x) = A \cos x + B \sin x x$$
 (C.10)

$$Y_1(y) = E \exp (\sqrt{y}) + F \exp(-\sqrt{Q}y)$$
 (C.11)

Use of B.C. $X_1 = 0$ at x = W, gives from eqn. (C.10)

$$A = -B \tan \chi W \qquad (C.12)$$

Use of $D_1 \frac{dX_1}{dx} = SX_1$ at x = 0 gives for $B \neq 0$

$$\chi \cot \chi W = -S/D_{h} \tag{0.13}$$

The use of B.C.;
$$\frac{dY_1}{dy} = 0$$
 at $y = 0$ gives
$$E = -F \tag{C.14}$$

Note that eqn. (C.13) has multiple solutions. Use of this fact and eqn. (C.12) and (C.14) in (C.10) and (C.11) gives the third term of the solution of $n_L(x,y)$ as given in eqn. (4.4) of the main text.

The terms $g_1(x)$ and $g_2(x)$ of eqn. (4.4) are obtained as follows. When $\lambda = 1/L_h^2$, one has the solution $g_1(x)$ of eqn. (4.4). The term $g_2(x)$ is the particular integral due to inhomogenuity of the continuity equation. We have guessed the particular integral to be of the form:

$$g_{2}(x) = \frac{Q(\lambda)\alpha(\lambda)}{Dh(\alpha^{2} - L_{h}^{-2})} \{A_{3} \exp[(-x+b)/L_{h}] - \exp(-\alpha(\lambda)x)\}$$
(C.15)

Using the boundary conditions, $g_2(x) = 0$ at x = W, in eqn.(C.15) we obtain the $g_2(x)$ of eqn.(4.4) of the main text.

AP1 ENDIX D

ALTERNATIVE ANALYSES OF LATER CELLS

D.1 Analysis of Lateral Cell by Fourier Series Expansion:

In a recent paper [Solid St.Electronics, 20,119,1977], Hu and Edelburg have analysed the lateral cell structure of using the technique of Fourier series expansion instead of "boundary matching" as has been done by us in the previous sections. We summarize, in the following, the relevant portion of the analysis of the Hu et al so that a comparison with the "boundary matching" can be done.

The differential equation in the two cases is the same, as given by eqn. (3.1). However, the boundary conditions that have been utilized are different, in as much as, in Hu's analysis, the B.C. number (iii) in Table 3.1 is not needed. Also note that we have analysed the structure based on a P-type semiconductor, whereas Hu etal have done it for N-type semiconductor. Their solution is written for holes which are the minority carriers.

The solution is expressed as sum of particular solution $\mathbf{p}_{\mathbf{p}}$ and the homogeneous solution $\mathbf{p}_{\mathbf{h}^*}$. The solution $\mathbf{p}_{\mathbf{p}}$ is given by

$$p_{p} = \tau \alpha Q \sum_{m=0}^{\infty} \frac{e^{-\alpha d} u_{m} + C_{m} (1 - e^{-\alpha d}) \cos \lambda_{m} y}{1 - L^{2} \alpha^{2} + L^{2} \lambda_{m}^{2}}$$
(D.1)

where L is the diffusion length in centimeters, $\lambda_{m} = m\pi/(L+B)$,

$$u_0 = 1$$
 and $u_m = 0$ for $m \neq 0$,

$$G_0 = \frac{b-a}{b};$$
 $G_m = -(\frac{2}{L+B}) \frac{\sin(B \lambda_m)}{\lambda_m}$

$$W_{m} = e^{-\alpha x} - \cosh \beta_{m} x + \left(\frac{\cosh \beta_{m} W - e^{-\alpha W}}{\sin \beta_{m} W}\right) \sinh \beta_{m} x$$

where
$$\beta_{m} = \left(\frac{1}{L^{2}} + \lambda_{m}^{2}\right)^{\frac{1}{2}}$$

and d is the thickness of metal stripes.

The related homogeneous solution is obtained by the technique of eigenfunction expansion,

$$p_{h} = \sum_{m=0}^{\infty} A_{m} \sinh\{\beta_{m}(W-x)\} \cos y / \sin \beta_{m} W \qquad (D.2)$$

where the A_m 's are the Fourier series coefficients of the excess hole concentration along the boundary x=0 and A_m 's are given by the following expression.

$$\begin{split} A_{m} &= C_{m} \left\{ A_{o} R_{o} + \frac{Q_{o}}{S} \left[e^{-\alpha d} + C_{o} (1 - e^{-\alpha d}) \right] \right\} \\ &+ (1 - u_{m}) (C_{o} + \frac{1}{2} C_{m}) \left[A_{m} R_{m} + (1 - e^{-\alpha d}) \frac{Q_{m} C_{m}}{S} \right] \\ &+ (\frac{1}{2} - \frac{1}{4} u_{m}) \sum_{\substack{j=1 \\ j \neq m}}^{\infty} (C_{m+j} + C_{m-j}) \left[A_{j} R_{j} + (1 - e^{-\alpha d}) \frac{Q_{j} C_{j}}{S} \right] \\ \text{where } R_{m} &= -(D/S) \beta_{m} \coth \beta_{m} W \\ Q_{m} &= \frac{QL^{2}}{1 - L^{2} \alpha^{2} + L^{2} \lambda_{m}^{2}} [\beta_{m} (\frac{\cosh \beta_{m} W - e^{-\alpha} W}{\sinh \beta_{m} W}) - \alpha \right] \quad (D.4) \end{split}$$

Note that eqns.(A.5) and (A.7) in Hu etal's paper have algebraic errors which have been pointed out by us and the corrected form is given in eqn. (D.3) and eqn. (D.4). The infinite set of equations (D.3) is modelled as a system of m simultaneous equations to be solved for the m lowest order Fourier series coefficients A_m . At least m = 70coefficients were needed by Hu etal for reasonable accuracy. Once the solution for the minority carriers are obtained, the calculation of efficiency etc. in the two methods is similar hence would not be discussed again. Thus so far, the comparison of the two methods is concerned it is to be only done from the point of view of ease of numerical computation in obtaining the minority carrier profile. Our experience shows that solving for several simultaneous equations would definitely be more horrendous than the computations needed in the "boundary matching" methods. Before concluding this section we would also like to point out that though the surface recombination velocity at the exposed part of the semiconductor has been incorporated in the analysis of Hu etal, its physical significance has not been explored at all nor have been the design aspects emphasized, keeping an appreciation of the operative physical mechanisms in view.

D.2 Numerical Analysis of Lateral Cell

The disadvantages of a dead layer on the top surface of a P-N junction solar cell were noticed by many workers but perhaps the first method of obviate this was proposed by Loferski etal [Technical Report NGR-40-002-093/2 to the National Aeronautics and Space Administration, June 1975]. His suggestion was to use a grating structure where "unlike a standard diffused cell which has its front surface covered completely by a thin diffused skin region, a grating type cell would have part of its front surface covered by a grating of finely spaced fine grid lines which form a potential barrier with the base substrate. The grating structure junction could be a diffused P-N junction, an alloyed P-N junction or a Schottky barrier junction". Thus we see that Loferski's grating structure is the one which we have called the lateral cell. He has set up the two dimensional continuity equation which is the same as our eqn.(3.1) and has solved it numerically by using finite difference technique. For the solution of the simultaneous equations he has used the successive overrelaxation method. As is well known, the disadvantage of a numerical method as compared to an analytical solution is that each problem has to be solved on its own and general design guidelines cannot be obtained. Hence we feel that the analytical method given in Section 3.1 would be more convenient than the numerical method given by Loferski.

D.3 Lateral Schottky barrier Solar Cell - Simplified Model.

The analysis of lateral SBSC given in the previous section requires computation of the matching coefficients B_p 's and C_q 's which, though rigorous, is time consuming. In many cases, it would be desirable to develop an approximate analysis which is computationally simple. Such an analysis of the lateral SBSC is provided in this section. The simplification is brought out by the fact that in this case no iteration is required while solving for B_p 's and C_q 's.

The method consists of solving the continuity equation in the collecting region as done in the previous section and of modifying the continuity equation in the lighted region as follows:

$$D_{n} \frac{d^{2}n_{L}}{dy^{2}} - \frac{n_{L}}{\tau_{n}} = -Q \alpha e^{-\alpha x}$$
(D.5)

Here the diffusion component in the x-direction has been neglected. Hence the boundary conditions (i) and (ii) in the lighted region in Table 3.1 are not required. The solution of eqn. (3.16) is obtained as

$$n_{L} = 2A_{1} \cosh \frac{y}{L_{n}} + \tau_{n} Q \alpha e^{-\alpha x}$$
 (D.6)

where A1 is the coefficient to be determined later.

In the collecting region the solution of the two dimensional continuity equation is given by eqn.(4.3) as in Section 4.1.

Using the condition that y=-L, $n_C=n_L=f(x)$ and $\partial n_C/\partial y=\partial n_L/\partial y$, the coefficient C_q 's, and A_1 can be expressed as

$$U_{n} = \frac{2\tau_{n} Q\alpha \{\beta_{n} (1-(-1)^{n} e^{-\alpha W})\}}{W(\alpha^{2}+\beta_{n}^{2}) \{1+P_{n}L_{n} \tanh(\frac{P_{n} (m-1)L}{2}) \coth \frac{L}{L_{n}}\}}$$
(D.7)

and

$$A_{1} = -\frac{L_{n}}{2\sinh(L/L_{n})} \sum_{q=1}^{\infty} C_{q} \sin(\beta_{q} x) P_{q} \tanh(P_{q} \frac{m-1}{2} L)$$
(D.8)

Once the coefficients ${}^{\text{C}}_{\mathbf{q}}$'s are known the expression of short circuit current is given by

$$I_{SC}(\lambda) = \frac{4q \ Q \alpha \ L_n^2}{W} \sum_{q=1}^{\infty} \frac{\beta_q^2 \{ 1 - (-1)^n \ e^{-W} \} \tanh \{ \frac{P_q B}{2} \}}{P_q(\alpha_+^2 \beta_q^2) \{ 1 + L_n P_q \tanh(\frac{P_q B}{2}) \tanh \frac{L}{L_n} \}}$$
(D.9)

Note that the symbol q has been used to denote charge of the electron as well as an index in the summation. The particular use is clear from the context.

The plot of I_{SC} for AMO sunlight versus the width of the metal stripe for several values of L is shown in Fig. D.1. In the calculation of eqn.(D.9), fourteen terms in the summation have been taken. The following points regarding the plot of Fig. D.1 should be noted.

- (1) It is worthwhileto compare the results of the approximate model as given in Fig. D.1, with those of two dimensional calculation given in Fig.4.3. One notes that the basic trend of the results in the two cases is the same. However, the numerical values are different and the amount of variation is given later. Here we only want to point to a general trend that is always present. This is that the value of I_{SC} found from the approximate calculation is always less than that from the two dimensional calculation. The reason is the use of one dimensional continuity equation in the lighted region. In this case the effective length that the carriers have to traverse before collection is increased, thereby increasing the chances of recombination thus lowering the short circuit current.
- (2) The amount of difference between the graph of Fig.4.3 and Fig. D.1 depends upon the values of L and B being considered. One finds that for L > 50 µm for the whole range of B, the difference between the two calculations is less than 20%. In case one is only interested in getting an approximate idea but with lots less numerical effort it is obvious that the approximate method leading to Fig.4.3 would be more convenient than the two-dimensional analysis. For example, one such use can be envisaged when one is interested in studying the temperature variation of the short circuit current as mentioned in Chapter 1.

Such calculation of variation of I_{SC} with temperature using the expression for the absorption coefficient given in eqn.(1.21) for silicon, is given in Fig. D.2.

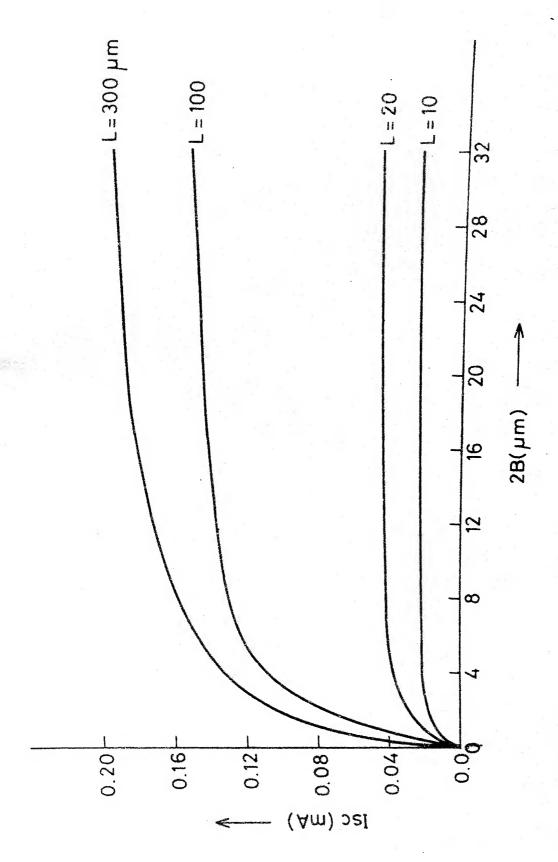


Fig. D.1 Plot of the short circuit current Isc versus the width of metal finger for several values of L.

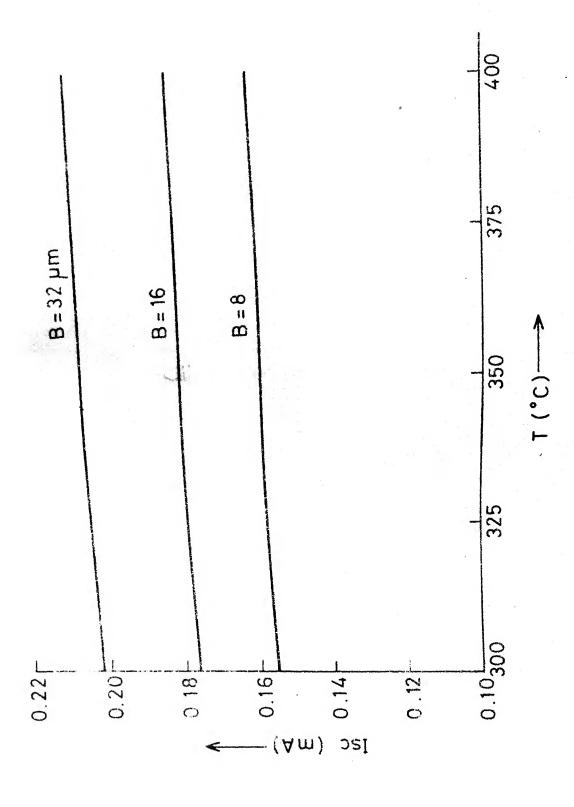


Fig. D.2 Temperature variation of short circuit current with L=300 µm and B as a parameter.

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